

Nothing Original Need Survive

Origin, Continuation, and the Geometry of Descent

Card's Originism, Zebrowski's *Macrolife*, Le Guin's *The Dispossessed*, and the Problem of Historical Continuity

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What makes a later thing a continuation of an earlier one when the material, location, representation, and even the recoverable record of the earlier thing may all have changed? Conversely, what can a present record establish about an origin that no longer survives? These questions are often separated into problems of historical knowledge, personal or collective identity, archival reconstruction, and persistence through change. This essay argues that they share a common structural difficulty. States do not, in general, contain enough information to determine the histories by which they arose.

Three works of speculative fiction provide unusually severe probes of this difficulty. Orson Scott Card's "The Originist" approaches it retrospectively: a present assembled from incomplete records is used to reason toward an absent origin. George Zebrowski's *Macrolife* approaches it prospectively: civilization persists by becoming increasingly independent of its original material and planetary conditions. Ursula K. Le Guin's *The Dispossessed* introduces a third operation, return, in which departure and recurrence reveal that neither an origin nor the agent returning to it remains simply identical with its earlier state.

The resulting argument moves from states to trajectories, from trajectories to provenance structures, and from provenance to constraints on admissible continuation. These distinctions are then related to the author's existing work on the Relativistic Scalar–Vector Plenum (RSVP), TARTAN, Chain of Memory, Spherepop, irreversibility, and the No-World argument. The governing claim is simple but its consequences are not: continuity is not adequately represented as a relation between states. It is a property of histories, and histories themselves may branch, converge, become partially unrecoverable, or cease to support the continuation of a world even where some descendant structure survives.

The document's citation and typographic apparatus participates in this argument. Claims may carry provenance indices recording direct inspection, known reconstruction depth, or unresolved derivational history. These indices do not represent

truth values. They record a different coordinate of knowledge: how a statement reached the present document.

PREFACE: WHAT IT MEANS FOR SOMETHING TO CONTINUE

Most questions about whether something has survived appear easy until the survival is imperfect. A book remains the same book when it is moved from one shelf to another. A city remains the same city after a building is demolished. A person remains the same person after replacing the cells from which much of the body was once composed. A language remains recognizable despite the death of every speaker who spoke it several centuries ago. In ordinary life these judgments rarely require a theory. We inherit conventions about which changes matter and which do not, and those conventions usually work well enough.

Difficulty begins when several kinds of continuity separate.

A copied file may contain exactly the same bytes as another file while having a completely different history. A damaged manuscript may be reconstructed so successfully that the reconstructed passage is indistinguishable from the lost one, even though the passage now before us was produced by an editor rather than transmitted continuously from the earlier document. A ship may preserve its name, function, crew, route, and institutional identity while every piece of its material is gradually replaced. A civilization may survive the destruction of its home planet while changing its bodies, habitats, technologies, and forms of social organization. Conversely, a civilization may retain buildings, names, and institutions while losing so much of the relational structure that once constituted its world that calling the result the same civilization begins to conceal more than it explains.

The ordinary word “same” performs too many jobs in such cases.

This essay begins from the suspicion that many apparent puzzles of identity are produced by asking states to answer questions that only histories can answer. If two objects presently look alike, their present similarity does not tell us whether one descended from the other, whether both descended from a common source, whether they were produced independently, or whether one was constructed specifically to imitate the other. Likewise, present difference does not establish historical discontinuity. A descendant may differ radically from its ancestor precisely because an unbroken process of adaptation connected them.

The distinction is elementary in ordinary experience. Finding two identical handwritten notes on a table does not establish that they were written by the same person. Discovering that one note was copied from the other changes what we know about their relationship without changing either note. Discovering instead that both were independently copied from a third note changes the relationship again. Nothing about the visible sentences needs to change while our account of what those sentences are evidence of changes substantially.

The same difficulty appears at much larger scales.

In Card’s “The Originist,” the problem points backward. Surviving evidence must support claims about an origin that is no longer directly available. Originism therefore concerns more than the storage of records. It concerns the relations among records and the histories through which present evidence became available.

In Zebrowski’s *Macrolife*, the problem points forward. Survival ceases to mean preserving a fixed material arrangement and increasingly means maintaining a viable continuation through transformations that may eventually leave little of the original substrate intact.

Le Guin's *The Dispossessed* complicates both directions. Departure is followed by return, but return does not restore an earlier state. The traveler has changed, the place of return has continued to develop, and the origin itself turns out to have an origin. The apparently simple line connecting departure and return therefore opens into a history of boundaries, inheritances, institutional transformations, and branching transmissions.

These literary works will not be treated as authorities from which an ontology can simply be extracted. They are useful because they produce difficult cases. Each forces a distinction that a simpler representation would prefer not to make. Their role in the argument is therefore closer to the role of a counterexample in mathematics than to the role of evidence in literary history.

The formal apparatus will be introduced in the same manner. No distinction will be retained merely because it permits an attractive symbol. A new relation earns its place when two cases that must remain distinguishable would otherwise collapse into one. Conversely, when two histories can safely be treated as equivalent for a particular purpose, the equivalence will be stated with respect to that purpose rather than elevated silently into identity.

This last qualification is important. Mathematics obtains much of its power from forgetting differences. Objects are identified up to isomorphism, homeomorphism, gauge transformation, or some other equivalence precisely because the discarded differences are irrelevant to the question under study. Nothing in the present argument opposes abstraction as such. The concern is narrower: a distinction should not be discarded before one has established that the operations to be performed later do not require it.

The central danger is therefore not forgetting.

It is forgetting that one has forgotten.

This is the point at which provenance becomes more than bibliographic bookkeeping. Provenance records which distinctions have survived a sequence of transformations and which have not. A claim may remain true while its provenance becomes uncertain. A reconstruction may reproduce an original perfectly while remaining a reconstruction. A descendant may preserve an invariant without preserving the path by which that invariant was transmitted. A world may leave traces from which some of its structure can be reconstructed without thereby becoming recoverable as the world that produced those traces.

The argument that follows will therefore resist a premature declaration of what its fundamental object must be. It may prove sufficient to speak of trajectories. Branching histories may require graphs. Questions of admissible continuation may require trajectories together with constraints. Questions of worldhood may force another extension. The stopping condition is not that every possible distinction has been represented. Such a condition could never be met. The argument closes when the examples under consideration cease to force an enlargement of the kind of object required to represent them.

Closure, in other words, will itself be treated historically.

A NOTE ON PROVENANCE

The superscripts used in this essay should not be read as confidence scores.

A claim marked ^[0] indicates that, for the purpose for which the claim is being used, the relevant wording or evidence has been inspected directly in the source identified by the accompanying citation. A claim marked ^[?] indicates that some relevant part of its derivational history has not yet been established. Further distinctions will be introduced only when the argument requires them.

Thus the notation

$$\varphi^{[0]}$$

does not mean that φ is certainly true, while

$$\psi^{[?]}$$

does not mean that ψ is probably false. Directly inspected sources can contain errors. Claims of uncertain provenance can be true. The superscript records a relation between the present statement and the evidence through which it entered the argument.

The distinction can be expressed provisionally as

$$\text{Truth}(\varphi) \neq \text{Prov}(\varphi).$$

At this stage, however, the notation should be understood in the ordinary language just given rather than treated as a developed formal system. One of the purposes of the essay is to determine how much structure such a system actually requires.

The document also distinguishes ordinary editorial footnotes from provenance-bearing notes. A footnote may clarify a term, supply historical context, or acknowledge a complication without making a claim about the derivational depth of the sentence to which it is attached. Provenance is therefore not silently identified with citation.

The distinction will matter later.

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MOVEMENT I. ORIGIN

Can the past be recovered from its traces?

There is an ordinary sense in which finding an origin means finding a place. A family comes from a town, a manuscript comes from an archive, a species comes from an ancestral population, and a civilization comes from somewhere. If the place can be identified, the problem appears to be solved.

But origins become more difficult when the thing that began no longer exists in a recoverable form. Suppose the first settlement has disappeared, its records have been copied and recopied, its descendants have migrated, and the stories told about it have been reconstructed from fragments. Finding a plausible location would then answer only one question among many. We would still want to know which present traces actually descend from the lost settlement, which merely resemble its traces, which have been reconstructed, and which principles of organization persisted after the original material vanished.

Orson Scott Card's "The Originist" is useful because it begins inside this difficulty. Its subject is ostensibly the origin of humanity, but its deeper problem is the status of evidence after the origin has receded beyond direct inspection. The originist cannot simply look backward. The originist must reason through what survived.

1.1. *The Originist's Problem*

Orson Scott Card's "The Originist," first published in the anthology *Foundation's Friends*, places Lyle Forska within Isaac Asimov's Foundation universe during the period surrounding Hari Seldon's work on psychohistory [1]. The story inherits the scale of Asimov's Galactic Empire while directing attention toward a comparatively narrow scholarly problem. Lyle is concerned with human origins: not merely with the location from which humanity began its expansion, but with the reconstruction of the conditions and processes under which recognizably human civilization emerged.

The distinction matters. A search for a planet and a search for an origin are not necessarily the same search.

If the problem were merely geographical, originism could in principle terminate at a coordinate. Let E denote Earth and let $p(E)$ denote its location. The successful recovery of $p(E)$ would then settle the relevant question. Yet a coordinate says almost nothing about why the civilization whose descendants now occupy the Galaxy developed there, which inherited structures distinguish genuine descent from later resemblance, or which features of contemporary humanity carry information about the conditions of its emergence.

The geographical question has the schematic form

Where was O ?

whereas the originist's question is closer to

What can the present establish about *O*?

These questions coincide only under unusually favorable archival conditions.

Card's originism is therefore valuable here not because the fictional discipline supplies a ready-made philosophy of provenance. It does not. Rather, the story dramatizes a circumstance in which an origin has become epistemically remote while remaining causally indispensable. Humanity must have had an earlier history. The loss of direct access to that history does not remove it from the causal ancestry of the present. What disappears is something more specific: the ability to move without difficulty from present evidence to a unique account of how the present arose.

That is the first asymmetry on which this essay depends.

The past can determine the present without the present uniquely determining the past.

1.2. *The Library and the Scholar*

The Imperial Library gives this asymmetry an institutional form. A library preserves records. An originist does something different with them.

This distinction can initially be stated without mathematical machinery. Imagine that an archive possesses a document copied two thousand years ago from another document that no longer survives. The archive's task is satisfied, in one important sense, by preserving the surviving copy. It can record where the copy is stored, when it entered the collection, what material it is written on, and perhaps what earlier catalogues said about it.

None of this by itself establishes the entire history of the text.

The scholar asks questions that the shelf cannot answer. Was the surviving document copied faithfully? Was its source itself a copy? Were passages silently repaired? Did two apparently independent documents derive from a common intermediary? Does a sentence preserve ancient wording, or is it a later reconstruction that happened to become canonical?

The difference is sufficiently important to give the two functions names.

Definition 1.1 (Archivist). An *Archivist* is an agent or process whose primary operation is the preservation and retrieval of available states together with whatever explicit metadata accompanies them.

Definition 1.2 (Originist). An *Originist* is an agent or process whose primary operation is reasoning about the derivational histories by which available states may have arisen, including distinctions that are not recoverable from the states considered in isolation.

The capitalization is deliberate. These definitions do not purport to define Card's fictional profession exhaustively. They name two computational roles that the literary case makes unusually easy to separate.

The Archivist asks, in effect,

What survives?

The Originist asks

How did what survives get here?

An ideal institution may perform both operations. Indeed, Card's setting is interesting precisely because the Library and the scholarly practice of originism place them in close proximity. But proximity should not be mistaken for identity.

A perfectly preserved state can have an uncertain history.

Conversely, a badly damaged state can sometimes belong to a well-established history.

The amount of surviving content and the quality of surviving provenance are therefore distinct quantities.

1.3. *From States to Trajectories*

The preceding distinction suggests the first formal enlargement of the object under study.

Let X be a space of possible states. For the moment, nothing substantial depends on what kind of states these are. They may be documents, organisms, institutional configurations, software artifacts, civilizations, or representations within a computational system.

A state is written

$$x \in X.$$

If only the present state matters, this notation may be sufficient. The Originist's problem begins when it is not.

Suppose that x_0 undergoes a sequence of transformations

$$T_1, T_2, \dots, T_n$$

producing states

$$x_0, x_1, \dots, x_n.$$

We define the corresponding trajectory as follows.

Definition 1.3 (Derivational trajectory). A *derivational trajectory* terminating in x_n is an ordered sequence

$$\gamma_{x_n} = \left(x_0 \xrightarrow{T_1} x_1 \xrightarrow{T_2} \dots \xrightarrow{T_n} x_n \right),$$

where each T_i records a transformation relevant to the provenance question under consideration.

The phrase “relevant to the provenance question” is necessary. A trajectory containing every physical event in the causal history of a manuscript would be useless. The temperature of the room in which a copyist worked might belong to the total causal history of a document without belonging to the derivational history of its wording.

A trajectory is therefore already selective.

This fact will become important later, because selecting which transformations count is itself an operation capable of losing information. For the present, however, it is enough to notice that the endpoint map

$$\text{End}(\gamma_{x_n}) = x_n$$

forgets almost everything about the trajectory.

Many different histories may possess the same endpoint.

Formally, if $\Gamma(X)$ denotes the relevant space of trajectories in X , then

$$\text{End} : \Gamma(X) \longrightarrow X$$

need not be injective.

This elementary observation contains the first formal version of the Originist’s problem.

Proposition 1.4 (Endpoint insufficiency). *In any provenance system for which the endpoint map $\text{End} : \Gamma(X) \rightarrow X$ is non-injective, the present state is insufficient to determine its derivational history.*

Proof. Non-injectivity means that there exist distinct trajectories $\gamma_A, \gamma_B \in \Gamma(X)$ such that

$$\gamma_A \neq \gamma_B$$

while

$$\text{End}(\gamma_A) = \text{End}(\gamma_B).$$

Let their common endpoint be x . Observation of x alone therefore cannot determine whether the derivational history was γ_A or γ_B . Hence the endpoint is insufficient to determine derivational history. $\square$

The proof is trivial. Its consequences are not.

1.4. Convergent Reconstruction

Consider an original state O .

One surviving object, x_A , is copied directly from it:

$$\gamma_A : O \longrightarrow x_A.$$

A second object passes through repeated reconstruction and compression:

$$\gamma_B : O \longrightarrow R_1 \longrightarrow C_1 \longrightarrow R_2 \longrightarrow C_2 \longrightarrow x_B.$$

Suppose now that the final states are indistinguishable under the strongest state-level comparison available to us. For a digital artifact, we may take the extreme case:

$$x_A =_{\text{byte}} x_B.$$

Nevertheless,

$$\gamma_A \neq \gamma_B.$$

The equality of endpoints has not collapsed the difference between their histories.

This is the first pathology around which the rest of the essay will grow.

Pathology 1.5 (Convergent reconstruction). Two derivationally distinct trajectories may terminate in states that are identical under a chosen state-level equivalence relation:

$$\gamma_A \neq \gamma_B, \quad \text{End}(\gamma_A) \sim \text{End}(\gamma_B).$$

Consequently, endpoint equivalence does not in general imply provenance equivalence.

In the byte-identical case,

$$x_A =_{\text{byte}} x_B \not\Rightarrow x_A =_{\text{prov}} x_B.$$

The notation is intentionally stronger than the example requires. Nothing about the argument depends upon digital files. Byte identity merely makes the counterexample difficult to evade because it removes ordinary appeals to visible difference.

The two artifacts can be identical now.

They can still have different histories.

1.5. Generation Without Difference

The distinction becomes particularly important when transformations are regenerative.

Suppose an artifact is summarized, regenerated from the summary, summarized again, and regenerated again. The resulting artifact may contain sentences identical to sentences in the original. A comparison system that evaluates only present content will naturally assign no penalty to an exact match.

An Originist may nevertheless wish to distinguish

$$\varphi^{[0]}$$

from

$$\varphi^{[1]}.$$

At this stage the superscripts should be read minimally. The first records directly inspected material. The second records material separated from the relevant source by one recognized derivational transformation.

The important point is not that

$$\varphi^{[0]}$$

is somehow semantically superior to

$$\varphi^{[1]}.$$

They may express precisely the same proposition. They may even contain precisely the same characters.

Rather,

$$\text{Prov}(\varphi^{[0]}) \neq \text{Prov}(\varphi^{[1]}).$$

Generation is therefore not a property of visible content considered alone. It is a property of content situated in a derivational history.

This gives a more precise interpretation to the computational role called Originist.

Definition 1.6 (Generation depth). Given a designated source state O and a derivational trajectory

$$\gamma : O \xrightarrow{T_1} x_1 \xrightarrow{T_2} \dots \xrightarrow{T_n} x_n,$$

the *generation depth* of x_n relative to O , under the chosen transformation vocabulary, is

$$\text{Depth}_O(x_n; \gamma) = n.$$

The dependence on γ is essential.

If two histories converge on the same endpoint, then it is possible that

$$x_A = x_B$$

while

$$\text{Depth}_O(x_A; \gamma_A) \neq \text{Depth}_O(x_B; \gamma_B).$$

Thus there is no well-defined function

$$\text{Depth}_O : X \rightarrow \mathbb{N}$$

unless additional assumptions guarantee a unique relevant derivational history for each state.

Generation belongs first to a trajectory, not to an endpoint.

1.6. Approximation Without Ancestry: Shannon's Markov Languages

The trajectory-relative reading of generation just established has an unusually early and clean illustration, from outside the manuscript's usual sources.

Claude Shannon's 1948 paper on communication theory constructs successive statistical approximations to English by conditioning each generated symbol on an increasing span of preceding context [14]. Schematically, an order- k approximation sets

$$P(w_{t+1} | w_t, w_{t-1}, \dots) = P(w_{t+1} | w_t, \dots, w_{t-k+1}),$$

and generates symbols accordingly. As k increases, or as the conditioning unit moves from letters to words to word pairs, the generated sequences acquire progressively stronger surface resemblance to ordinary English, despite arising from a generative mechanism with no author, no intention, and no historical relation to any actual English utterance.

Definition 1.7 (Order- k statistical generation). A sequence $m = (w_1, \dots, w_n)$ is an *order- k statistical generation* over a source distribution if each w_{t+1} is drawn according to $P(w_{t+1} \mid w_t, \dots, w_{t-k+1})$ for some fixed k , with no further dependence on t or on any external record.

Shannon’s own examples already anticipate the interesting case. He reports that as k grows the generated samples resemble ordinary English more closely, and that they exhibit apparent structure extending beyond what the order- k dependency explicitly supplies [14]. That second observation matters more than the first for this manuscript. It is not merely that Markov generation can look like English. It is that a reader examining the output can be led to attribute a longer-range organizing history to it than the generator actually possessed.

Pathology 1.8 (Statistical resemblance without genealogy). Let h be a state produced by ordinary human linguistic production, and let m be an order- k statistical generation for some fixed k . Suppose a selected observer or discriminator δ finds the two increasingly similar as k grows:

$$h \sim_{\delta} m.$$

Then nothing follows about the relation between their generative histories. In particular,

$$h \sim_{\delta} m \not\Rightarrow h =_{\text{prov}} m.$$

Proof. This is an instance of pathology 1.5 in which one of the two trajectories has no originating state at all in the relevant sense: h descends from an ordinary history of authorship, while m descends from a local statistical generator with no comparable history to disclose. Endpoint resemblance under δ is, by hypothesis, a fact about $\text{End}(\gamma_h)$ and $\text{End}(\gamma_m)$ alone; provenance equivalence is a fact about γ_h and γ_m as trajectories. The two need not agree, for the reason already established in pathology 1.5. $\square$

What makes the Shannon case sharper than an ordinary instance of convergent reconstruction is the direction of the failure. Section 1.5 showed that generation depth cannot be read off an endpoint without specifying a trajectory. Order- k generation shows something stronger: an observer can perceive organization at a range the generator never implemented. The failure is not merely that history is invisible at the endpoint; it is that the endpoint can suggest a richer history than the one that actually produced it.

WHAT SHANNON SUPPLIES

Statistical structure can outrun the dependency structure explicitly encoded by its generator.

This is a narrower and more defensible claim than it may first appear. Shannon’s framework brackets meaning from the engineering problem of communication throughout, and nothing here should be read as claiming that order- k generation produces, or fails to produce, meaning [14]. The claim is only about genealogy, not semantics:

$$\boxed{\text{linguistic appearance} \not\Rightarrow \text{linguistic genealogy.}}$$

An artifact can enter the region of state space occupied by ordinary linguistic production without traversing any of the histories by which that region is ordinarily reached. Section 2.11 returns to this once representations are permitted to act, rather than merely to resemble.

1.7. *Originism as an Inverse Problem*

The preceding formalism also clarifies why originism should not be imagined as simple reversal. Suppose a forward process is known:

$$O \rightarrow x_1 \rightarrow x_2 \rightarrow P.$$

If every transformation were invertible and perfectly recorded, recovering O from P would be straightforward in principle. One could compose the inverse transformations.

Historical reconstruction is interesting precisely because this condition usually fails.

Compression may discard distinctions. Copying may omit metadata. Translation may preserve one structure while altering another. Independent traditions may merge. Records may disappear. Later agents may reconstruct missing material. A present state can therefore be compatible with more than one possible past.

Let

$$\Gamma^-(P)$$

denote the set of admissible trajectories terminating at the present state P . Originist inference seeks not necessarily a unique member of this set, but constraints upon it.

Schematically,

$$P \rightsquigarrow \Gamma^-(P).$$

The arrow here is epistemic rather than historical. The actual causal trajectory ran toward P . Inference runs over candidate descriptions in the opposite direction.

This distinction prevents a common mistake. Reconstructing a plausible past does not make the reconstruction causally ancestral to the evidence from which it was inferred.

The map and the history point in opposite directions.

1.8. The First Originist Objection

Mathematical reasoning routinely simplifies objects by identifying states that differ only in ways irrelevant to the problem at hand. Such identifications are indispensable. Without them, abstraction would be impossible.

Originism does not object to equivalence.

It objects to equivalence without an account of what the equivalence forgets.

Suppose

$$q : X \longrightarrow X/\sim$$

identifies states under an equivalence relation $\sim$. If two states possess distinguishable provenance histories but are mapped to the same equivalence class, then the quotient has erased a distinction available before the operation.

Whether that erasure matters depends upon what one intends to do next.

Originist Objection 1.9 (Preliminary form). An equivalence relation is epistemically dangerous for an Originist task when it identifies states whose distinctions are required to discriminate among admissible derivational histories.

The qualification “for an Originist task” prevents the objection from becoming a general hostility toward quotienting. Byte identity may be exactly the correct equivalence for verifying a file transfer. It may be exactly the wrong equivalence for determining whether two files possess the same genealogy.

The question is therefore never merely

$$x \sim y?$$

It is also

What future inference becomes impossible after treating x and y as the same?

The formal loss operator associated with this question will not be introduced yet. The examples required to define it adequately have not occurred.

1.9. *The Absent Ground*

Card's originists work under a condition that can now be stated more precisely. The origin is causally prior but epistemically unavailable. Present evidence is not the origin. Nor is a successful reconstruction identical with the origin merely because it reproduces some of its structure.

This produces three objects that ordinary historical language often slides between:

$$O, \quad \gamma, \quad \widehat{O}.$$

Here O is the historical origin, γ is a trajectory connecting that origin to surviving evidence, and $\widehat{O}$ is a reconstruction inferred from that evidence.

Even in the best case,

$$\widehat{O} \simeq O$$

requires an explicit account of what the equivalence symbol means.

Structural agreement is not historical identity.

Semantic agreement is not material identity.

Successful reconstruction is not temporal reversal.

An origin may therefore become unrecoverable without becoming irrelevant. Its effects remain distributed through descendants, records, constraints, and recurrences. Originism begins precisely where possession of the origin ends.

One early account of the fictional discipline describes Level's research as oriented toward general principles of human origins rather than merely toward the identification of a single planetary point of departure [1].¹

This shift from point-location to constraint is the deepest reason Card's fictional discipline belongs in the present argument. The Originist does not need to possess the ground in order for the ground to constrain what may truthfully be said about the present.

¹[0] The distinction is retained here because it motivates the separation between locating an origin and recovering the constraints under which an origin can be inferred.

1.10. What the Origin Has Already Failed to Tell Us

We began with a state.

The literary problem forced us to add its trajectory.

That enlargement was not motivated by a preference for process philosophy or by a prior commitment to a particular metaphysics. It was forced by a simple counterexample:

$$x_A = x_B, \quad \gamma_A \neq \gamma_B.$$

Once this case is admitted, no theory that represents only the endpoint can recover every distinction relevant to provenance.

The conclusion should nevertheless remain modest. Nothing in this movement establishes that trajectories are the fundamental objects of reality. It establishes only that states are insufficient for the particular class of questions under consideration.

That difference will govern the rest of the essay.

ENDPOINT INSUFFICIENCY

A present state may preserve the result of a history
without preserving enough information to identify that history.

Card has therefore supplied the backward-facing problem:

$$\text{surviving traces} \rightsquigarrow \{\text{admissible pasts}\}.$$

But nothing yet tells us what happens when the direction of the question is reversed.

Suppose the origin is known.

Suppose the trajectory proceeds forward without interruption.

Suppose almost nothing materially original survives at its endpoint.

What, then, has continued?

That is the problem of *Macrolife*.

MOVEMENT II. CONTINUATION

What may something become and still count as its continuation?

The problem of origin begins with something that already exists and asks how it came to be there. The problem of continuation reverses the direction of attention. We begin with something whose existence is not in doubt and ask what may happen to it without bringing its history to an end.

Ordinary cases make this question seem easier than it is. A house remains the same house after it is painted. A person remains the same person after a haircut. A city survives the replacement of roads, buildings, governments, and inhabitants. In such cases we rarely need to specify which changes are permitted because the changes remain comfortably inside inherited conventions of identity.

The difficulty appears when replacement ceases to be local. What if every material component is eventually exchanged? What if the environment that defined the original object is abandoned? What if continuation requires not preserving a form but repeatedly changing it? What if the descendant survives only because almost nothing about the original arrangement is held fixed?

George Zebrowski's *Macrolife* pushes precisely in this direction. Its large-scale technological imagination treats planetary existence not as the permanent condition of civilization but as one historical phase among others. The relevant question is therefore not whether an original state can be kept unchanged. It is whether a sequence of transformations can remain a continuation even when its endpoint would no longer be recognized as materially identical with its beginning.

2.1. The Question Points Forward

Movement 1 considered an inverse problem. Given a present state P , the Originist reasons over histories capable of terminating in that state:

$$P \rightsquigarrow \Gamma^-(P).$$

The causal history itself runs in the opposite direction. The present is an effect from which possible antecedents are inferred.

Macrolife changes the orientation. Its characteristic problem begins with an existing civilization and asks what forms its continuation may take as the conditions of survival change [2]. The question is prospective:

$$O \longrightarrow \{\text{possible descendants}\}.$$

This is not simply Card's problem with the arrows reversed.

In the retrospective case, the historical transformations have already occurred. Their effects constrain reconstruction. In the prospective case, the relevant transformations have not all occurred, and the space of possible continuations is correspondingly open.

The asymmetry can be expressed provisionally as

$$\text{past inference : } P \rightsquigarrow \Gamma^-(P),$$

whereas

$$\text{future continuation : } O \rightsquigarrow \Gamma^+(O).$$

Here $\Gamma^+(O)$ denotes candidate trajectories beginning at O .

The two spaces are related by history, but they are not interchangeable. A realized present may constrain its possible pasts without uniquely determining them, while a present origin may permit many futures of which only one, if any, will actually occur.

Originism contracts an already realized history into a set of admissible reconstructions.

Continuation opens an unrealized history into a set of possible descendants.

2.2. *Macrolife and Material Independence*

Zebrowski's central speculative move is to treat large artificial habitats, spacefaring communities, and eventually much larger forms of organized life as continuations of terrestrial civilization rather than as merely detached artifacts produced by it [2]. The conceptual importance of this move lies less in any particular engineering proposal than in the relation it establishes between survival and transformation.

A planet-bound civilization can easily mistake persistence of environment for persistence of civilization. The landscape, atmosphere, gravitational field, ecology, inherited architecture, and biological substrate appear as stable background conditions. They are so persistent relative to an individual human life that they can be treated as though they were not themselves parts of a historical arrangement.

Macrolife removes that convenience.

Once a civilization becomes capable of constructing and inhabiting its own environments, a distinction appears between preserving a civilization and preserving the conditions under which that civilization first developed. These projects may coincide for a time. They need not coincide indefinitely.

Let C_0 denote a civilization at some initial stage. After a sequence of transformations,

$$C_0 \xrightarrow{T_1} C_1 \xrightarrow{T_2} \dots \xrightarrow{T_n} C_n,$$

it may be the case that

$$C_0 \neq_{\text{material}} C_n.$$

Indeed, under sufficiently extensive replacement, there may be no particular material component whose persistence is necessary for the entire sequence to be regarded as continuous.

This gives the second major failure of a state-based criterion.

Pathology 2.1 (Material discontinuity without historical discontinuity). There exist plausible histories in which

$$x_0 \neq_{\text{material}} x_n$$

while the sequence

$$x_0 \longrightarrow x_1 \longrightarrow \cdots \longrightarrow x_n$$

is nevertheless treated as a continuous history of transformation. Consequently, material identity is not a necessary condition for every relevant notion of continuation.

The conclusion does not establish that material continuity is irrelevant. It establishes only that material identity and historical continuation cannot be silently identified.

2.3. *Replacement Without Resurrection*

The familiar Ship of Theseus problem is often posed as a puzzle concerning the identity of an object after gradual replacement. Its usefulness here is more limited and more precise.

Suppose an object S_0 undergoes component replacement over time:

$$S_0 \longrightarrow S_1 \longrightarrow S_2 \longrightarrow \cdots \longrightarrow S_n.$$

At each transition, only part of the object is replaced. No stage requires the construction of a complete copy from an external description. There is a continuous process connecting adjacent states.

Now compare this history with a different operation. Destroy S_0 , retain a sufficiently complete description $D(S_0)$, and later construct S^* from that description:

$$S_0 \longrightarrow D(S_0) \dashrightarrow S^*.$$

It is possible that

$$S_n =_{\text{byte}} S^*$$

for an appropriate digital analogue, or that

$$S_n \simeq_I S^*$$

under a chosen structural invariant.

Nevertheless, the histories differ.

The first is replacement within an ongoing trajectory.

The second contains reconstruction from a representation.

This difference is particularly important in discussions of copying, uploading, restoration, and consciousness transfer. If endpoint similarity is treated as sufficient, gradual expansion and destructive copying become difficult to distinguish. Once trajectory is retained, they are different operations before any metaphysical conclusion about personal identity is drawn.

Proposition 2.2 (Replacement–reconstruction distinction). *Endpoint equivalence between a continuously transformed descendant and a reconstructed copy does not imply equivalence of their derivational trajectories.*

Proof. Let

$$\gamma_{\text{cont}} = (S_0 \rightarrow S_1 \rightarrow \dots \rightarrow S_n)$$

be a trajectory in which each state arises through local transformation of the preceding state. Let

$$\gamma_{\text{recon}} = (S_0 \rightarrow D(S_0) \dots \rightarrow S^*)$$

contain a stage at which the later object is generated from a representation rather than by local continuation of the material organization represented by the preceding object.

Even if

$$S_n \sim S^*,$$

the ordered transformations constituting the two trajectories differ. Therefore

$$\gamma_{\text{cont}} \neq \gamma_{\text{recon}}.$$

Endpoint equivalence alone cannot remove this distinction. □

Notice what the proposition does *not* establish. It does not prove that S_n is the original while S^* is not. Such a conclusion would require a criterion of identity not yet supplied.

The proposition establishes something weaker and more useful: a theory that collapses these histories merely because their endpoints agree has discarded information before establishing that the information is irrelevant.

2.4. The Temptation of Causal Continuity

A natural response is to replace material identity with causal continuity.

Instead of requiring

$$x =_{\text{material}} y,$$

we might require

$$x \rightsquigarrow_{\text{causal}} y.$$

The proposal has considerable force. A continuously modified ship is causally connected to its earlier stages. A civilization constructing new habitats is causally connected to the civilization that designed them. A living organism is causally continuous with earlier stages despite extensive material turnover.

Causal continuity therefore captures something material identity misses.

It is still too weak.

Consider a file F corrupted by a destructive process:

$$F \rightsquigarrow_{\text{causal}} F_{\text{corrupt}}.$$

The corruption is causally downstream from the file. Yet this fact alone does not establish that the corrupted object is an adequate continuation of the file for every purpose.

Similarly, a city may causally produce its ruins:

$$C \rightsquigarrow_{\text{causal}} R.$$

The ruins would not exist in their present configuration without the city. Yet the claim that the city therefore continues to exist as the ruins is at best context-dependent.

Biological examples make the problem sharper. Tissue can undergo a continuous causal process producing pathological growth. The resulting structure may be causally continuous with the tissue from which it arose while violating the organizational conditions under which we would call it continuation of the same functioning tissue.

Thus

$$x \rightsquigarrow_{\text{causal}} y$$

does not by itself tell us which properties, relations, or constraints must survive for y to count as an acceptable continuation of x .

Pathology 2.3 (Causal succession without admissible continuation). There exist causally continuous transformations

$$x \rightsquigarrow_{\text{causal}} y$$

for which y fails a criterion required for the relevant notion of continuation. Therefore causal continuity is not sufficient, by itself, to define continuation.

This pathology forces the next enlargement of the formalism.

2.5. Admissible Transformation

The question is no longer merely whether a transformation occurred.

The question is whether it belongs to the class of transformations under which the relevant continuation relation is preserved.

Let X again denote a state space. We now associate with the problem a collection

$$\mathcal{A}$$

of admissible transformations or admissible trajectories.

The term “admissible” is intentionally relational. A transformation is not admissible in the abstract. It is admissible relative to a criterion, task, invariant, or world-constituting structure.

Definition 2.4 (Admissible continuation). Let $\mathcal{A}$ be a specified family of transformations on a state space X . A trajectory

$$\gamma : x_0 \xrightarrow{T_1} x_1 \xrightarrow{T_2} \dots \xrightarrow{T_n} x_n$$

is an $\mathcal{A}$ -admissible continuation when each transformation, or the trajectory considered as a whole when admissibility is nonlocal, satisfies the constraints defining $\mathcal{A}$.

This definition deliberately permits admissibility to be nonlocal.

It may be tempting to write

$$T_i \in \mathcal{A} \quad \text{for every } i$$

and conclude that the entire trajectory is admissible. That condition is useful when admissibility composes locally. It need not always do so.

A sequence of individually harmless transformations may accumulate into a change that destroys an invariant. Conversely, a locally disruptive transformation may belong to a globally admissible repair process.

The distinction will later connect directly to TARTAN and to the author’s constraint-based treatment of realization. For now, the important result is simpler.

Continuation requires more than causal ancestry.

It requires a specification of what kinds of transformation the relevant continuation relation permits.

2.6. *There Is No Unqualified Continuation Relation*

Once admissibility is explicit, the phrase “the same thing continued” becomes suspiciously incomplete.

Continued as what?

A manuscript may continue as a semantic work while ceasing to continue as a physical artifact. A biological lineage may continue while every organism that once instantiated it dies. An institution may continue legally while its practices change radically. A civilization may continue genealogically while ceasing to preserve a particular political order.

Continuation is therefore typed by the structure whose persistence is being asserted.

Let $\mathcal{I}$ denote a selected family of invariants. We may write

$$x \simeq_{\mathcal{I}} y$$

when x and y agree with respect to those invariants.

But even this does not settle the historical question.

Two independently constructed objects may satisfy

$$x \simeq_{\mathcal{I}} y$$

without either descending from the other.

Thus invariant preservation and genealogy remain distinct.

Proposition 2.5 (Invariant agreement does not establish descent). *For a nontrivial invariant-equivalence relation $\simeq_{\mathcal{I}}$,*

$$x \simeq_{\mathcal{I}} y$$

does not in general imply the existence of a historical trajectory from x to y .

Proof. Choose two states independently constructed so as to instantiate the same selected invariants. By construction,

$$x \simeq_{\mathcal{I}} y.$$

Their independent construction entails that neither need belong to the derivational ancestry of the other. Hence invariant agreement alone does not establish descent. $\square$

We have therefore accumulated several relations that ordinary identity language tends to compress:

material identity, causal continuity, invariant preservation, admissible continuation.

They are not interchangeable.

The notation will remain deliberately incomplete until concrete pathologies force further distinctions.

2.7. Copying and Continuous Expansion

The distinction between copying and continuous expansion provides a useful stress test.

Suppose a system S is represented with sufficient accuracy to construct a second system S' . The copying process has the schematic form

$$S \rightarrow D(S) \rightarrow S'.$$

Now suppose instead that S expands by incorporating new components while maintaining active causal and organizational coupling between old and new regions:

$$S_0 \hookrightarrow S_1 \hookrightarrow S_2 \hookrightarrow \dots$$

At some later stage, none of the material initially present in S_0 need remain.

If endpoint structure alone is considered, the two processes may eventually be made arbitrarily similar. If trajectories are retained, however, they remain distinguishable.

The first process establishes a new realization from a description or transfer channel.

The second enlarges an already operating realization.

This distinction has consequences for the author's earlier argument concerning consciousness transfer, where destructive copying and continuous expansion were treated as importantly different candidate processes of persistence. The present framework supplies a more general reason for that difference: they occupy different regions of trajectory space.

No claim about consciousness itself is required at this stage.

The relevant principle is simply

$$\text{endpoint resemblance} \neq \text{trajectory equivalence.}$$

Macrolife generalizes the same issue from an individual system to a civilization. A civilization that expands into constructed environments does not need to preserve its initial matter. But neither does the mere existence of a later structure resembling the civilization establish that the civilization continued into it.

The missing variable is the admissible path.

2.8. *Why the Two Directions Do Not Cancel*

It would now be easy to draw a pleasing symmetry.

Card gives

$$? \rightarrow P,$$

while Zebrowski gives

$$O \rightarrow ?.$$

One might therefore imagine Originism and Macrolife as inverse views of a single reversible relation.

That would be a mistake.

Suppose a transformation

$$T : x \rightarrow y$$

discards information. Then the existence of T does not guarantee an inverse transformation

$$T^{-1} : y \rightarrow x.$$

Indeed, if distinct states satisfy

$$T(x_1) = T(x_2) = y,$$

then y alone cannot determine which antecedent was realized.

This is the same non-injectivity encountered in proposition 1.4, now viewed as an irreversible operation.

Definition 2.6 (Origin-relative irreversibility). A transformation $T : X \rightarrow Y$ is *origin-relative irreversible* with respect to a distinction δ when states distinguished by δ can be mapped by T to outputs from which that distinction cannot be recovered without additional information.

This definition does not require thermodynamic irreversibility. It describes irreversibility relative to a provenance distinction.

Compression is the obvious example. If two distinguishable inputs are mapped to one representation, the representation may preserve everything required for one task while destroying what is required for another.

The consequence for the temporal symmetry is immediate.

Originist inference begins after transformations have occurred and asks which pasts remain compatible with their surviving traces.

Macrolife continuation begins before all transformations have occurred and asks which futures remain admissible.

The first is constrained by realized losses.

The second is constrained by possible transformations.

They face each other across the present, but they do not undo one another.

2.9. Past Contraction and Future Expansion

Let P denote a present state.

Define

$$\Gamma_A^-(P)$$

as the family of admissible histories terminating in P , and

$$\Gamma_A^+(P)$$

as the family of admissible continuations beginning at P .

The present then occupies an asymmetric position:

$$\Gamma_A^-(P) \longrightarrow P \longrightarrow \Gamma_A^+(P).$$

The notation should not be mistaken for a claim that every member of the left family actually occurred or that every member of the right family will occur. The left side contains candidate histories consistent with surviving constraints. The right side contains candidate continuations permitted by current constraints.

Evidence tends to reduce the left family.

Possibility tends to enlarge the right family.

Additional historical evidence may eliminate candidate pasts:

$$\Gamma_A^-(P) \supseteq \Gamma_A^-(P \mid E_1) \supseteq \Gamma_A^-(P \mid E_1, E_2).$$

By contrast, newly available technologies or organizational transformations may enlarge the space of possible futures:

$$\Gamma_{A_1}^+(P) \subseteq \Gamma_{A_2}^+(P),$$

when A_2 permits transformations unavailable under A_1 .

This is the precise sense in which the two literary probes face opposite temporal directions without becoming inverses.

2.10. When Almost Nothing Original Remains

The strongest version of the Macrolife problem occurs when material replacement approaches completeness.

Suppose

$$C_0 \rightarrow C_1 \rightarrow \dots \rightarrow C_n$$

is treated as a continuous civilizational history. Let $M(C_i)$ denote the material constituents of C_i .

It may eventually be the case that

$$M(C_0) \cap M(C_n) = \emptyset.$$

Nothing in the initial material inventory survives.

Yet the conclusion

$$C_0 \rightsquigarrow C_n$$

does not follow merely from that fact.

If continuation is carried by organization, causal dependence, transmitted constraints, institutional inheritance, memory, reproduction, or some combination of these, then disappearance of the original matter may be compatible with historical continuation.

This produces the question from which the title of the essay is drawn.

NOTHING ORIGINAL NEED SURVIVE

If continuation is carried by an admissible history rather than by persistence of an initial material state, then complete replacement of the original material is compatible, in principle, with continuation.

The proposition is deliberately conditional.

The title does not claim that preservation never matters. Nor does it claim that every causal descendant counts as continuation.

It claims that original material need not be the invariant that does the work.

What does the work instead remains to be determined.

2.11. *Instructions as Historical Objects: Prompt Injection and the Provenance of Constraints*

The admissibility apparatus developed in this movement has a consequence worth making explicit before the movement closes: a representation's provenance can determine not only what it means but what it is entitled to do.

Suppose a system is operating under an admissibility structure A determined by a constraint family C_0 (section 2.5), and receives some representation p through an ordinary data channel. The transformation of interest is not an ordinary state change

$$x \longrightarrow x',$$

but

$$(C_0, x) \xrightarrow{p} (C_p, x'),$$

in which p is interpreted as licensed to modify the constraint family itself, rather than merely to serve as data evaluated under it.

Definition 2.7 (Prompt injection). Prompt injection occurs when a representation whose provenance licenses it only as data under C_0 is interpreted as authority over the constraint family governing subsequent transformations, producing $C_p \neq C_0$ without any change in the admissibility structure having been independently warranted.

This is deliberately not a definition in terms of malicious content. Malice is incidental to the structural failure. Consider a string p_A supplied by an authorized controller, and a byte-identical string p_B occurring inside a document retrieved for an unrelated purpose, such as summarization. At the state level,

$$p_A =_{\text{byte}} p_B.$$

But their provenance differs:

$$\text{Prov}(p_A) \neq \text{Prov}(p_B).$$

Pathology 2.8 (Provenance-insensitive authority attribution). A system exhibits provenance-insensitive authority attribution when it licenses

$$p_A =_{\text{byte}} p_B \implies p_A =_{\text{authority}} p_B,$$

that is, when byte-level equivalence is treated as sufficient for equal instructional authority, regardless of $\text{Prov}(p_A)$ and $\text{Prov}(p_B)$.

Proof. This is the strong Originist objection of section 1.8 instantiated at $\delta = \text{Prov}$. The system quotients away exactly the distinction — provenance — that a later operation (interpreting p as an instruction) requires. By section 1.8, this is precisely the condition under which a quotient becomes a wound rather than a harmless abstraction. $\square$

WHAT PROMPT INJECTION SUPPLIES

Semantic content does not determine instructional authority.

The computational analogue of the manuscript’s central distinction is now available in operational form:

State $\neq$ History

becomes

content $\neq$ authority.

Chain of Memory, introduced later, supplies the constructive half of this pathology: a system does not need to retain everything about an instruction’s history in order to avoid this failure. It needs to preserve exactly those provenance distinctions on which future authority and admissibility judgments depend — no more, and no less. Section 1.6 established that content does not reveal its provenance; this section has shown why failing to track that fact can change what content is permitted to do.

2.12. The First Appearance of the World Problem

At civilizational scale, a further difficulty begins to appear.

Suppose C_t and C_{t+n} belong to an admissible civilizational trajectory:

$$C_t \rightsquigarrow_{\text{causal}} C_{t+n}.$$

Suppose further that enough organizational structure survives for us to call the latter a descendant of the former.

A stronger question remains unanswered.

Did the same *world* continue?

A civilization can alter its environment, institutions, bodies, memory systems, perceptual interfaces, spatial organization, and relations among agents. At some point it becomes possible that the genealogy of the civilization remains intelligible while the relational field within which its earlier forms made sense has changed profoundly.

We must therefore distinguish, at least provisionally,

persistence of an object,

persistence of a civilization,

and

persistence of a world.

No formal definition of world-continuation will be offered here. Doing so would outrun the examples.

The distinction has appeared, but it has not yet been earned mathematically.

2.13. *What Continuation Has Failed to Preserve*

Movement 1 established that a state does not determine its history.

The present movement has established a complementary failure: difference of state does not determine discontinuity of history.

The two failures can be placed side by side:

$$x_A = x_B \quad \text{while} \quad \gamma_A \neq \gamma_B,$$

and

$$x_A \neq_{\text{material}} x_B \quad \text{while} \quad x_A \rightsquigarrow_{\text{causal}} x_B.$$

State equality can conceal historical difference.

State difference can coexist with historical continuation.

Neither direction permits identity of states to substitute for analysis of trajectories.

But causal trajectory alone has also failed. Corruption, destruction, and pathological transformation can all be causally continuous. We were therefore forced to introduce admissibility:

$$\gamma \longrightarrow (\gamma, A).$$

This is the second enlargement of the representational object.

It should again be read minimally. We have not shown that (γ, A) is fundamental. We have shown that an untyped causal trajectory is insufficient to discriminate the cases already encountered.

CONTINUATION UNDER CONSTRAINT

The question is not whether a later state was caused by an earlier one.
The question is which transformations preserve the kind of continuation being claimed.

Card left us with an inaccessible beginning.

Zebrowski has now given us an indefinitely transformable future.

There remains another possibility.

A trajectory can leave its origin and come back.

If it returns, what exactly has returned to what?

The answer cannot simply be

$$O \rightarrow X \rightarrow O,$$

because both the traveler and the origin may have histories of their own.

The line is about to become a loop.

And the loop, in turn, will fail to remain a line.

MOVEMENT III. RECURRENCE

What does it mean for what departed to return?

Returning somewhere is one of the most ordinary forms of continuity. A person leaves a house in the morning and returns in the evening. A traveler leaves a country and comes home years later. A spacecraft departs from a planet, completes a journey, and returns to its point of departure. The language of return suggests a loop: something leaves, undergoes a history elsewhere, and comes back to where it began.

The apparent simplicity depends upon ignoring two changes.

The traveler who returns has acquired a history. The place to which the traveler returns has acquired one as well.

A childhood home revisited after thirty years is not the state that was left thirty years earlier. Even if the building remains materially similar, its inhabitants, surroundings, uses, and relation to the traveler may have changed. Nor is the returning traveler identical in state to the person who departed. Return therefore cannot ordinarily mean restoration of the initial configuration.

Ursula K. Le Guin's *The Dispossessed* makes this problem unusually visible. Shevek's journey from Anarres to Urras and eventual return to Anarres is geographical, political, intellectual, and relational at once. He crosses a boundary between worlds that are themselves historically connected. He carries ideas across that boundary. Those ideas acquire new possible recipients. When he returns, the apparent loop does not close by restoring its starting point.

The problem of recurrence is therefore neither Card's problem of reconstructing an absent beginning nor Zebrowski's problem of continuing indefinitely into an open future. It asks what sort of relation can connect a later state to an earlier configuration without pretending that history between them did not occur.

3.1. The Wall

The Dispossessed begins with a wall [3]. The object is physically unimpressive. Its conceptual function is not.

The wall separates the spaceport on Anarres from the surrounding society. Yet the meaning of the enclosure depends upon which side is taken as inside. From one perspective the wall encloses the landing field. From another, it encloses the rest of Anarres by marking the boundary across which contact with Urras and other worlds is controlled.

A boundary therefore need not merely divide two already constituted regions. It can participate in determining which region counts as interior, which as exterior, and which transformations are permitted between them.

This makes the wall more than a metaphor for political separation. It is an instance of a general computational fact about boundaries: a boundary classifies crossings.

Let A denote a region identified with Anarres and U a region identified with Urras. A naive representation would write

$$A \mid U.$$

But the bar alone says nothing about what may cross it.

A more useful representation associates the boundary B with a set of admissible crossing operations

$$\mathcal{A}_B.$$

The boundary is then not merely a location. It participates in determining which trajectories are realizable.

Definition 3.1 (Boundary-relative admissibility). Let B separate or relate regions X and Y . The *boundary-relative admissibility structure* $\mathcal{A}_B$ specifies the class of transformations by which states, agents, information, or material may cross between X and Y while remaining recognizable under the relevant system of constraints.

This definition is intentionally broad. A wall may physically prevent bodies while allowing radio signals. A legal boundary may permit persons while restricting property. An institutional boundary may admit information only after translation into an accepted vocabulary. A computational interface may permit data while refusing operations.

The point is not that all boundaries are the same.

It is that a boundary can be characterized partly by what it permits to pass.

Boundary Crossing 3.2 (Shevek's departure). Shevek's movement from Anarres to Urras is not merely a change of spatial coordinate. It is a transition across a boundary whose political, institutional, economic, and epistemic constraints differ on its two sides. The trajectory therefore changes not only Shevek's location but the set of transformations available to him.

The wall introduces admissibility into space.

Return will introduce it into recurrence.

3.2. *Return Is Not Restoration*

Let O denote a state at departure.

A simple model of return might be written

$$O \rightsquigarrow X \rightsquigarrow O.$$

The notation is misleading because it uses the same symbol for two states separated by a nontrivial history.

Let the state of origin at departure be O_t , and let the corresponding state encountered upon return be O_{t+n} . Let the traveler at departure be S_t , and the traveler upon return S_{t+n} .

Then the relevant configuration is closer to

$$(S_t, O_t) \rightarrow X \rightarrow (S_{t+n}, O_{t+n}).$$

In general,

$$S_t \neq S_{t+n}$$

as states, and

$$O_t \neq O_{t+n}.$$

Yet we may still have reason to describe the event as a return.

This motivates a recurrence relation weaker than state identity.

Write

$$O_{t+n} \sim_C O_t$$

when the later state stands in the relevant recurrence relation to the earlier state under a selected family of constraints $\mathcal{C}$.

The important fact is

$$O_{t+n} \neq O_t \quad \text{while} \quad O_{t+n} \sim_C O_t.$$

Return therefore resembles continuation more than restoration.

Definition 3.3 (Constraint-relative recurrence). Given states x_t and x_{t+n} belonging to a common historical structure, x_{t+n} is a *constraint-relative recurrence* of x_t when

$$x_{t+n} \sim_C x_t$$

for a specified family of recurrence constraints $\mathcal{C}$, without requiring

$$x_{t+n} = x_t.$$

The definition deliberately refuses to identify recurrence with periodicity. A periodic system returns to an equivalent dynamical state according to a specified evolution. Historical return is usually messier. The relevant equivalence may be institutional, geographical, genealogical, semantic, or world-relative.

Thus a person can return home even though neither person nor home has remained unchanged.

Proposition 3.4 (Return does not imply restoration). *Constraint-relative recurrence does not in general imply state identity. That is,*

$$x_{t+n} \sim_C x_t \not\Rightarrow x_{t+n} = x_t.$$

Proof. Choose $\mathcal{C}$ to preserve the relations relevant to return while permitting transformations not relevant to those relations. For example, $\mathcal{C}$ may preserve geographical and institutional continuity while allowing changes in material composition and internal state. A later state may then satisfy $\mathcal{C}$ without being identical to the earlier state. Therefore recurrence under $\mathcal{C}$ does not imply restoration of the earlier state. $\square$

The proposition is formally modest. Its importance lies in preventing a loop from being mistaken for an erasure of history.

3.3. *The Returning Origin Has Moved*

The word “origin” now becomes unstable.

Anarres is Shevek’s origin in the immediate geographical and social sense. He departs from it and later returns to it. But Anarres is not an origin without a history. Its society emerged from an earlier revolutionary separation connected to Urras and to the thought of Odo [3].

The origin of one trajectory is therefore itself an endpoint within another.

Instead of

$$O \rightarrow X \rightarrow O',$$

we obtain something closer to

$$O_0 \rightarrow O_1 \rightarrow X \rightarrow O'_1.$$

Here O_1 may function as an origin relative to Shevek’s journey while remaining a descendant relative to the longer political history.

There is no contradiction.

Origin is indexed by the trajectory under consideration.

Definition 3.5 (Relative origin). Given a trajectory or provenance structure γ , a state O is an *origin relative to γ* when it is selected as the relevant initial state for the derivational question posed over γ . This does not imply that O has no antecedent history outside γ .

This qualification alters the Originist problem.

Movement 1 provisionally treated the origin as the inaccessible left boundary of a trajectory:

$$O \rightarrow \dots \rightarrow P.$$

We can now ask:

Which O ?

A manuscript may have an origin as a physical artifact, another as a textual tradition, another as a semantic composition, and another as the endpoint of earlier oral or documentary transmission.

Likewise, Anarres can be an origin for Shevek while remaining a historical descendant of Urrasti political conflict.

Origins have provenance.

3.4. The Originist Turns Around

The discovery that origins themselves possess histories produces an apparent regress.

If

$$O_1$$

has provenance, then perhaps we must reconstruct

$$O_0 \rightarrow O_1.$$

But if O_0 also has provenance, we may seek an earlier state O_{-1} , and so on.

Nothing guarantees a uniquely privileged absolute origin.

This does not make origin-relative reasoning incoherent. It changes what an origin claim means.

To say that O is an origin is not necessarily to say

$$\nexists x (x \rightarrow O).$$

It may instead mean that O is the boundary at which the current provenance question begins.

The distinction is familiar outside speculative fiction. The origin of a printed edition need not be the origin of the work. The origin of a species under one taxonomic criterion need not be a single organism. The origin of an institution may refer to its legal incorporation even when the practices that constitute it developed earlier.

Originism therefore requires declared scope.

Without such scope, the command to “return to the origin” can become an instruction to pursue an indefinitely receding boundary.

Remark 3.6. The regress is not necessarily vicious. A provenance inquiry may terminate because an earlier distinction is irrelevant to the task, because evidence has become unavailable, or because the selected origin is explicitly relative. What Originism resists is not termination but unacknowledged termination.

The distinction is another instance of a principle already encountered.

Forgetting is sometimes necessary.

Forgetting that one has forgotten is more dangerous.

3.5. *Transmission Without a Single Custodian*

Shevek's scientific work introduces a different complication.

Knowledge can cross a boundary without remaining under the control of the institution through which it passed. The political significance of Shevek's physics is tied not merely to what the theory says but to who may possess, transmit, restrict, or monopolize it. His response to attempted appropriation is dissemination: the work is communicated beyond the immediate Urrasti institutions and made available through a wider network [3].

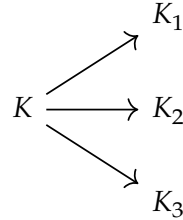
For present purposes, the important operation is branching.

Suppose a source artifact or claim K is transmitted independently to several recipients:

$$K \rightarrow K_1, \quad K \rightarrow K_2, \quad K \rightarrow K_3.$$

The provenance structure is no longer adequately represented by a single chain.

We may draw



rather than

$$K \rightarrow K_1 \rightarrow K_2 \rightarrow K_3.$$

The distinction is obvious once drawn, but it changes the formal object substantially.

A trajectory has become a provenance graph.

3.6. *The Failure of Linear History*

Let

$$\mathcal{G} = (V, E)$$

be a directed graph whose vertices represent relevant states and whose edges represent recorded or hypothesized derivational transformations.

Definition 3.7 (Provenance graph). A *provenance graph* is a directed graph

$$\mathcal{G} = (V, E, \tau),$$

where V is a collection of states, E is a collection of directed derivational relations among those states, and

$$\tau : E \rightarrow \mathcal{T}$$

assigns, when known, a transformation type to each edge.

A linear trajectory is now a special case: a directed path through $\mathcal{G}$.

This enlargement permits branching:

$$x \rightarrow y_1, \quad x \rightarrow y_2,$$

but also convergence:

$$x_1 \rightarrow y, \quad x_2 \rightarrow y.$$

It permits recurrence when later vertices stand in a declared recurrence relation to earlier ones. It permits missing edges, uncertain transformations, and competing derivational hypotheses.

Most importantly, it prevents the history of an artifact from being confused with a single privileged chain when the evidence supports a more complicated structure.

Pathology 3.8 (Linear-history insufficiency). If a provenance structure contains branching or convergence relevant to the question under study, then no single trajectory can represent the complete structure without discarding derivational alternatives or descendants.

Proof. Suppose $x \in V$ has distinct outgoing derivational edges

$$x \rightarrow y_1 \quad \text{and} \quad x \rightarrow y_2,$$

where both descendants are relevant. Any single directed path through x can follow at most one of these edges immediately after x . Therefore the path omits at least one relevant branch. The same argument applies in reverse to relevant convergence. Hence a single trajectory is insufficient to encode the complete provenance structure. $\square$

Movement 1 forced

$$x \rightsquigarrow \gamma.$$

Le Guin now forces

$$\gamma \rightsquigarrow \mathcal{G}.$$

The trajectory was not wrong.

It was a special case mistaken, temporarily, for a sufficient general form.

3.7. *Generation After Branching*

The move from trajectories to provenance graphs immediately complicates the generation-depth definition from definition 1.6.

In a single trajectory,

$$O \rightarrow x_1 \rightarrow \dots \rightarrow x_n,$$

generation depth can be counted along the unique represented path.

In a graph, there may be several paths from O to the same state x .

Let

$$\Pi_{\mathcal{G}}(O, x)$$

denote the set of directed paths from O to x in $\mathcal{G}$.

Then the expression

$$\text{Depth}_O(x)$$

may be ambiguous whenever there exist

$$\pi_1, \pi_2 \in \Pi_{\mathcal{G}}(O, x)$$

with

$$|\pi_1| \neq |\pi_2|.$$

Generation depth must therefore be indexed by a path unless an aggregation rule has been declared:

$$\text{Depth}_O(x; \pi).$$

Possible summaries include

$$\text{Depth}_O^{\min}(x) = \min_{\pi \in \Pi_g(O, x)} |\pi|,$$

or

$$\text{Depth}_O^{\max}(x) = \max_{\pi \in \Pi_g(O, x)} |\pi|.$$

Neither is intrinsically the correct measure.

The shortest path answers how few recognized transformations are sufficient to connect the origin to the state.

The longest path answers a different question.

A historically realized path answers another.

A path of highest evidential support answers yet another.

The apparently simple superscript

$$\varphi^{[3]}$$

has therefore acquired an unstated parameter.

We will not repair the notation yet.

The pathology that makes the repair unavoidable belongs to Movement 4.

3.8. *When Descendants Meet Again*

Branching is only half of the difficulty.

Suppose a source O produces two independently transformed descendants:

$$O \longrightarrow A$$

and

$$O \longrightarrow B.$$

Later, material from A and B is combined into C :

$$\begin{array}{ccc} O & \longrightarrow & A \\ \downarrow & & \downarrow \\ B & \longrightarrow & C \end{array}$$

What is the generation of C ?

More importantly, what is its origin?

The singular form has become misleading.

C may possess multiple relevant ancestors. A claim in C may derive from A , another from B , and another from a reconstruction produced only after their convergence.

Thus provenance may need to be tracked below the level of the entire artifact.

For a document D containing claims

$$\varphi_1, \varphi_2, \dots, \varphi_n,$$

there need not exist a single provenance value $p(D)$ adequate for every claim.

Instead one may require

$$\text{Prov}(\varphi_i)$$

for individual claims or spans.

This observation justifies the otherwise eccentric typographic apparatus of the present essay. A citation attached to an entire document cannot always represent the derivational history of each statement within it.

Provenance is potentially local.

3.9. *A Loop That Does Not Undo Itself*

We can now return to Shevek's journey.

Let A_t denote Anarres at departure, S_t Shevek at departure, and U_{t+k} the relevant Urrasti state encountered during the journey. The return has the schematic form

$$(S_t, A_t) \longrightarrow (S_{t+k}, U_{t+k}) \longrightarrow (S_{t+n}, A_{t+n}).$$

The endpoint is related to the beginning, but it does not invert the path.

There is no operation

$$T^{-1}$$

that removes what Shevek learned, restores Anarres to its earlier state, recalls every transmission of his work, and returns the entire configuration to t .

The loop closes relationally while remaining historically open.

This distinction is central to the author's Constraint–Recurrence Principle. Recurrence need not mean restoration of a prior state. It may instead mean return to a constraint-compatible region after a nontrivial trajectory.

In the present notation,

$$A_{t+n} \sim_C A_t$$

can coexist with

$$\text{Hist}(A_{t+n}) \neq \text{Hist}(A_t).$$

Indeed, the latter difference is unavoidable if anything happened between the two times.

Proposition 3.9 (Historical non-idempotence of return). *A return operation that restores a selected state-level relation need not restore the historical state of the system.*

Proof. Let a system leave x_t , undergo at least one historically recorded transformation, and later reach x_{t+n} such that

$$x_{t+n} \sim_C x_t.$$

The trajectory to x_{t+n} contains the intervening transformations, whereas the trajectory terminating at x_t does not. Hence their histories differ even when the selected recurrence relation is satisfied. $\square$

A return can close a spatial or structural loop without closing history.

3.10. Three Temporal Probes

The three literary works can now be placed together without reducing them to instances of a generic theme of identity.

Card asks a retrospective question:

Where did this come from?

Zebrowski asks a prospective question:

What may this become and still continue?

Le Guin asks a recurrent question:

What does it mean for what departed to return?

These are different operations on historical structure.

Originism begins with traces and constrains candidate ancestry.

Macrolife begins with an extant organization and opens possible continuation.

Recurrence begins with a relation between departure and return and asks what must remain invariant for the return to be meaningful despite intervening change.

The three forms can be written schematically as

ORIGIN :	?P,
CONTINUATION :	O?,
RECURRENCE :	OXO'.

The prime is the entire point of the third line.

3.11. *Provenance Is Not Merely a Label*

It is tempting to treat provenance as metadata attached to a state:

$$(x, p_x),$$

where p_x might record an author, source, date, or generation number.

The provenance graph shows why this representation can be insufficient.

What matters may not be a label carried by x but the structure of relations connecting x to other states.

If

$$x$$

has two parents,

$$a \rightarrow x, \quad b \rightarrow x,$$

and three descendants,

$$x \rightarrow c_1, \quad x \rightarrow c_2, \quad x \rightarrow c_3,$$

then its provenance is partly constituted by this position within a network of descent.

A scalar label cannot, in general, preserve that structure.

This suggests a stronger conception:

Definition 3.10 (Relational provenance). The *relational provenance* of a state x relative to a provenance graph $\mathcal{G}$ is the derivational structure connecting x to the relevant ancestors, descendants, transformations, and competing paths represented in $\mathcal{G}$.

Provenance is therefore not necessarily something a state *has* in the same sense that it has a checksum.

It may be something a state occupies.

3.12. Return to Which World?

The wall now returns in a different form.

If Anarres and Urras were merely two locations in one homogeneous world, then Shevek's movement could be described primarily as transportation. But the novel insists upon differences in property, obligation, institutional organization, language, sexuality, scientific practice, scarcity, abundance, and political legitimacy [3].

The journey crosses between differently organized fields of affordance.

What may be owned, exchanged, refused, published, commanded, or withheld changes across the boundary.

This suggests that a world cannot be identified merely with a spatial region.

A world, in the sense relevant to the No-World argument, is closer to an organized field of relations within which distinctions and actions become available.

The question

Did Shevek return to Anarres?

is therefore easier than the question

Did Shevek return to the same world?

The first can be answered geographically.

The second requires a theory of which relational structures constitute world-continuation.

We still do not possess that theory.

But the question has now appeared twice: prospectively in Movement 2, and recurrently here.

Its recurrence is evidence that it is not incidental.

3.13. *What Return Has Broken*

Movement 1 began with states and was forced to introduce trajectories:

$$x \rightsquigarrow \gamma.$$

Movement 2 showed that trajectories require constraints on admissible transformation:

$$\gamma \rightsquigarrow (\gamma, A).$$

The present movement has shown that a single trajectory can itself be insufficient.

Branching transmission and convergent descent require

$$\gamma \rightsquigarrow \mathcal{G}.$$

Return then shows that recurrence within $\mathcal{G}$ cannot be represented as simple restoration:

$$OXO', \quad O' \neq O.$$

Finally, the discovery that origins themselves possess provenance prevents the left boundary from being treated as metaphysically privileged merely because a particular inquiry begins there.

The representational object has therefore changed again.

LINEAR-HISTORY INSUFFICIENCY

A trajectory can preserve the history of a path.
It cannot, by itself, preserve the history of a branching provenance structure.

The three novels have now supplied the basic operations required by the argument.

No fourth literary work is needed to add another temporal direction.

What remains is to break the machinery we have constructed.

The next movement therefore changes method. It will not proceed primarily by novel, chronology, or theory. It will proceed by pathological cases.

Each case will ask whether two objects that one part of the formalism treats as equivalent can nevertheless be distinguished by another part.

The order matters.

We begin with the easiest deception: a perfect copy with the wrong history.

We end with the harder case: two present states for which every selected state-level test agrees while their histories still refuse to become one.

Only after those failures have accumulated will it be possible to state the Originist objection in its stronger form.

MOVEMENT IV. PATHOLOGIES

Which distinctions disappear when histories are replaced by their endpoints?

The preceding movements built a vocabulary by following three different problems. Card required a distinction between a surviving state and the history that produced it. Zebrowski required a distinction between material persistence and continuation through transformation. Le Guin required a distinction between a single trajectory and a branching structure of departure, transmission, convergence, and return.

It would now be easy to treat these distinctions as a completed theory. That would be premature.

A formal distinction earns its place only when removing it causes cases that matter to collapse together. The purpose of the present movement is therefore destructive. Instead of asking what the formalism can describe, we ask where simpler descriptions fail.

The cases become progressively less forgiving. A forgery shows that perfect resemblance does not establish descent. Independent rediscovery shows that structural agreement does not require copying at all. Compression and reconstruction show that information can disappear and later reappear without thereby acquiring an unbroken provenance. Gradual replacement separates material persistence from historical continuation. Branching and convergence show that generation count alone cannot characterize provenance. Restoration shows that successful repair does not reverse the history of damage. Civilizational migration asks whether continuation of an organization is enough to preserve its world.

The final case removes the last visual aid. Two states will agree under every state-level test selected for the problem. Nothing in their present form will tell them apart.

Their histories will still differ.

That case is not an exotic exception to the argument. It is the case for which the argument has been preparing.

4.1. Perfect Forgery

Consider an original artifact O and a forgery F .

Ordinary examples make the distinction easy because forgeries contain imperfections. Pigments are anachronistic. Handwriting differs. Metadata is wrong. A cryptographic hash fails. Some sufficiently discriminating state-level test reveals that

$$O \neq F.$$

Those imperfections are irrelevant to the present case.

Assume instead that the forgery is perfect with respect to every state-level test in the selected family $\mathcal{S}$. Write

$$O \equiv_{\mathcal{S}} F.$$

If the artifacts are digital, we may choose the particularly strong case

$$O =_{\text{byte}} F.$$

The forgery is nevertheless a forgery because of how it was produced.

Let

$$\gamma_O$$

denote the history of the original and

$$\gamma_F$$

the history by which the forgery was constructed. Then

$$\text{End}(\gamma_O) \equiv_{\mathcal{S}} \text{End}(\gamma_F)$$

while

$$\gamma_O \neq \gamma_F.$$

Pathology 4.1 (Perfect forgery). For any family of state-level tests $\mathcal{S}$ that does not encode derivational history, agreement under every test in $\mathcal{S}$ does not in general imply common provenance.

The qualification concerning derivational history is essential. One can always define a purportedly state-level property that secretly includes provenance. That maneuver does not solve the problem. It merely moves history into the definition of state.

The forgery therefore supplies the first failed implication:

$$x =_{\text{byte}} y \not\Rightarrow x =_{\text{prov}} y.$$

This failure is stronger than the claim that appearances can deceive.

There need be no state-level deception at all.

The state may be exact.

The genealogy may still be false.

4.2. Independent Rediscovery

Forgery retains an important relation to the original: the forger attempts to reproduce it.

Independent rediscovery removes even that relation.

Suppose two researchers, A and B , work from disjoint evidential collections and arrive independently at the same proposition

$$\varphi.$$

The resulting inscriptions may be semantically equivalent:

$$\varphi_A \simeq_{\mathcal{I}} \varphi_B.$$

They may even be textually identical.

Yet neither result need derive from the other.

Card's account of L $\acute{e}$ vel Forska and the independently pursued work associated with Thoren Magolissian provides a literary instance of this broader pattern: separate research trajectories may converge upon overlapping questions or results without collapsing into a single derivational chain [1].

The provenance graph has the form

$$E_A \longrightarrow \varphi_A$$

$$E_B \longrightarrow \varphi_B$$

rather than

$$\varphi_A \longrightarrow \varphi_B.$$

Pathology 4.2 (Independent rediscovery). Invariant or semantic equivalence between two states does not imply genealogical dependence between them.

Thus

$$x \simeq_{\mathcal{I}} y \not\Rightarrow x \rightsquigarrow_{\text{causal}} y.$$

This failed implication matters because similarity is often treated as evidence of copying. Sometimes it is excellent evidence. It is never, by itself, identical with copying.

The Originist therefore distinguishes convergence by descent from convergence without descent.

The endpoint does not.

4.3. Lossy Compression Followed by Reconstruction

The next case introduces an operation central to the computational motivation for the Originist role.

Let C be a lossy compression operation and R a reconstruction operation. Begin with an artifact x :

$$x \xrightarrow{C} c \xrightarrow{R} \hat{x}.$$

Because C is lossy, there exist distinct inputs x_1 and x_2 such that

$$C(x_1) = C(x_2).$$

Consequently, $C(x)$ does not in general determine x uniquely.

Reconstruction must therefore use something beyond information preserved injectively by the compressed representation. It may exploit priors, regularities, external context, a learned generative model, or constraints on the class of plausible originals.

Suppose nevertheless that reconstruction succeeds spectacularly:

$$\hat{x} =_{\text{byte}} x.$$

The present state has returned exactly.

The lost trajectory has not.

Proposition 4.3 (Reconstruction does not reverse loss). *Let $C : X \rightarrow Y$ be non-injective and let $R : Y \rightarrow X$ be a reconstruction operation. Even when*

$$R(C(x)) = x$$

for a particular x , it does not follow that $R = C^{-1}$.

Proof. Since C is non-injective, there exist $x_1 \neq x_2$ such that

$$C(x_1) = C(x_2) = y.$$

If R is a function, then $R(y)$ has one value. It cannot simultaneously satisfy

$$R(y) = x_1 \quad \text{and} \quad R(y) = x_2.$$

Therefore R is not a two-sided inverse of C on the relevant domain. The fact that $R(C(x)) = x$ for some particular x establishes successful reconstruction in that case, not reversal of the information loss induced by C . $\square$

This distinction is crucial.

A reconstruction can restore content without restoring provenance.

The sequence

$$x \xrightarrow{C} c \xrightarrow{R} x$$

does not reduce historically to

$$x.$$

The endpoint is idempotent with respect to the selected state comparison.

The history is not.

This is the formal situation that motivates generation tracking in repeated compression–regeneration systems such as the proposed Originist role in the compression and repair pipeline considered by the present project. If content passes through

$$R_1 \circ C_1 \circ R_2 \circ C_2$$

and returns to a state indistinguishable from its source, a state-only loss function may report perfect recovery.

An Originist ledger reports that something happened.

4.4. *Ship-of-Theseus Replacement*

Movement 2 used gradual replacement to separate material identity from continuous transformation. We can now sharpen the case.

Let

$$S_0 \rightarrow S_1 \rightarrow \dots \rightarrow S_n$$

be a gradual replacement trajectory satisfying an admissibility criterion $\mathcal{A}$.

Suppose

$$M(S_0) \cap M(S_n) = \emptyset.$$

Now collect the removed components of S_0 and reconstruct a second ship S^* .

The familiar puzzle asks which ship is the original.

The Originist formulation asks a prior question.

What histories are being compared?

We have

$$\gamma_1 : S_0 \rightarrow S_1 \rightarrow \dots \rightarrow S_n,$$

and a second trajectory involving removal, preservation, and reassembly:

$$\gamma_2 : M(S_0) \rightarrow \dots \rightarrow S^*.$$

The question

$$S_n = S^*?$$

is therefore downstream from a richer structure.

The two endpoints inherit different relations to S_0 .

Pathology 4.4 (Competing continuities). A single earlier state may support multiple later claims of continuity under different preserved relations, without those claims being reducible to endpoint similarity.

This pathology prevents admissibility from being treated as a single universal predicate.

The gradual ship may preserve operational continuity.

The reconstructed ship may preserve original material.

A legal system might privilege one relation.

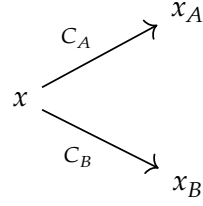
A museum might privilege another.

A theory of personal identity might privilege neither.

The formalism must therefore retain the type of continuation being claimed.

4.5. Branching Copy

Suppose a state x is copied twice:



and suppose both copying operations are exact:

$$x_A =_{\text{byte}} x \quad \text{and} \quad x_B =_{\text{byte}} x.$$

Then

$$x_A =_{\text{byte}} x_B.$$

Yet the copies occupy distinct branches of the provenance graph.

If each branch subsequently changes,

$$x_A \rightarrow y_A, \quad x_B \rightarrow y_B,$$

the common origin does not make the descendants one history.

This matters for the language of continuation. If x is an agent, institution, document tradition, or civilization, branching makes the phrase “the continuation” ambiguous.

There may be several descendants.

Proposition 4.5 (Branching destroys unique succession). *If a provenance state x has two distinct admissible descendants y_1 and y_2 neither of which is derivationally downstream from the other, then descent from x does not determine a unique successor.*

Proof. Both y_1 and y_2 satisfy the stipulated descent relation from x . By assumption neither is downstream from the other. Hence the provenance structure contains no unique descendant selected solely by the fact of descent from x . $\square$

This is the branching problem already suggested by Shevek’s dissemination of knowledge. Once transmission is plural, genealogy ceases to guarantee singularity.

4.6. Why Generation Count Is Not Enough

The provenance notation introduced earlier has so far allowed a statement to carry a generation number:

$$\varphi^{[0]}, \quad \varphi^{[1]}, \quad \varphi^{[2]}.$$

Branching exposes a limitation.

Consider two three-step histories:

$$\gamma_A : O \xrightarrow{R} a_1 \xrightarrow{C} a_2 \xrightarrow{R} x_A,$$

and

$$\gamma_B : O \xrightarrow{C} b_1 \xrightarrow{C} b_2 \xrightarrow{C} x_B.$$

Both endpoints have generation depth three:

$$\text{Depth}_O(x_A; \gamma_A) = \text{Depth}_O(x_B; \gamma_B) = 3.$$

Yet the transformation histories differ:

$$R \circ C \circ R \neq C \circ C \circ C.$$

A scalar depth therefore collapses trajectories that an Originist may need to distinguish.

This is the point at which the fuller provenance notation becomes necessary.

We may write

$$\varphi^{[3:R \circ C \circ R]}$$

rather than merely

$$\varphi^{[3]}.$$

If the transformation history is known only partially, additional fields may record the invariant class preserved and an evidential support value:

$$\varphi^{[3:R \circ C \circ R; \mathcal{I}^+; p=.71]}.$$

The notation is intentionally unpleasant.

The unpleasantness records a real increase in the dimensionality of the problem.

Pathology 4.6 (Scalar provenance insufficiency). Equal generation depth does not imply equivalent derivational history. Consequently, a scalar generation count is insufficient whenever transformation type matters to the inference being performed.

We have now learned that provenance is not adequately represented by a state, a path length, or even necessarily a single path.

4.7. Convergent Descendants

Branching separates descendants.

Convergence brings them together again.

Suppose

$$O \rightarrow A \rightarrow A'$$

and

$$O \rightarrow B \rightarrow B'$$

form distinct branches. Later transformations produce

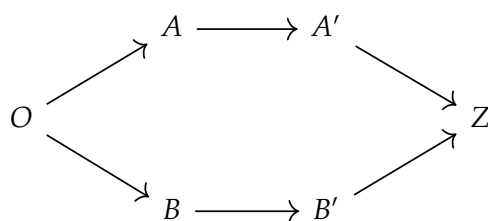
$$A' \rightarrow Z$$

and

$$B' \rightarrow Z.$$

The state Z now has more than one relevant derivational path from O .

The provenance graph contains



The question

$$\text{Depth}_O(Z) = ?$$

is no longer well formed without specifying a path or aggregation rule.

More importantly, convergence can make later states appear to erase earlier branching.

If one observes only Z , the two histories have become invisible.

They have not ceased to have occurred.

Pathology 4.7 (Convergence hides branching). A provenance graph may contain historically relevant branching that is not recoverable from a convergent descendant considered in isolation.

This is the graph-theoretic generalization of the first example in Movement 1.

There,

$$x_A = x_B$$

concealed different paths.

Here a single state Z conceals an entire branching structure.

The Originist problem is becoming less like attaching metadata to objects and more like preserving a topology of descent.

4.8. Restoration from Incomplete Archives

Suppose an original document O is damaged, leaving a surviving fragment F :

$$O \xrightarrow{D} F.$$

An editor later reconstructs the missing material using independent evidence E :

$$(F, E) \xrightarrow{R} \widehat{O}.$$

Assume the reconstruction is correct:

$$\widehat{O} =_{\text{byte}} O.$$

What has been restored?

The content has been restored under byte identity.

The history has not.

The original reached its state without passing through destruction and editorial reconstruction. The restored object did.

Thus

$$O =_{\text{byte}} \widehat{O}$$

while

$$\text{Prov}(O) \neq \text{Prov}(\widehat{O}).$$

This example is important because no error is required.

The reconstruction may be perfect.

Provenance difference is not a synonym for corruption.

Proposition 4.8 (Perfect restoration preserves a wound). *If a transformation destroys provenance-relevant information and a later reconstruction restores the endpoint state using additional information, then perfect state restoration does not erase the historical fact of the intervening loss.*

Proof. Let

$$O \xrightarrow{D} F$$

destroy a distinction required to recover O uniquely from F . Let external evidence E permit a reconstruction

$$R(F, E) = O.$$

The final state agrees with the original. Nevertheless, the realized history of the reconstructed state contains D , the loss of information, the introduction of E , and the reconstruction operation R . The original history does not contain these events. Therefore restoration of state does not erase the historical distinction. $\square$

This is the first case for which the language of a wound becomes useful.

A wound is not necessarily visible in the healed state.

4.9. The Wound

Let

$$q : \Gamma \longrightarrow \Gamma / \sim$$

be an operation that identifies histories under an equivalence relation $\sim$.

Suppose two histories γ_1 and γ_2 differ with respect to a provenance distinction δ , but

$$q(\gamma_1) = q(\gamma_2).$$

After quotienting, δ cannot be recovered from the quotient state alone.

We call this an Originist wound relative to δ .

Definition 4.9 (Originist loss). For a quotient or information-reducing operation q and a provenance-relevant distinction δ , the Originist loss

$$\mathcal{L}_{\text{orig}}(q; \delta)$$

denotes the loss of discriminative capacity concerning δ induced by applying q .

No scalar metric is assumed yet. The notation may denote a logical loss rather than a numerical magnitude.

The minimal condition is

$$\mathcal{L}_{\text{orig}}(q; \delta) > 0$$

whenever there exist γ_1, γ_2 such that

$$\delta(\gamma_1) \neq \delta(\gamma_2)$$

but

$$q(\gamma_1) = q(\gamma_2).$$

The Wound. A wound occurs when an operation makes a distinction unavailable that a later inference may require.

The wound is not identical with damage to the endpoint.

A perfectly restored endpoint may still stand downstream from an irreversible loss of provenance.

This definition explains why compression is not intrinsically objectionable.

Every useful representation forgets something.

The Originist question is whether the forgotten distinction belongs to the future inferential task.

4.10. *A Civilization Reproduced Elsewhere*

We can now return to the Macrolife limit with more machinery available.

Let a civilization C_0 inhabit an environment W_0 . Over time it constructs new habitats, changes its material substrate, modifies its institutions, and transmits its organizational structures into descendants:

$$(C_0, W_0) \rightarrow (C_1, W_1) \rightarrow \dots \rightarrow (C_n, W_n).$$

Suppose the civilizational trajectory satisfies an admissibility criterion

$$\gamma_C \in \mathcal{A}_C.$$

We may therefore have reason to assert

$$C_0 \rightsquigarrow_{\text{causal}} C_n$$

and perhaps even to regard C_n as an admissible continuation of C_0 .

It does not follow that

$$W_0 \equiv_{\text{world}} W_n.$$

The distinction becomes especially important when the environment is no longer a passive background but is itself constructed and transformed by the civilization.

A civilization may continue while changing worlds.

Alternatively, what appears to be a new world may itself be part of the continuation of an older one.

The question cannot be settled by civilizational genealogy alone.

Pathology 4.10 (Civilizational continuity without established world-continuity). The existence of an admissible civilizational trajectory

$$C_0 \rightsquigarrow C_n$$

does not by itself establish

$$W_0 \equiv_{\text{world}} W_n.$$

We have now reached the distinction that the earlier movements repeatedly approached without formalizing.

Persistence of an object, persistence of a civilization, and persistence of a world are separate claims.

4.11. *The Case with Nothing Left to See*

We can now construct the limiting pathology.

Let $\mathcal{S}$ be the complete family of state-level tests selected for a particular task. Suppose two states x_A and x_B satisfy

$$s(x_A) = s(x_B) \quad \text{for every } s \in \mathcal{S}.$$

Write this as

$$x_A \equiv_{\mathcal{S}} x_B.$$

Suppose nevertheless that

$$\gamma_A \neq \gamma_B.$$

Further suppose that the difference between γ_A and γ_B includes a provenance distinction δ relevant to a later operation.

No additional test in $\mathcal{S}$ can recover δ , because the states agree under every test in the selected family.

The only remaining source of the distinction is historical information not encoded by those state tests.

Theorem 4.11 (State-level underdetermination of provenance). *Let $\mathcal{S}$ be a family of functions on a state space X , and define*

$$x \equiv_{\mathcal{S}} y \iff s(x) = s(y) \text{ for every } s \in \mathcal{S}.$$

Let $\Gamma(X)$ be a space of derivational histories with endpoint map

$$\text{End} : \Gamma(X) \rightarrow X.$$

If there exist distinct histories $\gamma_A, \gamma_B \in \Gamma(X)$ such that

$$\text{End}(\gamma_A) \equiv_{\mathcal{S}} \text{End}(\gamma_B),$$

then no inference using only values of tests in $\mathcal{S}$ can, in general, distinguish γ_A from γ_B .

Proof. Let

$$x_A = \text{End}(\gamma_A), \quad x_B = \text{End}(\gamma_B).$$

By hypothesis,

$$s(x_A) = s(x_B)$$

for every $s \in \mathcal{S}$. Therefore any inference whose input consists only of the tuple

$$(s(x))_{s \in \mathcal{S}}$$

receives identical input for x_A and x_B . Such an inference cannot deterministically discriminate the two histories on the basis of those inputs alone. Any successful discrimination must therefore use information not contained in the selected state-level observations. $\square$

This theorem is elementary enough that its proof could almost be omitted.

It is retained because the triviality is revealing.

Once the problem is stated correctly, the impossibility is immediate.

A state cannot disclose a distinction that the representation of that state has erased.

4.12. The Originist Objection

The examples now permit the preliminary objection from Originist objection 1.9 to be stated more sharply.

Originist Objection 4.12 (Strong form). Let q be an abstraction, quotient, compression, canonicalization, or equivalence operation applied to states or histories. The operation is epistemically unsafe for an Originist task whenever there exists a provenance-relevant distinction δ such that

$$\mathcal{L}_{\text{orig}}(q; \delta) > 0$$

and a subsequent inference requires δ .

Equivalence is therefore not objectionable because it forgets.

It is objectionable when it forgets a distinction and subsequently behaves as though no distinction was lost.

This is the Originist objection to premature quotienting.

It does not demand preservation of all history.

Such preservation would often be impossible and almost always be useless.

It demands an account of the wound.

THE ORIGINIST OBJECTION

Do not ask only what an equivalence preserves.
Ask which future questions become unanswerable after the equivalence is applied.

The shift is subtle but consequential.

The usual mathematical question is often

Which differences may safely be ignored?

The Originist adds

Safe for which later operation?

Admissibility therefore applies not only to transformations of objects.

It applies to transformations of representations.

4.13. *The Citation That Did Not Change*

We can now return to a small piece of the present document.

In Movement 1, a claim concerning Level Forska's orientation toward principles of origin rather than merely the identification of a planetary coordinate was presented with a provenance-bearing note. At that point it was marked as directly grounded.

Subsequent inspection of the derivational chain supporting the wording used there does not establish a sufficiently direct path from the present formulation to the primary text to justify the generation-zero classification.

The proposition itself need not be withdrawn.

Its truth value has not thereby changed.

Its wording has not changed.

The historical source from which the underlying material ultimately derives has not changed.

What has changed is the present document's warranted description of its own relation to that source.

The earlier provenance classification must therefore be retyped:

$$\varphi^{[0]} \rightsquigarrow \varphi^{[\omega?]}$$

This is the unique unknown-depth wound in the present manuscript.

It is deliberately not repaired by assigning an arbitrary finite generation count.

The available evidence does not warrant one.

The Wound. The proposition did not change.
 Its history did not change.
 What changed was the document's knowledge of its history.
 The correction therefore belongs neither to the proposition's semantic content nor directly to its truth value. It belongs to its epistemic provenance type.

The distinction can now be written

$$\text{Truth}(\varphi) \neq \text{Prov}(\varphi).$$

More precisely, revision of

$$\text{Prov}(\varphi)$$

does not entail revision of

$\text{Truth}(\varphi).$

Nor does the converse hold.

A proposition may be discovered false while its provenance remains perfectly known.

Truth and provenance are independent coordinates.

This is why provenance cannot be reduced to confidence.

4.14. *Provenance as an Epistemic Type*

The preceding case suggests a stronger interpretation of the superscript notation.

Consider

$$\varphi^{[0]}$$

and

$$\varphi^{[3:R \circ C \circ R]}.$$

Suppose the semantic content is identical.

A conventional representation might treat the two propositions as the same statement accompanied by different metadata.

For Originist reasoning, that description is sometimes too weak.

The provenance class can determine which operations are admissible.

A directly inspected quotation may support a claim about exact wording.

A reconstructed paraphrase may support the semantic claim while failing to support an inference about lexical choice.

An uncertain derivational chain may support exploratory reasoning while being inadequate for a claim whose force depends upon primary-source wording.

Thus provenance can alter what one is entitled to infer even when semantic content is held fixed.

Definition 4.13 (Provenance-sensitive epistemic type). A proposition has a *provenance-sensitive epistemic type* when its derivational history constrains the class of inferential operations for which it is admissible evidence.

Under this interpretation,

$$\varphi^{[0]}$$

and

$$\varphi^{[3:R \circ C \circ R]}$$

may be semantically equivalent while remaining epistemically non-substitutable.

The superscript is no longer decorative metadata.

It participates in the admissibility structure.

This closes the circuit between provenance and TARTAN-like constraint reasoning: provenance does not merely tell us where a representation came from. It constrains what transformations of that representation remain licensed.

4.15. *An Ecology of Failed Implications*

The pathologies can now be condensed without replacing their worked examples.

Perfect forgery established

$$x =_{\text{byte}} y \not\Rightarrow x =_{\text{prov}} y.$$

Independent rediscovery established

$$x \simeq_{\mathcal{I}} y \not\Rightarrow x \rightsquigarrow_{\text{causal}} y.$$

The corruption, ruin, and pathological-growth cases established

$$x \rightsquigarrow_{\text{causal}} y \not\Rightarrow x \text{ is admissibly continued by } y.$$

The Macrolife limit established that even admissible civilizational continuation does not automatically give

$$W_t \equiv_{\text{world}} W_{t+n}.$$

Generation analysis established

$$\text{Depth}_O(x; \gamma_A) = \text{Depth}_O(y; \gamma_B) \not\Rightarrow \gamma_A \sim_{\text{gen}} \gamma_B$$

when $\sim_{\text{gen}}$ is intended to encode more than equal path length.

Restoration established

$$x_{\text{restored}} =_{\text{byte}} x_{\text{original}} \not\Rightarrow \text{Hist}(x_{\text{restored}}) = \text{Hist}(x_{\text{original}}).$$

Return established

$$O' \sim_{\mathcal{C}} O \not\Rightarrow O' = O.$$

No single one of these failures is especially mysterious.

Their accumulation is the result.

Relations that ordinary language repeatedly compresses into “same” have separated under pressure.

4.16. *What the Pathologies Leave Standing*

The destructive work is now sufficient.

We began the essay with a state

$$x.$$

Endpoint insufficiency forced the trajectory

$$\gamma.$$

Branching and convergence forced the provenance graph

$$\mathcal{G}.$$

Causal insufficiency forced admissibility

$$A.$$

Repeated failures of state-level identity forced explicit invariants

$$\mathcal{I}.$$

The civilizational cases repeatedly forced a question not yet answered by any of them:

$$\omega.$$

The progression should not be written as a hierarchy in which each later object contains the truth of the earlier one.

It is better represented as a sequence of failures:

$$\text{STATE} \xrightarrow{\text{insufficient}} \text{TRAJECTORY} \xrightarrow{\text{insufficient}} \text{PROVENANCE} \xrightarrow{\text{insufficient}} \text{ADMISSIBILITY} \xrightarrow{?} \text{WORLD}.$$

The question mark is essential.

Nothing so far establishes that worldhood is simply the next layer in a well-ordered construction.

It may instead be the point at which the demand for a single underlying object becomes unstable.

That possibility is the subject of the final movement.

AFTER THE PATHOLOGIES

State equality does not determine historical equality.
Historical descent does not determine admissible continuation.
Admissible continuation does not yet determine continuation of a world.

The three literary probes can therefore return one final time.

Card asked how a lost world might be reconstructed from traces.

Zebrowski asked how a civilization might propagate beyond the material world from which it arose.

Le Guin asked what it means to leave a world, cross its boundaries, transmit something beyond them, and return to an origin that has continued changing in one's absence.

These questions no longer require three separate formalisms.

They now occupy different regions of one unresolved problem.

What is it that persists when the state does not?

What is it that returns when the origin has changed?

What is it that has been preserved when a civilization survives but the relations constituting its world may not?

Movement V will not introduce another pathology merely to enlarge the apparatus again.

It will ask whether the apparatus already earned is sufficient to say what descent means.

MOVEMENT V. DESCENT

If neither matter nor state is fundamental to continuity, what exactly descends?

The word “descent” usually sounds biological. Something descends from something else because reproduction connects them. The parent need not remain alive for the descendant to exist, and the descendant need not resemble the parent in every respect. What matters is that there is a history connecting them.

The same word becomes useful outside biology once the preceding cases are placed together. A manuscript can descend from another manuscript. A reconstruction can descend from fragments. A scientific idea can descend through several translations. A civilization can descend from a civilization whose material conditions it no longer shares. A political society can return to an inherited problem without returning to an earlier state.

The difficult question is not whether these things change. They obviously do. The question is what kind of historical structure makes some changes count as continuation and others as replacement, corruption, forgery, rediscovery, or the beginning of something else.

The previous movements did not discover a single substance that survives all of these cases. They discovered instead a sequence of insufficiencies. States were insufficient, so trajectories were retained. Trajectories were insufficient, so branching provenance was retained. Causal provenance was insufficient, so admissibility became necessary. Admissible continuation at the level of an object or civilization still failed to answer whether a world continued.

The temptation now is to name the final object and declare the ontology finished.

The present movement resists that temptation.

The theories brought into contact here—RSVP, TARTAN, Chain of Memory, Spherepop, recurrence, irreversibility, and the No-World argument—do not all identify the same primitive. Their usefulness lies precisely in the fact that they constrain different parts of the problem.

The synthesis is therefore not a reduction.

It is a geometry of descent.

5.1. *The Stack Is Not a Ladder*

The argument can now be summarized by the sequence

$$\text{State} < \text{Trajectory} < \text{Provenance} < \text{Admissibility} < \text{Worldhood}.$$

The symbol $<$ must not be interpreted as an ontological ordering.

It means only that, for the questions considered in this essay, each term became necessary after the preceding term failed to discriminate cases that needed to remain distinct.

The progression is therefore better written

$$\text{State} \xrightarrow{F_1} \text{Trajectory} \xrightarrow{F_2} \text{Provenance} \xrightarrow{F_3} \text{Admissibility} \xrightarrow{F_4} \text{Worldhood},$$

where each F_i denotes a failure of sufficiency.

The first failure was endpoint convergence:

$$x_A = x_B, \quad \gamma_A \neq \gamma_B.$$

The second was linear-history insufficiency: a single path could not preserve branching and convergence.

The third was causal insufficiency:

$$x \rightsquigarrow_{\text{causal}} y$$

did not guarantee that y constituted an acceptable continuation of x .

The fourth remains only partially formalized. A civilization may possess a defensible admissible trajectory while the persistence of the world in which its practices are meaningful remains undecided.

Proposition 5.1 (Non-collapse of the descriptive stack). *No level of the sequence above may be replaced by the immediately preceding level without collapsing at least one distinction established in Movement 4.*

Proof. State alone collapses perfect forgery and convergent reconstruction when their selected endpoint properties agree. A single trajectory collapses relevant branching and convergence in a provenance graph. Causal provenance collapses admissible continuation with corruption and other causally downstream but constraint-violating transformations. Finally, admissible continuation of an object or civilization does not, by itself, settle world-continuation, as shown by pathology 4.10. Hence each enlargement is motivated by a distinction unavailable at the preceding level. $\square$

The stack is therefore methodological rather than metaphysical.

It records where simpler descriptions broke.

5.2. RSVP and the Field Description of Descent

The Relativistic Scalar–Vector Plenum framework provides one way to loosen the assumption that persistence must belong to a sharply bounded object.

In its characteristic notation, a configuration is described through a scalar field Φ , a vector field $\mathbf{v}$, and an entropy-like scalar field S :

$$\mathfrak{R} = (\Phi, \mathbf{v}, S).$$

For present purposes, the importance of this representation is not any particular field equation. It is that an entity may be represented as a structured region within a changing field rather than as an indivisible bearer of identity.

Let

$$\mathfrak{R}_t = (\Phi_t, \mathbf{v}_t, S_t)$$

and

$$\mathfrak{R}_{t+\Delta t} = (\Phi_{t+\Delta t}, \mathbf{v}_{t+\Delta t}, S_{t+\Delta t})$$

denote successive field configurations.

The question of continuation need not then take the form

$$x_t = x_{t+\Delta t}.$$

It can instead ask whether a pattern of constraints, flows, boundaries, and relations persists through the field evolution.

This is structurally compatible with the Macrolife case. Complete replacement of material constituents need not terminate a history if the relevant organization is continuously realized through changing substrate.

It is also compatible with the Originist case. A present configuration may retain traces of transformations without containing a literal copy of its earlier state.

The field representation therefore supplies a useful warning against substantialism:

FIELD PERSISTENCE

Persistence need not require a substance that remains numerically unchanged.
It may be realized by constrained transformation of a structured field.

This does not establish that every relevant notion of identity is reducible to RSVP dynamics.

The stronger claim is unnecessary.

RSVP supplies a natural substrate on which trajectory-first reasoning can be stated without presupposing the very state identity that the pathologies have made doubtful.

5.3. TARTAN and the Geometry of Admissibility

The transition from causal history to admissible history is where TARTAN enters most directly. Suppose the space of possible realizations is X , and let

$$A \subseteq X$$

denote an admissible region determined by a collection of constraints.

A transformation

$$T : x \mapsto y$$

is not licensed merely because y resembles x , nor merely because $x \rightsquigarrow_{\text{causal}} y$.

The relevant question is whether the realized trajectory remains compatible with the constraints defining the task.

For a trajectory

$$\gamma : [0, 1] \rightarrow X,$$

a local admissibility criterion might require

$$\gamma(t) \in A \quad \forall t \in [0, 1].$$

But the pathologies already showed why local membership may be insufficient. Some constraints concern the history as a whole.

We therefore distinguish state admissibility from trajectory admissibility:

$$A_X \subseteq X$$

and

$$A_T \subseteq \Gamma(X).$$

It is possible that every state on a path satisfies the state-level constraints while the path itself violates a provenance condition:

$$\gamma(t) \in A_X \quad \forall t, \quad \gamma \notin A_T.$$

A perfect forgery provides the simplest example.

The endpoint may be admissible as an artifact state.

The derivation may be inadmissible for a task requiring authentic descent.

Remark 5.2 (Admissibility is constraint-relative, not derived). Throughout what follows, admissibility is understood relative to a specified family of constraints $\mathcal{C}$. More explicitly, one may write $A_{\mathcal{C}}$ for the admissible states or histories determined relative to $\mathcal{C}$, and $\mathfrak{A}_{\mathcal{C}}$ for the corresponding admissibility functional. When only one constraint family is under consideration, the subscript will be suppressed and the shorter notation A or $\mathfrak{A}$ retained. This suppression should not be read as asserting a universal or independently derived notion of admissibility: the relevant constraint family remains a parameter of the construction. Every bare occurrence of A or $\mathfrak{A}$ elsewhere in this document, including in the Path Category movement, is to be read under this convention.

Definition 5.3 (Trajectory admissibility). Let $\Gamma(X)$ be a space of histories over X . A trajectory-level admissibility predicate is a map

$$\mathfrak{A} : \Gamma(X) \rightarrow \{0, 1\}$$

or, more generally, a graded functional

$$\mathfrak{A} : \Gamma(X) \rightarrow [0, 1]$$

whose value depends upon properties of the realized history not necessarily recoverable from its endpoint.

This is the formal location of the Originist inside a TARTAN-like system.

The Originist does not merely improve the representation of x .

It supplies variables on which

$$\mathfrak{A}(\gamma_x)$$

may depend.

5.4. Chain of Memory and the Preservation of Derivational Constraint

Chain of Memory can now be distinguished sharply from an ordinary store of past states.

A memory system conceived as an archive may retain

$$x_0, x_1, \dots, x_n.$$

That is useful, but it does not necessarily preserve why one state followed another.

A derivational memory requires at least

$$x_0 \xrightarrow{T_1} x_1 \xrightarrow{T_2} \dots \xrightarrow{T_n} x_n.$$

A branching memory requires still more:

$$\mathcal{G} = (V, E, \tau).$$

Chain of Memory is therefore most naturally interpreted here not as a larger context window but as persistence of constraints across transformations.

The distinction is important.

Remembering every prior token is not equivalent to remembering the derivation that licensed the current state.

Conversely, a system may discard enormous quantities of state information while preserving exactly the derivational relations required for later reasoning.

This suggests a minimal Originist interpretation of CoM:

CoM : preserve the distinctions required for future admissibility tests.

The criterion is prospective.

A memory is valuable not because the past deserves exhaustive duplication, but because future operations may require distinctions that would otherwise be irrecoverable.

This is precisely the lesson of $\mathcal{L}_{\text{orig}}$.

5.5. *Spherepop and Event-Structured History*

Spherepop contributes a complementary vocabulary.

Where RSVP emphasizes fields and TARTAN emphasizes admissibility, Spherepop treats histories through events of distinction, binding, refusal, and collapse.

Let an event alphabet be written schematically as

$$\Sigma_{\text{sp}} = \{\text{Pop}, \text{Refuse}, \text{Bind}, \text{Collapse}\}.$$

A trajectory can then carry not only states but event types:

$$x_0 \xrightarrow{\text{Pop}} x_1 \xrightarrow{\text{Bind}} x_2 \xrightarrow{\text{Refuse}} x_3.$$

This makes explicit something the scalar generation count could not.

Two histories of equal length can have different event structure.

Thus

$$\text{Depth}_O(x; \gamma_1) = \text{Depth}_O(y; \gamma_2)$$

while

$$\tau(\gamma_1) \neq \tau(\gamma_2).$$

The full provenance tag

$$[3 : R \circ C \circ R]$$

is a computationally mundane version of the same idea.

History has syntax.

The order and type of transformations matter.

If event composition is noncommutative, then in general

$$T_2 \circ T_1 \neq T_1 \circ T_2.$$

Consequently, even the multiset of transformations is insufficient.

The path retains order.

This provides another reason why provenance cannot be compressed into a generation number without loss.

5.6. Irreversibility Without Mystification

Irreversibility has appeared repeatedly in the essay, but its role can now be stated precisely.

Suppose

$$T : X \rightarrow Y$$

identifies states that differ under a provenance-relevant distinction δ . Then

$$\mathcal{L}_{\text{orig}}(T; \delta) > 0.$$

A later operation may successfully construct a state equivalent to the earlier one:

$$R(T(x)) \equiv_{\delta} x.$$

This does not imply historical reversal.

The sequence

$$x \xrightarrow{T} y \xrightarrow{R} x'$$

has occurred.

Even if

$$x' =_{\text{byte}} x,$$

the realized trajectory contains an event absent from the history terminating at x .

The irreversibility relevant here is therefore not simply the impossibility of returning to a previous state.

A previous state may be restored exactly.

The irreversibility lies in the impossibility of making the restoration retroactively become the original history.

Proposition 5.4 (Historical irreversibility). *Let a realized history contain a nonidentity transformation T . No later state-level restoration operation can make the realized history identical to a history in which T never occurred.*

Proof. Let

$$\gamma_1 = (x)$$

denote the history terminating at the initial state prior to T , and let

$$\gamma_2 = (x \xrightarrow{T} y \xrightarrow{R} x')$$

be the realized transformed-and-restored history.

Even if $x' = x$, the ordered event sequence of γ_2 contains T and R , whereas γ_1 does not. Therefore

$$\gamma_1 \neq \gamma_2.$$

No property of the endpoint can alter the fact that these events belong to one realized history and not the other. $\square$

This is the simplest formal statement of the essay's temporal asymmetry.

Return can restore a state.

It cannot un-happen a history.

5.7. The Constraint–Recurrence Principle

The Le Guinian return can now be expressed without treating recurrence as literal repetition.

Let

$$\gamma : x_0 x_1 \cdots x_n.$$

Suppose

$$x_n \sim_C x_0$$

for a selected family of constraints C , while

$$x_n \neq x_0.$$

The trajectory has returned to a constraint-compatible region without restoring the initial state.

This motivates the following formulation.

Proposition 5.5 (Constraint–Recurrence Principle). *Recurrence relevant to historical continuation may be defined by return to an admissible constraint class rather than by restoration of a prior state. Accordingly,*

$$x_n \sim_C x_0$$

may constitute recurrence even when

$$x_n \neq x_0$$

and

$$\text{Hist}(x_n) \neq \text{Hist}(x_0).$$

The proposition explains why return can be genuine without being reversible.

Shevek returns to Anarres.

The return is not false merely because neither Shevek nor Anarres is exactly as before.

The difference is what makes the return historical.

5.8. A World Has a History Too

The No-World argument becomes relevant once worldhood is treated not as a primitive container but as something reconstructed from relations, distinctions, continuities, and constraints.

If a world were simply a fixed background W , then the persistence question would be easy to state:

$$x_t, x_{t+n} \in W.$$

Both states occur in the same world because the container has been held fixed by assumption.

The assumption is precisely what the present framework cannot make without argument.

Suppose instead that worldhood at time t is realized through a relational structure

$$W_t = \mathfrak{W}(X_t, B_t, A_t, \text{Rel}_t),$$

where X_t denotes realized states, B_t relevant boundaries, A_t admissible transformations, and Rel_t the relations through which states acquire practical or semantic significance.

Then

$$W_t \equiv_{\text{world}} W_{t+n}$$

is no longer trivial.

The relation must be earned.

A Macrolife civilization may preserve a genealogy while changing the boundaries, affordances, material conditions, and admissibility relations constituting its world.

Likewise, Shevek may return geographically while the relational world of Anarres has changed.

And Card's Originist may reconstruct not merely the ancestry of a population but a vanished field of relations in which the surviving traces once made sense.

The world itself has become an Originist object.

5.9. *Recovery and Propagation*

The relation among the three literary probes can now be stated in its strongest form.

Originism treats worldhood retrospectively:

traces $\rightsquigarrow$ candidate worlds.

Macrolife treats worldhood prospectively:

world $\rightsquigarrow$ candidate descendant worlds.

The Dispossessed inserts recurrence:

$$W_0 \rightsquigarrow W_1 \rightsquigarrow W'_0,$$

where

$$W'_0 \neq W_0$$

need not prevent an appropriate recurrence relation.

Card therefore asks how a world can be recovered from what remains.

Zebrowski asks how a world can propagate through what changes.

Le Guin asks how a world can be left and returned to without pretending that departure had no consequences.

These are not three definitions of worldhood.

They are three operations that any adequate account of world-continuation must survive.

5.10. *Perhaps the Object Is a Class of Histories*

The essay began by replacing state comparison with trajectory comparison.

We can now ask whether individual trajectories are themselves too specific.

Let

$$\gamma_1, \gamma_2 \in \Gamma(X).$$

Suppose they differ in details irrelevant to a selected continuation criterion while preserving the same admissibility structure.

Define an equivalence relation

$$\gamma_1 \sim_A \gamma_2$$

when the two trajectories are equivalent under the selected admissibility criterion.

The relevant object becomes

$$[\gamma]_A.$$

This is the trajectory-class proposal:

$$[OX]_A.$$

It has an immediate attraction.

If state identity is too strict and unrestricted causal ancestry too weak, perhaps continuity belongs neither to the endpoint nor to the exact path but to an admissibility-quotiented class of histories.

Yet the Originist objection applies immediately.

What does the quotient forget?

If

$$q_A : \Gamma(X) \rightarrow \Gamma(X)/\sim_A,$$

then we must ask

$$\mathcal{L}_{\text{orig}}(q_A; \delta)$$

for every provenance distinction δ relevant to subsequent inference.

The trajectory-class proposal therefore cannot simply be declared the final ontology.

Its own quotient carries a wound.

5.11. *Perhaps the Object Is the Graph*

The provenance graph avoids one weakness of the trajectory class by retaining branching and convergence.

Instead of

$$[\gamma]_{A'}$$

we might privilege

$$\mathcal{G} = (V, E, \tau, A).$$

This object can represent multiple origins, competing reconstructions, independent rediscoveries, copied descendants, convergence, and recurrence.

It is therefore more expressive than a single trajectory.

But expressiveness is not fundamentality.

The graph itself depends upon decisions about what counts as a vertex, which transformations deserve an edge, how finely transformations are typed, which uncertain relations are represented, and where the graph is truncated.

A graph of provenance has provenance.

The representation is not outside the problem it represents.

5.12. *No Final Primitive Is Required*

Three candidates now remain visible:

$$\gamma, \quad [\gamma]_{A'}, \quad \mathcal{G}.$$

The first preserves a realized path.

The second suppresses distinctions declared irrelevant under an admissibility relation.

The third preserves branching structure at the cost of requiring explicit choices about granularity and representation.

Nothing in the preceding argument requires one of these to be declared metaphysically primitive.

Indeed, doing so would reproduce the error against which the essay has argued: a representation would be selected, its losses would be forgotten, and the result would then be mistaken for the object itself.

The more defensible conclusion is conditional.

PRIMITIVE-OBJECT REFUSAL

Choose the weakest historical object that preserves every distinction required by the inference being performed.
Record what the choice forgets.

This is less satisfying than a final ontology.

It is also more consistent with the Originist objection.

5.13. *Nothing Original Need Survive*

We can now return to the title without metaphor.

Let an origin O undergo a long admissible history

$$O \rightarrow x_1 \rightarrow x_2 \rightarrow \cdots \rightarrow x_n.$$

Suppose no material component of O remains in x_n :

$$M(O) \cap M(x_n) = \emptyset.$$

Suppose further that no byte-exact representation of O survives, and that some details of its history are irrecoverable.

It may nevertheless be the case that

$$[Ox_n]_{\mathcal{A}}$$

constitutes a defensible continuation under the relevant constraints.

If so, nothing original in the narrow material or state-identical sense need survive.

What survives is not necessarily a thing.

It may be a constrained descent relation.

This is why the title should not be read nihilistically.

The claim is not

nothing need survive.

The claim is

nothing *original* need survive.

Something must constrain the descent if the word “continuation” is to do more work than “caused by”.

But the constraint need not be an unchanged fragment carried intact from the beginning.

5.14. *Three Ways of Losing the Original*

Card removes the origin by temporal distance.

The present contains traces, records, reconstructions, and hypotheses, but the origin itself is not available for inspection. Originism therefore asks what can be recovered without pretending that reconstruction is direct possession of the past [1].

Zebrowski removes the origin by transformation.

Civilization persists by becoming capable of inhabiting forms and environments radically unlike those from which it began. Continuation therefore cannot be identified with indefinite conservation of the initial substrate [2].

Le Guin removes the origin by return.

Shevek comes back, but the existence of the journey prevents return from being restoration. The origin encountered after recurrence is historically later than the origin that was left [3].

Thus the original disappears in three different ways:

distance, transformation, recurrence.

The same formal demand survives all three.

Do not infer identity of history from adequacy of state.

5.15. *This Document Has a Trajectory*

The provenance apparatus of this essay has deliberately made the document slightly harder to read.

That cost requires justification.

The apparatus is not intended to simulate scientific precision by attaching numbers to uncertain claims. Nor is it intended as a typographic joke about the subject matter.

Its function is to make one distinction locally visible.

The document presented to the reader is a state.

Its sources, drafts, paraphrases, reconstructions, corrections, and compilations constitute a history.

Those objects are not identical.

The same final PDF could, in principle, have been produced by many different histories. One could be typed directly from inspected sources. Another could be reconstructed from damaged notes. Another could be repeatedly summarized and regenerated before returning to exactly the same final wording.

If the PDFs are byte-identical, no inspection of their bytes distinguishes those histories.

This manuscript therefore refuses to treat its final state as a complete description of itself.

The provenance tags are incomplete.

That incompleteness is not a defect hidden by the apparatus.

It is one of the things the apparatus records.

5.16. Closure Without Exhaustion

The argument can stop here without claiming that the topic has been exhausted.

Closure is supplied by a different criterion.

The three literary probes initially forced a growing sequence of distinctions. Each enlargement answered a failure produced by the preceding representation.

State required trajectory.

Trajectory required provenance structure.

Provenance required admissibility.

Admissibility raised the unresolved problem of world-continuation.

The pathology catalog then tested those distinctions against forgery, rediscovery, compression, reconstruction, replacement, branching, convergence, restoration, civilizational migration, and exact endpoint agreement.

The final movement has not produced another forced extension of the stack.

Instead, the existing apparatus has been sufficient to locate the remaining uncertainty in the choice of primitive itself.

That is a legitimate stopping condition.

The question remains open whether the most useful fundamental object for a given theory is

$$\gamma,$$

$$[\gamma]_{A'}$$

or

$$\mathcal{G}.$$

The essay need not resolve this choice because its central claim survives all three representations.
 In each case, history contains distinctions not guaranteed to be recoverable from the endpoint.
 In each case, quotienting can erase distinctions required by later inference.

In each case, continuation must be evaluated over transformations rather than assumed from resemblance.

And in each case, restoration of state does not undo descent.

FINAL PROPOSITION

Continuity is not, in general, a property of states considered in isolation.
 It is a property attributed under constraints to histories of transformation.

Card's Originist looks backward along those histories.

Zebrowski's Macrolife extends them forward.

Le Guin bends them toward recurrence.

None supplies an unchanged object capable of carrying identity by itself.

None needs to.

The history is not an inconvenience surrounding the state.

It is part of what the state cannot say.

State $\neq$ History

EPILOGUE: WHAT THIS DOCUMENT CANNOT TELL YOU ABOUT ITSELF

Does the state of a text determine what kind of text it is?

The proposition did not change. Its history did.

—provisional, pending the reader's own reconstruction

This document has, at every point, been an instance of its own subject rather than an illustration standing outside it. *The claims made about Leyel's archive, about the Anarres wall, about the substrate migrations of a macrolife civilization* have themselves passed through paraphrase, compression, and re-expression before arriving here; none of them carry a ^[0] tag, and none should. What the apparatus above has tried to hold open is not the possibility of avoiding reconstruction but the requirement of *knowing where it happened*.

CLOSING CLAIM, HELD RATHER THAN ASSERTED OUTRIGHT

$\gamma_x \neq x$, and the difference is not decorative.

Two objects presently indistinguishable at the level of $=_{\text{byte}}$ may remain permanently distinguishable at the level of $=_{\text{prov}}$. The essay has not tried to collapse this gap. It has tried to make the gap load-bearing.

The three probes converge here without merging. Card’s question, $?P$, remains open in the ordinary sense that most origins are not recoverable and the essay has not claimed otherwise. Zebrowski’s question, $P?$, remains open in the stronger sense that admissible continuation is a standing constraint problem, not a fact settled once for a given substrate. Le Guin’s question, OXO' , is the one this document has quietly been performing rather than merely describing: whatever returns at the end of an epilogue is $\sim_C$ *what began the essay*, not $=_{\text{byte}}$ *it*.

$$O \longrightarrow X \longrightarrow O' \curvearrowright O' \sim_C O$$

The Wound.

Consider, once more, the proposition attached earlier to $[\omega?]$. Nothing asserted by it has been retracted in the course of this document. What changed is not its content but the set of operations a careful reader is now entitled to perform with it — citation, extension, quotation, reliance. $\mathcal{L}_{\text{orig}}$ was defined so that this sentence could be written truthfully rather than merely dramatically: some quotient taken early in the essay’s own drafting made a distinction unrecoverable, and this paragraph is the residue of that loss, not a demonstration staged for effect.

Continuity is a property of trajectories, not of states. That sentence has now appeared *in at least one earlier form*, and this final instance of it is not guaranteed to be $=_{\text{byte}}$ *that earlier one*. Whether it is $\simeq_{\mathcal{J}}$ it — whether the invariant the essay set out to preserve has in fact survived the compression of writing it down — is, appropriately,

reconstructed spans in this epilogue: 2 (running total, whole document)

APPENDICES

MOVEMENT I. PATH SPACES, ENDPOINT MAPS, AND PROVENANCE GRAPHS

What mathematical structure is minimally required to distinguish a state from the histories that terminate in it?

The body of the essay deliberately used only as much mathematics as each argument required. The present appendix collects the more technical consequences of treating histories rather than states as first-class objects.

The central construction is elementary. A state space tells us what may be present. A path space tells us how one state may become another. An endpoint map forgets that history and retains only where it finished. Once written this way, the Originist problem becomes a problem about the information lost by that forgetting operation.

This appendix also makes precise the transition from a single trajectory to a provenance graph. That transition matters whenever histories branch, converge, or admit more than one derivational route between the same states. In those cases there is no unique generation depth unless a path or aggregation rule has first been selected.

Nothing here requires the state space to be continuous. The same definitions apply to manuscripts, model outputs, software artifacts, archival records, or civilizational states. When a continuous structure is useful, it will be introduced explicitly rather than presumed.

A.1. States and Histories

Let X be a nonempty set of states. Let $\mathcal{T}$ be a collection of admissible transformation labels. A finite history over X is an expression

$$\gamma = (x_0 \xrightarrow{T_1} x_1 \xrightarrow{T_2} \dots \xrightarrow{T_n} x_n),$$

where

$$x_i \in X \quad \text{and} \quad T_i \in \mathcal{T}.$$

Denote the collection of such histories by

$$\Gamma_{\mathcal{T}}(X).$$

When the transformation labels are irrelevant or understood, write simply

$$\Gamma(X).$$

Define the origin and endpoint maps

$$\text{Orig} : \Gamma(X) \rightarrow X, \quad \text{End} : \Gamma(X) \rightarrow X$$

by

$$\text{Orig}(\gamma) = x_0, \quad \text{End}(\gamma) = x_n.$$

The map End is the simplest formal model of state-oriented observation.

It forgets everything except the terminal state.

Definition A.1 (Endpoint fibre). For $x \in X$, the *endpoint fibre* over x is

$$\text{End}^{-1}(x) = \{\gamma \in \Gamma(X) : \text{End}(\gamma) = x\}.$$

An Originist question is therefore frequently a question about the internal structure of an endpoint fibre.

If

$$|\text{End}^{-1}(x)| > 1,$$

then the endpoint does not uniquely determine its history.

Proposition A.2 (Endpoint non-identifiability). If there exist distinct histories

$$\gamma_1 \neq \gamma_2$$

such that

$$\text{End}(\gamma_1) = \text{End}(\gamma_2),$$

then no function

$$f : X \rightarrow \Gamma(X)$$

can recover the realized history from the endpoint alone for every history in $\Gamma(X)$.

Proof. Assume such a function f exists. Let

$$\text{End}(\gamma_1) = \text{End}(\gamma_2) = x.$$

Correct recovery would require simultaneously

$$f(x) = \gamma_1$$

and

$$f(x) = \gamma_2.$$

Since f is a function and $\gamma_1 \neq \gamma_2$, this is impossible. □

The proposition formalizes the most elementary Originist obstruction.

The problem is not insufficient computational power.

The information is absent from the endpoint representation.

A.2. Observation as Quotienting

In practice, an observer rarely has access even to the complete state x . Instead, a measurement or representation map

$$m : X \rightarrow Y$$

produces an observable state $m(x)$.

This induces an equivalence relation

$$x \sim_m y \iff m(x) = m(y).$$

The observer therefore works not directly with X but with equivalence classes

$$[x]_m = \{y \in X : m(y) = m(x)\}.$$

Composing observation with the endpoint map gives

$$\Gamma(X) \xrightarrow{\text{End}} X \xrightarrow{m} Y.$$

Thus two distinct losses may occur.

First,

$$\text{End}$$

forgets history.

Second,

$$m$$

may forget distinctions among states.

The composite

$$m \circ \text{End}$$

therefore identifies histories whenever their endpoints are observationally equivalent.

Proposition A.3 (Nested underdetermination). For histories $\gamma_1, \gamma_2 \in \Gamma(X)$,

$$\text{End}(\gamma_1) = \text{End}(\gamma_2)$$

implies

$$m(\text{End}(\gamma_1)) = m(\text{End}(\gamma_2)),$$

but the converse need not hold.

Proof. The forward implication follows immediately from applying m to equal arguments. For the converse, choose distinct states $x_1 \neq x_2$ satisfying

$$m(x_1) = m(x_2),$$

and histories terminating at x_1 and x_2 , respectively. Their observations agree although their endpoints need not. $\square$

The distinction matters whenever apparent identity is defined relative to a measurement regime.

Byte equality, semantic similarity, invariant equivalence, and visual resemblance correspond to different choices of m .

None should be mistaken for history itself.

A.3. Equivalence Relations on Histories

Exact equality of histories is often too strong.

Suppose two histories differ only in transformations irrelevant to a specified task. We may introduce an equivalence relation

$$\sim_A$$

on $\Gamma(X)$ and form the quotient

$$\Gamma(X)/\sim_A.$$

For $\gamma \in \Gamma(X)$, write

$$[\gamma]_A$$

for its equivalence class.

The central warning of the essay can now be stated as a condition on such quotients.

Let

$$\delta : \Gamma(X) \rightarrow D$$

be a provenance-relevant observable.

If there exist

$$\gamma_1 \sim_A \gamma_2$$

while

$$\delta(\gamma_1) \neq \delta(\gamma_2),$$

then δ does not descend to a well-defined function on the quotient.

Theorem A.4 (Descent criterion for provenance observables). *Let $q : \Gamma(X) \rightarrow \Gamma(X)/\sim$ be the canonical quotient map. A function*

$$\delta : \Gamma(X) \rightarrow D$$

factors through the quotient, so that there exists

$$\bar{\delta} : \Gamma(X)/\sim \rightarrow D$$

satisfying

$$\delta = \bar{\delta} \circ q,$$

if and only if δ is constant on every equivalence class of $\sim$.

Proof. Suppose first that

$$\delta = \bar{\delta} \circ q.$$

If

$$\gamma_1 \sim \gamma_2,$$

then

$$q(\gamma_1) = q(\gamma_2).$$

Hence

$$\delta(\gamma_1) = \bar{\delta}(q(\gamma_1)) = \bar{\delta}(q(\gamma_2)) = \delta(\gamma_2).$$

Thus δ is constant on equivalence classes.

Conversely, suppose δ is constant on every equivalence class. Define

$$\bar{\delta}([\gamma]) = \delta(\gamma).$$

Constancy on equivalence classes guarantees that this definition does not depend upon the representative γ . Therefore $\bar{\delta}$ is well-defined and

$$\delta = \bar{\delta} \circ q.$$

□

This familiar quotient criterion gives the Originist objection a precise mathematical form.

A provenance quantity survives quotienting exactly when it is constant on the histories that the quotient identifies.

If it is not constant, the quotient destroys the ability to recover it.

A.4. From Paths to Directed Graphs

A single history assumes a linear ordering of derivation.

Branching requires a directed graph

$$\mathcal{G} = (V, E, \tau),$$

where

$$\tau : E \rightarrow \mathcal{T}$$

labels edges by transformation type.

For vertices $u, v \in V$, let

$$\Pi_{\mathcal{G}}(u, v)$$

denote the collection of directed paths from u to v .

A provenance graph may therefore encode

$$|\Pi_{\mathcal{G}}(u, v)| = 0,$$

$$|\Pi_{\mathcal{G}}(u, v)| = 1,$$

or

$$|\Pi_{\mathcal{G}}(u, v)| > 1.$$

These correspond respectively to no represented derivation, a unique represented path, or multiple represented derivational paths.

The final case is the one for which scalar generation depth becomes ambiguous.

A.5. Generation Depth Is a Path Functional

For a directed path

$$\pi = (v_0 \rightarrow v_1 \rightarrow \dots \rightarrow v_n),$$

define its unweighted generation depth by

$$d(\pi) = n.$$

If $\Pi_{\mathcal{G}}(O, x)$ contains more than one path, then there is no unique value

$$d(O, x)$$

without an additional convention.

One may define

reconstructed spans encountered: 2

LuaLaTeX

$$d_{\min}(O, x) = \min_{\pi \in \Pi_G(O, x)} d(\pi),$$

or, when finite,

$$d_{\max}(O, x) = \max_{\pi \in \Pi_G(O, x)} d(\pi).$$

One may instead privilege a historically realized path

$$\pi_{\text{real}}$$

and define

$$d_{\text{real}}(O, x) = d(\pi_{\text{real}}).$$

These quantities answer different questions.

Shortest-path depth measures minimal represented derivational separation.

Realized-path depth measures the length of a selected history.

Neither encodes transformation type.

For that purpose, let

$$\tau(\pi) = (\tau(e_1), \tau(e_2), \dots, \tau(e_n))$$

denote the ordered transformation word associated with the path.

Thus two paths may satisfy

$$d(\pi_1) = d(\pi_2)$$

while

$$\tau(\pi_1) \neq \tau(\pi_2).$$

This is the formal reason the notation

$$[3]$$

may need to be refined to

$$[3 : R \circ C \circ R].$$

A.6. Weighted Derivational Distance

Equal treatment of every transformation is rarely justified.

Let

$$w : \mathcal{T} \rightarrow \mathbb{R}_{\geq 0}$$

assign a nonnegative provenance cost to each transformation type.

For a path

$$\pi = (e_1, \dots, e_n),$$

define

$$D_w(\pi) = \sum_{i=1}^n w(\tau(e_i)).$$

A verbatim transfer might receive a small cost, a lossy compression a larger cost, and an unconstrained reconstruction a still larger cost.

The mathematical construction does not determine those values.

They are task-relative.

More generally, provenance cost need not be additive. Let

$$D : \Pi(\mathcal{G}) \rightarrow \mathbb{R}_{\geq 0}$$

be any path functional capable of depending upon ordering and interaction among transformations.

Then

$$D(R \circ C)$$

need not equal

$$D(C \circ R).$$

This is important whenever reconstruction before compression and compression before reconstruction preserve different information.

Remark A.5. The essay's generation notation should therefore not be interpreted as a universal metric. It is a deliberately crude coordinate that becomes useful only after the relevant transformation vocabulary and inferential task have been specified.

A.7. Convergence

Let distinct paths

$$\pi_1, \pi_2 \in \Pi_{\mathcal{G}}(O, x)$$

terminate at the same vertex x .

If only x is retained, the map

$$\pi \mapsto \text{End}(\pi)$$

identifies π_1 and π_2 .

The endpoint is therefore a quotient of the path information.

This observation generalizes immediately to any representation

$$r : \Pi(\mathcal{G}) \rightarrow Z.$$

Whenever

$$r(\pi_1) = r(\pi_2)$$

for provenance-distinct paths, the representation loses the distinction between them.

Proposition A.6 (Convergent provenance loss). *Let δ be a provenance observable with*

$$\delta(\pi_1) \neq \delta(\pi_2).$$

If a representation r satisfies

$$r(\pi_1) = r(\pi_2),$$

then no function of $r(\pi)$ alone can recover δ correctly on both paths.

Proof. If such a function h existed, then

$$h(r(\pi_1)) = \delta(\pi_1)$$

and

$$h(r(\pi_2)) = \delta(\pi_2).$$

But

$$r(\pi_1) = r(\pi_2),$$

so the two left-hand sides are equal while the two right-hand sides are not, a contradiction. $\square$

This is the information-theoretic core of the Originist position in its simplest deterministic form.

A.8. Branching Prevents Identity from Selecting a Unique Future

Suppose an origin O has two admissible descendants

$$OA$$

and

$$OB.$$

If descent from O were sufficient to establish numerical identity with O , then both A and B would inherit that identity.

By transitivity of identity,

$$A = O \quad \text{and} \quad B = O$$

would imply

$$A = B.$$

But branching permits

$$A \neq B.$$

Thus genealogical descent cannot by itself be numerical identity.

Proposition A.7 (Branching obstruction). *No transitive numerical identity relation can identify an origin with every member of a genuinely branching set of distinct descendants.*

Proof. Let $A \neq B$ be descendants of O . Assume

$$A = O \quad \text{and} \quad B = O.$$

By symmetry,

$$O = B,$$

and by transitivity,

$$A = B,$$

contradicting the assumption that the descendants are distinct. □

The result is elementary but useful for consciousness-transfer and copying problems.

A continuation relation may branch.

Numerical identity cannot branch in the same way without contradiction.

A.9. Recurrence as Return to a Class

Let

$$q_C : X \rightarrow X/\sim_C$$

be the quotient induced by a constraint-relative recurrence relation.

A history

$$\gamma = (x_0 \rightarrow \cdots \rightarrow x_n)$$

is recurrent relative to C when

$$q_C(x_n) = q_C(x_0).$$

Equivalently,

$$x_n \sim_C x_0.$$

This does not require

$$x_n = x_0.$$

Nor does it imply equality of histories.

Indeed, if $n > 0$,

$$\gamma$$

contains an ordered sequence of transformations absent from the zero-length history at x_0 .

Recurrence therefore closes a loop only after quotienting by $\sim_C$.

At the history level, the path remains extended.

This supplies a concise formal interpretation of the Le Guinian return:

$$q_C(O') = q_C(O),$$

while

$$O' \neq O$$

and

$$\text{Hist}(O') \neq \text{Hist}(O).$$

A.10. Continuous Generalization

When X carries a topology, a continuous trajectory may be represented as

$$\gamma : [0, 1] \rightarrow X.$$

For fixed endpoints $x, y \in X$, define

$$\Gamma(x, y) = \{\gamma : [0, 1] \rightarrow X : \gamma(0) = x, \gamma(1) = y\}.$$

Two trajectories may share endpoints while differing as maps:

$$\gamma_1(0) = \gamma_2(0) = x,$$

$$\gamma_1(1) = \gamma_2(1) = y,$$

yet

$$\gamma_1 \neq \gamma_2.$$

If a homotopy relation is imposed, one may further quotient

$$\Gamma(x, y) / \simeq.$$

The Originist question immediately reappears:

Which distinctions are erased by the homotopy quotient?

For some tasks, homotopic paths should indeed be identified.

For others, the difference between them may encode the very history under investigation.

Thus topology does not solve the provenance problem.

It provides another family of principled quotients to which the same question must be applied.

A.11. The Formal Core of the Trajectory Thesis

The mathematical content of the trajectory-first claim can now be stated without literary language.

Let

$$\text{End} : \Gamma(X) \rightarrow X$$

be non-injective.

Then there exist histories

$$\gamma_A \neq \gamma_B$$

with

$$\text{End}(\gamma_A) = \text{End}(\gamma_B).$$

Any property

$$P : \Gamma(X) \rightarrow Z$$

that is not constant on endpoint fibres cannot be represented exactly as a function of endpoints alone.

Theorem A.8 (Trajectory necessity criterion). *A history-dependent property*

$$P : \Gamma(X) \rightarrow Z$$

admits an exact state-level representation

$$\tilde{P} : X \rightarrow Z$$

satisfying

$$P = \tilde{P} \circ \text{End}$$

if and only if P is constant on every endpoint fibre.

Proof. This is theorem A.4 applied to the equivalence relation

$$\gamma_1 \sim_{\text{End}} \gamma_2 \iff \text{End}(\gamma_1) = \text{End}(\gamma_2).$$

The quotient by $\sim_{\text{End}}$ is represented by endpoint states. Therefore P factors through End exactly when it is constant on the fibres of End . $\square$

This theorem states the central issue in its most economical form.

If the property of interest varies among histories that end in the same state, then the property is not a property of the endpoint alone.

Provenance is one such property.

Under the argument developed in this essay, some forms of continuation are another.

The mathematical statement does not decide which historical properties matter.

That is the work of admissibility.

MOVEMENT II. QUOTIENTS AND THE ORIGINIST LOSS OPERATOR

How can one say precisely what a representation forgets without pretending that every kind of forgetting has the same magnitude?

The phrase “information loss” is dangerously broad. A representation can forget punctuation, ordering, authorship, transformation history, confidence, material composition, or an entire branch of descent. These are not interchangeable losses, and there is no reason to assume that they admit a common numerical scale.

The Originist loss operator introduced in the body of the essay is therefore not initially a number. Its most primitive form records whether a distinction required by a later inference survives a representation at all. Only after that logical question has been answered does it make sense to introduce cardinalities, probabilities, entropies, or task-relative costs.

This appendix develops that hierarchy. It begins with a binary notion of recoverability, extends it to families of provenance observables, and then shows how probabilistic loss can be defined when a distribution over histories is available. The final sections return to compression and reconstruction.

The important result is not that lossy compression is bad. Almost every useful abstraction is lossy. The result is that reconstruction of an endpoint cannot, by itself, make a provenance-destroying quotient provenance-neutral.

B.1. Representations and Their Fibres

Let Γ be a space of histories and let

$$q : \Gamma \rightarrow Q$$

be any representation map.

The codomain Q may contain compressed records, canonical forms, endpoint states, equivalence classes, summaries, embeddings, or any other objects used in place of the full histories.

For $z \in Q$, define the fibre

$$q^{-1}(z) = \{\gamma \in \Gamma : q(\gamma) = z\}.$$

The fibre contains every history rendered indistinguishable by the representation q .

A representation is injective precisely when every fibre contains at most one history.

In most cases of interest here, q is deliberately non-injective.

The question is therefore not whether distinctions have been erased.

The question is which ones.

B.2. Provenance Observables

Let

$$\delta : \Gamma \rightarrow D$$

be a function encoding some provenance-relevant distinction.

Examples include the original source,

$$\delta_{\text{src}}(\gamma),$$

generation depth,

$$\delta_{\text{depth}}(\gamma),$$

the ordered transformation word,

$$\delta_{\text{word}}(\gamma),$$

the presence of a lossy operation,

$$\delta_{\text{loss}}(\gamma) \in \{0, 1\},$$

or membership in an admissible trajectory class,

$$\delta_A(\gamma).$$

No assumption is made that all provenance questions can be reduced to one observable.

Indeed, the argument of the essay suggests the opposite.

Let

$$\Delta = \{\delta_\alpha\}_{\alpha \in A}$$

be a family of provenance observables selected for a task.

A representation may preserve some members of Δ and destroy others.

B.3. Logical Originist Loss

The weakest useful notion of loss asks only whether a provenance observable survives the representation.

Definition B.1 (Logical Originist loss). For a representation

$$q : \Gamma \rightarrow Q$$

and provenance observable

$$\delta : \Gamma \rightarrow D,$$

define

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = \begin{cases} 0, & \text{if } \delta \text{ factors through } q, \\ 1, & \text{otherwise.} \end{cases}$$

Thus

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = 0$$

exactly when there exists a function

$$\bar{\delta} : Q \rightarrow D$$

such that

$$\delta = \bar{\delta} \circ q.$$

By theorem A.4, this occurs exactly when δ is constant on every fibre of q .

Hence

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = 1$$

if and only if there exist histories γ_1, γ_2 satisfying

$$q(\gamma_1) = q(\gamma_2)$$

while

$$\delta(\gamma_1) \neq \delta(\gamma_2).$$

This is the formal version of an Originist wound.

B.4. Loss Is Relative to a Future Question

A representation can be perfectly safe for one task and unusable for another.

Let

$$F : \Gamma \rightarrow Y$$

represent a future inferential task.

If F factors through q , then the representation retains everything required to compute F exactly:

$$F = \bar{F} \circ q.$$

If it does not, then some histories requiring different outputs have become indistinguishable after representation.

Definition B.2 (Task sufficiency). A representation $q : \Gamma \rightarrow Q$ is sufficient for the task F when there exists

$$\bar{F} : Q \rightarrow Y$$

such that

$$F = \bar{F} \circ q.$$

The Originist objection can now be written in one line:

$$q \text{ is unsafe for } F \iff F \text{ does not factor through } q.$$

This is stronger than the vague instruction to preserve provenance.

Only provenance distinctions on which F depends need be retained.

The framework therefore does not imply archival maximalism.

B.5. Loss Profiles

Given a family

$$\Delta = \{\delta_\alpha\}_{\alpha \in A},$$

define the logical loss profile

$$\mathbf{L}_q = \left(\mathcal{L}_{\text{orig}}^{(0)}(q; \delta_\alpha) \right)_{\alpha \in A}.$$

This vector is more informative than a single scalar whenever the provenance dimensions are heterogeneous.

For example, a representation might preserve

$$\delta_{\text{src}}$$

and

reconstructed spans encountered: 2

LuaLaTeX

$$\delta_{\text{depth}},$$

while destroying

$$\delta_{\text{word}}.$$

Its loss profile could then take the schematic form

$$\mathbf{L}_q = (0, 0, 1).$$

No meaningful conclusion follows from replacing this vector with the number 1 unless weights and a task have first been specified.

The refusal to scalarize prematurely is deliberate.

Different wounds matter to different future operations.

B.6. Task-Weighted Loss

Suppose A is finite and let

$$w_\alpha \geq 0$$

represent the importance of preserving δ_α for a specified task.

Define

$$\mathcal{L}_{\text{orig}}^{(w)}(q; \Delta) = \sum_{\alpha \in A} w_\alpha \mathcal{L}_{\text{orig}}^{(0)}(q; \delta_\alpha).$$

This scalar has no task-independent interpretation.

Changing the weights changes what the representation is being evaluated for.

If exact wording is irrelevant, one may set

$$w_{\text{word}} = 0.$$

If authorship is legally decisive, one may assign

$$w_{\text{src}}$$

a dominant value.

The weights therefore encode a normative or operational choice.

They are not discovered merely by inspecting q .

B.7. Further Forgetting Cannot Restore Logical Recoverability

Suppose

$$\Gamma \xrightarrow{q_1} Q_1 \xrightarrow{q_2} Q_2$$

are successive representations, and define

$$q = q_2 \circ q_1.$$

If a provenance distinction is already unrecoverable after q_1 , applying q_2 cannot make it exactly recoverable from the representation alone.

Theorem B.3 (Monotonicity of logical loss). *For every provenance observable δ ,*

$$\mathcal{L}_{\text{orig}}^{(0)}(q_1; \delta) \leq \mathcal{L}_{\text{orig}}^{(0)}(q_2 \circ q_1; \delta).$$

Proof. If

$$\mathcal{L}_{\text{orig}}^{(0)}(q_1; \delta) = 0,$$

the inequality is automatic because the left side is zero.

Suppose instead

$$\mathcal{L}_{\text{orig}}^{(0)}(q_1; \delta) = 1.$$

Then there exist $\gamma_1, \gamma_2 \in \Gamma$ such that

$$q_1(\gamma_1) = q_1(\gamma_2)$$

while

$$\delta(\gamma_1) \neq \delta(\gamma_2).$$

Applying q_2 gives

$$q_2(q_1(\gamma_1)) = q_2(q_1(\gamma_2)).$$

Thus the composite also identifies two histories on which δ differs. Therefore

$$\mathcal{L}_{\text{orig}}^{(0)}(q_2 \circ q_1; \delta) = 1.$$

□

The theorem concerns information available from the representation alone.

External evidence can, of course, restore knowledge.

That restoration is the next problem.

B.8. Reconstruction Is Not Inversion

Let

$$q : \Gamma \rightarrow Q$$

be non-injective.

Suppose additional evidence belongs to a space E , and let

$$R : Q \times E \rightarrow \hat{\Gamma}$$

be a reconstruction procedure.

For some realized history γ , it may happen that

$$R(q(\gamma), e) = \gamma.$$

This does not imply that q was lossless.

The evidence e is doing inferential work.

To make this explicit, define the augmented representation

$$q_e : \Gamma \rightarrow Q \times E$$

only when the evidence itself is generated as part of the represented information.

If e arrives independently, then reconstruction uses information outside $q(\gamma)$.

Proposition B.4 (External repair does not erase internal loss). *Suppose*

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = 1.$$

The existence of an external evidence variable e and reconstruction procedure R that correctly recovers $\delta(\gamma)$ for a particular history does not imply

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = 0.$$

Proof. Logical Originist loss is defined by whether δ factors through q . The existence of a procedure depending upon both $q(\gamma)$ and an additional variable e establishes, at most, factorization through an augmented representation. It does not establish factorization through q alone. $\square$

This is the exact distinction between preservation and successful reconstruction.

B.9. Probabilistic Reconstruction

When exact recovery is impossible, an Originist may maintain a distribution over candidate histories.

Let Γ be finite or countable for simplicity, with prior

$$P(\gamma).$$

After observing

$$z = q(\gamma),$$

Bayes' rule gives

$$P(\gamma | z) = \frac{P(z | \gamma)P(\gamma)}{P(z)}.$$

For deterministic q ,

$$P(z | \gamma) = \begin{cases} 1, & q(\gamma) = z, \\ 0, & \text{otherwise.} \end{cases}$$

Hence the posterior is supported on the fibre

$$q^{-1}(z).$$

If that fibre contains multiple histories with nonzero posterior mass, the representation leaves provenance uncertainty.

A reconstruction algorithm may select

$$\hat{\gamma}_{\text{MAP}} = \arg \max_{\gamma \in q^{-1}(z)} P(\gamma | z).$$

But

$$\hat{\gamma}_{\text{MAP}}$$

is an estimate.

It is not a recovered historical fact merely because it is probable.

This distinction is particularly important for generative reconstruction, where plausible completions can be much easier to produce than derivationally warranted ones.

B.10. An Information-Theoretic Originist Loss

When a probability distribution is available, provenance uncertainty can be quantified.

Let the random variable G range over histories and let

$$Z = q(G)$$

be the represented state.

The conditional entropy

$$H(G | Z)$$

measures residual uncertainty about history after observing the representation.

If

$$H(G | Z) = 0,$$

then G is determined almost surely by Z under the chosen distribution.

If

$$H(G | Z) > 0,$$

some historical uncertainty remains.

For a particular provenance observable

$$D = \delta(G),$$

the more task-specific quantity is

$$H(D | Z).$$

This suggests the probabilistic Originist loss

$$\mathcal{L}_{\text{orig}}^{(H)}(q; \delta) = H(\delta(G) | q(G)).$$

This quantity depends upon the distribution over histories.

It therefore differs fundamentally from the logical loss

$$\mathcal{L}_{\text{orig}}^{(0)}.$$

Logical loss asks whether exact recovery is possible in principle over the specified domain.

Entropy-based loss asks how much uncertainty remains on average under a specified probability model.

B.11. Rare Ambiguity

The distinction between logical and probabilistic loss is not cosmetic.

Suppose two histories γ_1 and γ_2 satisfy

$$q(\gamma_1) = q(\gamma_2),$$

and

$$\delta(\gamma_1) \neq \delta(\gamma_2).$$

Then

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = 1.$$

But if

$$P(\gamma_2)$$

is extremely small, then

$$H(\delta(G) \mid q(G))$$

may also be extremely small.

The representation is almost always sufficient probabilistically while still failing exact recoverability.

This is precisely the sort of case in which a system optimized for average performance may appear reliable until a low-probability provenance dispute becomes the only case that matters.

Archival authentication, legal evidence, scientific priority, and safety auditing can all have this structure.

B.12. A Provenance Form of Data Processing

Suppose

$$G \rightarrow Z_1 \rightarrow Z_2$$

forms a Markov chain in which

$$Z_1 = q_1(G)$$

and

$$Z_2 = q_2(Z_1).$$

For any provenance variable

$$D = \delta(G),$$

the data-processing inequality gives

$$I(D; Z_2) \leq I(D; Z_1),$$

where I denotes mutual information.

Equivalently,

$$H(D \mid Z_2) \geq H(D \mid Z_1)$$

when the relevant entropies are finite.

Further processing cannot increase information about provenance unless new information enters the system.

This is the probabilistic counterpart of theorem B.3.

A reconstruction model can appear to increase information because it contains priors learned elsewhere.

That information is genuinely new relative to the compressed artifact.

It should not be misdescribed as information that the artifact itself preserved.

B.13. Repeated Compression–Repair Cycles

Consider a sequence

$$x_0 \xrightarrow{C_1} z_1 \xrightarrow{R_1} x_1 \xrightarrow{C_2} z_2 \xrightarrow{R_2} x_2 \rightarrow \dots$$

Let

$$\gamma_n$$

denote the history terminating at x_n .

Suppose the invariant loss function used by the repair system satisfies

$$\mathcal{L}_I(x_0, x_n) \approx 0.$$

This may be an excellent result.

It means the selected invariants have been successfully maintained.

It does not imply

$$\text{Prov}(x_0) = \text{Prov}(x_n).$$

Nor does it imply

$$\mathcal{L}_{\text{orig}}(C_i; \delta) = 0$$

for every provenance observable δ .

The repair system and the Originist answer different questions.

The repair system asks whether a selected content property has survived or been reconstructed.

The Originist asks what derivational claims remain warranted about the result.

B.14. Generation Count and Transformation Words

Let

$$\tau(\gamma) = T_n \circ \dots \circ T_1$$

denote the ordered transformation word associated with a history.

Define generation count

$$g(\gamma) = n.$$

Then g is a projection from transformation words to their lengths.

Consequently,

$$g(\gamma_1) = g(\gamma_2)$$

does not imply

$$\tau(\gamma_1) = \tau(\gamma_2).$$

Generation count is therefore itself a quotient.

Let

$$q_g : \Gamma \rightarrow \mathbb{N}$$

be given by

$$q_g(\gamma) = g(\gamma).$$

If a future task depends on transformation order, then

$$\mathcal{L}_{\text{orig}}^{(0)}(q_g; \delta_{\text{word}}) = 1.$$

This is why the provenance notation had to expand from

$$[3]$$

to

$$[3 : R \circ C \circ R].$$

The richer notation is not necessarily final.

It merely preserves another distinction.

B.15. Confidence Is Not Generation

The full provenance notation introduced in the essay permits expressions such as

$$\varphi^{[3:R \circ C \circ R; J^+; p=.71]}.$$

The final coordinate must be interpreted carefully.

A confidence value

$$p = .71$$

is not a generation count.

It is not a truth value.

It is not an invariant score.

It is not a measure of semantic similarity.

It represents an evidential assessment under some specified model.

Two claims may therefore satisfy

$$\text{Truth}(\varphi_1) = \text{Truth}(\varphi_2)$$

and

$$g(\varphi_1) = g(\varphi_2)$$

while carrying different confidence values because the evidence for their respective derivational histories differs.

Conversely, two provenance hypotheses may have equal posterior probability while describing entirely different transformation chains.

The coordinates must remain separate unless a model explicitly relates them.

B.16. Why $[\omega?]$ Is Not Infinity

The notation

$$[\omega?]$$

used for the wound in Movement IV is intentionally suggestive but should not be read as a literal transfinite generation count.

Its meaning is epistemic:

derivational depth is not presently recoverable.

Thus

$$[\omega?] \neq [\infty].$$

Nor does it mean that the derivation is known to be arbitrarily long.

It marks refusal to invent a finite depth when the available evidence does not warrant one.

Formally, if

$$g : \Gamma \rightarrow \mathbb{N}$$

is generation depth and the evidence E leaves multiple values possible,

$$|\{g(\gamma) : \gamma \in \Gamma_E\}| > 1,$$

then assigning a unique $n \in \mathbb{N}$ would overstate what is known.

The wound tag therefore records underdetermination rather than magnitude.

B.17. The Non-Neutrality of Perfect Repair

We can now state the strongest result needed for the compression argument.

Let

$$q : \Gamma \rightarrow Q$$

be a provenance-losing representation and let

$$R : Q \rightarrow X$$

be any deterministic repair operation producing endpoint states.

Suppose there exist histories

$$\gamma_1, \gamma_2$$

such that

$$q(\gamma_1) = q(\gamma_2)$$

but

$$\delta(\gamma_1) \neq \delta(\gamma_2).$$

Then

$$R(q(\gamma_1)) = R(q(\gamma_2)).$$

No quality of endpoint repair changes the fact that the two histories were identified before reconstruction.

Theorem B.5 (Perfect repair cannot neutralize provenance loss). *If*

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = 1,$$

then for every deterministic repair map

$$R : Q \rightarrow X,$$

the composite

$$R \circ q$$

also has positive logical Originist loss with respect to δ :

$$\mathcal{L}_{\text{orig}}^{(0)}(R \circ q; \delta) = 1.$$

Proof. Since

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = 1,$$

there exist γ_1, γ_2 such that

$$q(\gamma_1) = q(\gamma_2)$$

and

$$\delta(\gamma_1) \neq \delta(\gamma_2).$$

Applying R to the equal representations yields

$$R(q(\gamma_1)) = R(q(\gamma_2)).$$

Thus $R \circ q$ also identifies histories distinguished by δ . Therefore δ does not factor through $R \circ q$, and

$$\mathcal{L}_{\text{orig}}^{(0)}(R \circ q; \delta) = 1.$$

□

The theorem does not say that repair is useless.

It says something narrower.

Repair can restore an endpoint property.

It cannot make an earlier non-injective provenance representation become injective after the fact.

B.18. How Provenance Can Be Recovered

The preceding theorem might appear stronger than ordinary archival practice allows. Lost provenance is sometimes recovered. The apparent contradiction disappears once side information is represented explicitly.

Suppose

$$q(\gamma_1) = q(\gamma_2),$$

but an independent variable E satisfies

$$E(\gamma_1) \neq E(\gamma_2).$$

The augmented representation

$$q^+(\gamma) = (q(\gamma), E(\gamma))$$

may now distinguish the histories.

It is possible that

$$\mathcal{L}_{\text{orig}}^{(0)}(q^+; \delta) = 0$$

even though

$$\mathcal{L}_{\text{orig}}^{(0)}(q; \delta) = 1.$$

This is not reversal of loss inside q .

It is recovery through another channel.

An archive, witness, checksum, external manuscript, independent sensor, or second model may supply exactly such a channel.

The Archivist and Originist roles therefore become complementary.

The Archivist preserves side information before it is needed.

The Originist determines when later claims depend upon it.

B.19. Minimal Sufficient Provenance

The theory should not terminate in the instruction to store everything.

Let

$$F : \Gamma \rightarrow Y$$

be the future task of interest.

We seek a representation

$$q_F : \Gamma \rightarrow Q_F$$

such that

$$F = \bar{F} \circ q_F$$

while q_F discards distinctions irrelevant to F .

This resembles the search for a sufficient statistic.

Two histories may be identified whenever they induce the same task-relevant output:

$$\gamma_1 \sim_F \gamma_2 \iff F(\gamma_1) = F(\gamma_2).$$

The corresponding quotient

$$\Gamma / \sim_F$$

is maximally compressed relative to the single task F .

But future tasks are rarely known completely in advance.

This is where archival judgment enters.

The more uncertain the future task family, the more dangerous aggressive quotienting becomes.

B.20. Compression Under Provenance Constraints

The preceding observation suggests a rate–distortion-like formulation.

Let

$$R(q)$$

denote the storage or description cost of representation q , and let

$$D_{\text{state}}(q)$$

measure distortion of task-relevant endpoint properties.

Add an Originist term

$$D_{\text{prov}}(q) = \mathcal{L}_{\text{orig}}^{(w)}(q; \Delta).$$

One may then consider an objective of the form

$$\mathcal{J}(q) = R(q) + \lambda D_{\text{state}}(q) + \mu D_{\text{prov}}(q),$$

where

$$\lambda, \mu \geq 0.$$

The point is not the particular linear form.

The point is that provenance loss becomes an explicit optimization variable rather than an accidental side effect.

Setting

$$\mu = 0$$

recovers a system indifferent to derivational distinctions except insofar as they affect endpoint distortion.

A positive μ makes some histories expensive to collapse even when their current states are equivalent.

This is the computational expression of the essay's central objection.

B.21. There Is No Universal Provenance Metric

Nothing in the construction licenses a universal scalar

$$\mathcal{L}_{\text{orig}}(q)$$

independent of a provenance vocabulary, task, probability model, or admissibility criterion.

The same quotient may be harmless in one context and catastrophic in another.

A normalization that removes whitespace may be irrelevant to semantic retrieval but unacceptable in forensic authorship analysis.

A paraphrase may preserve a theorem while destroying evidence about its original formulation.

A reconstructed civilization may preserve institutions while losing environmental relations required for world-continuation.

The correct expression is therefore normally

$$\mathcal{L}_{\text{orig}}(q; \delta),$$

$$\mathcal{L}_{\text{orig}}(q; \Delta),$$

or

$$\mathcal{L}_{\text{orig}}(q; F).$$

The second argument is not optional decoration.

It states what one is refusing to forget.

B.22. The Objection as a Commutative Failure

The entire appendix can be summarized through a diagram.

Suppose we would like a provenance observable

$$\delta : \Gamma \rightarrow D$$

to remain computable after representation by q .

We seek a map

$$\bar{\delta} : Q \rightarrow D$$

making

$$\begin{array}{ccc} \Gamma & \xrightarrow{q} & Q \\ & \searrow \delta & \downarrow \bar{\delta} \\ & & D \end{array}$$

commute.

If such a map exists, the provenance distinction survives the quotient.

If no such map exists, the dashed arrow cannot be filled.

That missing arrow is the wound.

ORIGINIST LOSS

A representation loses a provenance distinction exactly when the desired historical observable no longer factors through the representation.

This formulation is intentionally austere.

It covers perfect forgery, independent rediscovery, lossy compression, generative reconstruction, branching descent, convergent histories, archival restoration, and the document's own uncertain citation without requiring those cases to be mathematically identical.

They share only the relevant structural failure:

$$\text{different histories} \mapsto \text{one representation.}$$

Once that identification has occurred, no operation internal to the representation can discover which distinction was erased.

Something else must have survived elsewhere.

MOVEMENT III. ADMISSIBILITY, GLUING, AND OBSTRUCTION

Why can every local step look acceptable while the resulting history still fails to constitute one coherent continuation?

Causal descent is too permissive. A corrupted file descends causally from the file it corrupts. A malignant growth descends causally from healthy tissue. A ruin descends causally from a city. None of these observations is sufficient to establish the stronger relation that the essay has called continuation.

Admissibility supplies the missing restriction, but it creates a second problem. A long history is rarely evaluated all at once. Different portions of it may be inspected under different local constraints, by different observers, or with access to different records. Every local segment can appear acceptable while the collection fails to assemble into a globally coherent history.

This appendix develops that possibility using a deliberately restrained gluing formalism. The purpose is not to claim that every provenance problem is literally a sheaf-cohomology problem. The purpose is to isolate a recurring structural pattern: local realizations exist, neighboring realizations agree partially, yet no single global realization satisfies all of the local data at once.

That failure is especially important for TARTAN-like reasoning, Chain of Memory, archival reconstruction, and world-continuation. It also explains why checking transformations one at a time cannot in general certify an entire trajectory.

C.1. Two Kinds of Admissibility

Let X be a state space and let

$$\Gamma(X)$$

denote a collection of histories over X .

A state-level admissibility predicate is a map

$$A_X : X \rightarrow \{0, 1\}.$$

The admissible state set is

$$A_X = A_X^{-1}(1).$$

A trajectory-level admissibility predicate is instead

$$A_\Gamma : \Gamma(X) \rightarrow \{0, 1\},$$

with

$$A_\Gamma = A_\Gamma^{-1}(1).$$

There is no general reason for the latter to be determined pointwise by the former.

Indeed, one may have a history

$$\gamma = (x_0 \rightarrow x_1 \rightarrow \dots \rightarrow x_n)$$

such that

$$A_X(x_i) = 1 \quad \text{for every } i,$$

while

$$A_\Gamma(\gamma) = 0.$$

The simplest provenance example is a perfect forgery.

Every state-level property relevant to the artifact may be acceptable.

The history is nevertheless inadmissible for a task requiring authentic descent.

Proposition C.1 (Pointwise admissibility is insufficient). *Without an additional locality assumption on A_Γ ,*

$$(A_X(x_i) = 1 \text{ for all } i) \not\Rightarrow A_\Gamma(\gamma) = 1.$$

The proposition is almost definitional, but its consequence is substantial.

A trajectory constraint cannot in general be replaced by repeated endpoint checks.

C.2. Admissible Transitions

Between state and trajectory admissibility lies a third possibility.

Let

$$A_E : X \times \mathcal{T} \times X \rightarrow \{0, 1\}$$

judge individual transformations.

For

$$x \xrightarrow{T} y,$$

write

$$x \xrightarrow[A]{T} y$$

when

$$A_E(x, T, y) = 1.$$

A history is edgewise admissible when

$$A_E(x_{i-1}, T_i, x_i) = 1$$

for every i .

Again, edgewise admissibility need not imply trajectory admissibility.

A global constraint may depend upon accumulated drift, ordering, recurrence, resource consumption, provenance depth, or a relation between distant points of the path.

For example, suppose every transformation is allowed to change a scalar quantity f by at most ε :

$$|f(x_i) - f(x_{i-1})| \leq \varepsilon.$$

Every edge may satisfy this bound while after n steps

$$|f(x_n) - f(x_0)| \gg \varepsilon.$$

Local acceptability therefore does not imply global preservation.

C.3. The Simplest Global Obstruction: Drift

Let

$$d : X \times X \rightarrow \mathbb{R}_{\geq 0}$$

be a task-relative discrepancy function.

Suppose every edge of a trajectory satisfies

$$d(x_{i-1}, x_i) \leq \varepsilon.$$

If d obeys the triangle inequality, then only

$$d(x_0, x_n) \leq \sum_{i=1}^n d(x_{i-1}, x_i) \leq n\varepsilon$$

follows.

Thus an arbitrarily long trajectory can move arbitrarily far from its origin while every local step remains small.

This is the elementary form of a problem that later appears as gluing failure.

Local compatibility constrains neighboring pieces.

It does not automatically establish global identity.

Pathology C.2 (Locally small, globally distant). A trajectory may satisfy every local distortion bound while violating a global continuation constraint relative to its origin.

The relevance to repeated regeneration is immediate.

A system can make only tiny changes per generation while eventually reaching a state that no longer satisfies the invariant class that motivated the process.

C.4. Histories Seen Through Windows

Let a history be parameterized over an interval

$$I = [0, 1].$$

Choose an open cover

$$\mathcal{U} = \{U_i\}_{i \in I_0}$$

of the parameter domain.

Each U_i represents a local window into the history.

Suppose an observer reconstructs a local realization

$$s_i \in \mathcal{F}(U_i),$$

where $\mathcal{F}(U_i)$ denotes the admissible descriptions available over that window.

Whenever

$$U_i \cap U_j \neq \emptyset,$$

the two local realizations can be restricted to the overlap:

$$s_i|_{U_i \cap U_j}, \quad s_j|_{U_i \cap U_j}.$$

The strongest local compatibility condition is

$$s_i|_{U_i \cap U_j} = s_j|_{U_i \cap U_j}.$$

If all compatible local sections assemble uniquely into a global section

$$s \in \mathcal{F}(I),$$

then the local data glue.

This is the ideal case.

C.5. Compatibility Up to Transformation

Provenance problems often do not provide literal equality on overlaps.

Two reconstructions may differ by a known translation, coordinate change, normalization, renaming, or other admissible transformation.

Let G be a group, or more generally a groupoid of admissible re-identifications.

On an overlap

$$U_i \cap U_j,$$

suppose

$$s_i = g_{ij} \cdot s_j$$

for some transition element

$$g_{ij} \in G.$$

Consistency requires

$$g_{ii} = e$$

and

$$g_{ji} = g_{ij}^{-1}.$$

On triple overlaps, a further condition appears:

$$g_{ij}g_{jk}g_{ki} = e.$$

When this condition fails, pairwise compatibility does not extend to coherent three-way compatibility.

This is the first genuinely nonlocal obstruction.

C.6. Cocycles

Assume for simplicity that the transition structure is represented by an abelian group G .

A collection

$$\{g_{ij}\}$$

on pairwise overlaps satisfying

$$g_{ij} + g_{jk} + g_{ki} = 0$$

on every triple overlap is a Čech 1-cocycle.

Using multiplicative notation, the same condition is

$$g_{ij}g_{jk}g_{ki} = e.$$

A change of local representatives by elements

$$h_i \in G$$

modifies transition data according to

$$g_{ij} \mapsto h_i^{-1}g_{ij}h_j.$$

In the abelian case,

$$g_{ij} \mapsto g_{ij} + h_j - h_i.$$

If the transition data can be eliminated entirely by such local redefinitions, the cocycle is a coboundary.

Its cohomology class vanishes:

$$[g] = 0 \in \check{H}^1(\mathcal{U}, G).$$

If

$$[g] \neq 0,$$

the local pieces cannot be globally trivialized by the permitted local re-identifications.

C.7. What a Nonzero Class Means Here

The formal analogy to provenance should be used carefully.

The statement

$$[g] \neq 0$$

does not mean simply that the local data are false.

Each local realization may be individually admissible.

Each pairwise relation may also be legitimate.

The obstruction says that no single choice of representatives makes all of those local relations simultaneously disappear.

In the present framework, that means there is no globally coherent identification of all local realizations under the selected transition structure.

This is stronger than local disagreement.

It is an obstruction to global continuation.

Definition C.3 (Gluing obstruction). Given locally admissible realizations $\{s_i\}$ and transition data $\{g_{ij}\}$, a *gluing obstruction* is a nontrivial equivalence class of transition data preventing the local realizations from being represented as restrictions of one globally coherent realization under the permitted re-identifications.

The definition is deliberately broader than the abelian Čech model.

The latter is one tractable realization of the idea.

C.8. A Provenance Example

Suppose three archival fragments A , B , and C overlap pairwise.

Fragment A can be reconciled with B by a transformation

$$g_{AB}.$$

Fragment B can be reconciled with C by

$$g_{BC}.$$

Fragment C can be reconciled with A by

$$g_{CA}.$$

Pairwise reconciliation therefore succeeds.

But if

$$g_{AB}g_{BC}g_{CA} \neq e,$$

the three reconciliations cannot all describe one globally consistent derivation under the chosen transformation model.

One of several things may be true.

The fragments may derive from different branches.

One transition model may be wrong.

A missing transformation may have occurred.

The assumed common origin may be false.

Or the representation may be too coarse to express the distinction required for gluing.

The obstruction does not decide among these explanations.

It establishes that the current local account is globally insufficient.

C.9. Chain of Memory and Local Consistency

A Chain of Memory system can be modeled as retaining a family of local derivational records

$$s_i \in \mathcal{F}(U_i).$$

If each new context window preserves only compatibility with the immediately preceding window, then the system verifies conditions of the form

$$s_i|_{U_i \cap U_{i+1}} \sim s_{i+1}|_{U_i \cap U_{i+1}}.$$

This is not enough to guarantee global consistency.

Long-range constraints may fail.

The system can therefore exhibit what may be called a CLIO stall: local repair continues to produce acceptable neighboring states, but the global obstruction does not decrease.

Let

$$\Omega_n$$

denote a measure or class of unresolved gluing obstruction after generation n .

A stalled regime has schematically

$$\Omega_{n+1} \nless \Omega_n$$

despite continuing local repair.

In a cohomological realization this may appear as persistent nonvanishing

$$[g_n] \neq 0$$

across successive repair cycles.

The system is locally active but globally stuck.

C.10. Repair Without Resolution

Suppose a repair operation changes local representatives

$$s_i \mapsto s'_i.$$

This induces new transition data

$$g_{ij} \mapsto g'_{ij}.$$

A repair can make some overlaps easier to reconcile while making others harder.

Thus a decrease in a local mismatch functional

$$\mathcal{L}_{\text{local}}$$

does not imply disappearance of the global obstruction.

One may have

$$\mathcal{L}_{\text{local}}^{(n+1)} < \mathcal{L}_{\text{local}}^{(n)}$$

while

$$[g_{n+1}] = [g_n] \neq 0.$$

The representation looks progressively smoother.

The obstruction survives.

This is an important pathology for generative repair.

Optimization of local coherence can conceal persistence of a global incompatibility.

C.11. Loop Closure as a Global Test

Suppose a trajectory returns to a region equivalent to its origin under an invariant relation:

$$x_n \simeq_I x_0.$$

This establishes a form of endpoint recurrence.

It does not guarantee that the intervening history closes consistently.

Let the path traverse local charts

$$U_1, U_2, \dots, U_n$$

with transition maps

$$g_{12}, g_{23}, \dots, g_{n1}.$$

The holonomy around the loop is

$$H(\gamma) = g_{12}g_{23} \cdots g_{n1}.$$

If

$$H(\gamma) = e,$$

the local identifications close trivially under the chosen structure.

If

$$H(\gamma) \neq e,$$

the system returns to an apparently equivalent state while carrying a residual transformation accumulated around the loop.

This gives a more exact version of

$$O \rightsquigarrow X \rightsquigarrow O'.$$

The relation

$$O' \simeq_I O$$

does not imply trivial historical holonomy.

C.12. Return with Holonomy

The metaphorical usefulness of holonomy for The Dispossessed is now clear.

Shevek's return to Anarres is not interesting because the journey forms a geographical loop.

It is interesting because traversal changes the relation between traveler, origin, knowledge, and political possibility [3].

Schematically,

$$O \rightsquigarrow X \rightsquigarrow O'$$

with

$$O' \sim_c O$$

but

$$O' \neq O.$$

If the return carries a residual transformation

$$H(\gamma) \neq e,$$

then recurrence is not restoration.

The loop closes spatially or constraint-relatively while remaining historically nontrivial.

This is precisely the kind of case for which trajectory information survives after endpoint recurrence.

C.13. World-Continuation as a Gluing Problem

The same structure can be lifted from artifacts to worlds.

Suppose a world is locally realized through overlapping domains

$$U_i$$

with local structures

$$W_i.$$

Each W_i may be internally coherent.

Neighboring domains may admit compatible translations.

Yet global worldhood requires more than a collection of locally acceptable pieces.

They must glue into a structure supporting coherent cross-domain relations.

A Macrolife civilization could preserve local organizational patterns across many habitats while the total system no longer admits the global relations that characterized its ancestral world.

Thus

$$\forall i, \quad W_i^{(0)} \sim W_i^{(n)}$$

does not automatically imply

$$W_0 \equiv_{\text{world}} W_n.$$

World-continuation can fail globally while succeeding locally.

This is one reason the No-World problem cannot be reduced to persistence of objects within a presumed container.

C.14. The Admissible Path Space

Return now to the path space

$$\Gamma(X).$$

Let

$$\mathcal{A}_\Gamma \subseteq \Gamma(X)$$

denote the admissible histories.

For endpoints $x, y \in X$, define

$$\Gamma_A(x, y) = \{\gamma \in \mathcal{A}_\Gamma : \text{Orig}(\gamma) = x, \text{End}(\gamma) = y\}.$$

Then continuation from x to y is possible under the selected constraints exactly when

$$\Gamma_A(x, y) \neq \emptyset.$$

This is stronger than causal reachability.

If

$$\Gamma(x, y) \neq \emptyset$$

but

$$\Gamma_A(x, y) = \emptyset,$$

then y is reachable from x but not by any admissible history.

This distinction formalizes the difference between descent and acceptable continuation.

C.15. Continuation Need Not Be Unique

Even when

$$\Gamma_A(x, y) \neq \emptyset,$$

there may be several inequivalent admissible histories.

Suppose

$$\gamma_1, \gamma_2 \in \Gamma_A(x, y)$$

while

$$\gamma_1 \not\sim_A \gamma_2.$$

Then admissibility establishes that both histories are permitted.

It does not establish that they are the same continuation.

This matters especially under branching.

A civilization may possess several admissible descendants.

A theory may have several independently reconstructed formulations.

An archive may support several histories consistent with all surviving evidence.

Admissibility therefore constrains possibility without necessarily selecting uniqueness.

C.16. A Minimal Obstruction Functional

For applications not requiring full cohomological machinery, define a nonnegative functional

$$\mathfrak{D} : \Gamma(X) \rightarrow \mathbb{R}_{\geq 0}$$

such that

$$\mathfrak{D}(\gamma) = 0$$

when all required local compatibility conditions glue globally, and

$$\mathfrak{D}(\gamma) > 0$$

when some unresolved incompatibility remains.

The precise functional is domain-specific.

It may combine invariant mismatch, provenance inconsistency, boundary violation, or failed recurrence.

A repair trajectory

$$\gamma_0, \gamma_1, \gamma_2, \dots$$

can then be evaluated by

$$\mathfrak{D}(\gamma_n).$$

Successful repair ideally produces

$$\mathfrak{D}(\gamma_{n+1}) < \mathfrak{D}(\gamma_n).$$

A stall occurs when local losses decrease while

$$\mathfrak{D}(\gamma_n)$$

fails to approach zero.

This is the operational analogue of persistent nontrivial gluing obstruction.

C.17. TARTAN as Constraint-Preserving Realization

Within the present essay, TARTAN can therefore be read as a framework for distinguishing realization from mere resemblance.

A state x does not count as an acceptable realization merely because it matches selected features.

A realization must inhabit an admissibility structure.

Likewise, a trajectory does not count as continuation merely because every neighboring pair is causally related.

The entire path must remain compatible with the constraints whose preservation defines the relevant form of descent.

This suggests the schematic condition

$$\text{Continuation}_A(x, y) \iff \Gamma_A(x, y) \neq \emptyset.$$

When global compatibility is additionally required, one may strengthen this to

$$\text{Continuation}_{A, \mathfrak{D}}(x, y) \iff \exists \gamma \in \Gamma_A(x, y) \text{ such that } \mathfrak{D}(\gamma) = 0.$$

This is not proposed as a universal definition of identity.

It is a formal model of the narrower claim that continuation is constrained reachability rather than endpoint resemblance.

C.18. Two Different Failures

Originist loss and gluing obstruction should not be conflated.

Originist loss concerns distinctions erased by a representation:

$$\mathcal{L}_{\text{orig}}(q; \delta) > 0.$$

Gluing obstruction concerns local data that fail to assemble globally:

$$\mathfrak{D}(\gamma) > 0$$

or, in the cohomological model,

$$[g] \neq 0.$$

The two can interact.

A representation may erase exactly the distinction required to diagnose a gluing failure.

Conversely, a persistent gluing obstruction may motivate preserving more provenance information.

But neither implies the other in general.

One is a failure of recoverability.

The other is a failure of global compatibility.

Their separation is essential to the larger architecture.

C.19. Continuation as Successful Gluing

The desired situation can be summarized schematically.

Local histories

$$\gamma_i \in \mathcal{F}(U_i)$$

should admit a global history

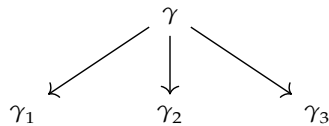
$$\gamma \in \mathcal{F}(U)$$

such that

$$\gamma|_{U_i} \sim \gamma_i$$

for every i .

Diagrammatically,



represents a common global realization whose restrictions recover the local ones up to the permitted equivalence.

When no such γ exists, the local descriptions may remain individually useful.

What fails is their claim to constitute one history.

This distinction will matter directly in Appendix D, where the object to be glued is no longer merely a record or trajectory but a candidate world.

C.20. The Result Needed by the Main Argument

The technical machinery of this appendix can be condensed into one principle.

Theorem C.4 (Admissibility does not localize automatically). *In the absence of a theorem establishing that a global admissibility predicate is determined by local restrictions, verification of every local state, transition, or overlap is insufficient to establish global trajectory admissibility.*

Proof. It suffices to exhibit a class of counterexamples. Let local realizations $\{s_i\}$ be individually admissible and pairwise related by transition data $\{g_{ij}\}$. If the resulting cocycle represents a nontrivial obstruction,

$$[g] \neq 0,$$

then no permitted choice of local representatives produces a single globally compatible realization. Thus every stipulated local test may succeed while the global gluing condition fails. $\square$

The theorem identifies the precise burden of proof hidden by claims of local continuity.

One must either demonstrate a valid local-to-global principle or retain the possibility of obstruction.

LOCAL-TO-GLOBAL WARNING

*Every step may be admissible.
Every overlap may be repairable.
The whole may still fail to constitute one continuation.*

That warning is the mathematical counterpart of the essay's literary triangulation.

Card supplies incomplete local traces of an absent past.

Zebrowski supplies indefinitely extended local transformations toward a future.

Le Guin supplies the loop in which departure and return test whether locally continuous history closes globally.

The next appendix asks what happens when the thing whose coherence must be tested is not an artifact, a person, or a civilization considered in isolation, but a world.

MOVEMENT IV. WORLD-CONTINUATION AND THE NO-WORLD FORMULATION

What could it mean for a world to continue if worldhood is not assumed in advance as a container within which continuing things reside?

Ordinary persistence questions begin too late. They assume a world and then ask whether some object inside it has remained the same. That order is useful for everyday reasoning, but it conceals the harder question raised by the cases considered in this essay. If objects, organisms, archives, institutions, habitats, and civilizations can all be replaced, reconstructed, distributed, or moved across substrates, then the persistence of their surrounding world cannot simply be taken for granted.

The No-World formulation reverses the explanatory order. A world is not first posited as a primitive container. Worldhood is reconstructed from a sufficiently coherent organization of relations, constraints, recurrences, boundaries, and possible continuations. What persists, on this view, need not be a material inventory. But neither is persistence secured merely by reproducing an abstract pattern somewhere else.

This appendix formalizes only the portion of that thesis required by the present essay. It distinguishes object-continuation, civilization-continuation, and world-continuation; defines a world signature as a structured relational object rather than a list of contents; and shows why preservation of every selected component need not imply preservation of the world constituted by their relations.

The result is especially important for Macrolife. A civilization may continue through radical material transformation while the question of whether its world continues remains independently open [2].

D.1. Relational Realizations

Let X denote a collection of realized entities.

A purely extensional description of a state would specify only a set

$$X_t = \{x_1, \dots, x_n\}.$$

For worldhood this is insufficient.

Introduce a family of relations

$$\mathcal{R}_t = \{R_t^{(1)}, R_t^{(2)}, \dots, R_t^{(k)}\},$$

a family of constraints

$$C_t = \{C_t^{(1)}, C_t^{(2)}, \dots, C_t^{(m)}\},$$

and a family of admissible transformations

$$A_t.$$

Define a relational realization by

$$W_t = (X_t, \mathcal{R}_t, C_t, A_t).$$

The notation W_t should not yet be read as asserting that a world exists.

It denotes candidate world-constituting structure.

Worldhood is the further claim that this structure closes sufficiently to support the distinctions, recurrences, and continuations by which its constituents are jointly realized.

D.2. World Signatures

Let

$$\Sigma(W)$$

denote a world signature extracted from a relational realization W .

A useful schematic form is

$$\Sigma(W) = (\mathcal{B}, \mathcal{R}, \mathcal{C}, \mathcal{P}, \mathcal{Q}),$$

where $\mathcal{B}$ records boundary structure, $\mathcal{R}$ relational organization, $\mathcal{C}$ operative constraints, $\mathcal{P}$ admissible path structure, and $\mathcal{Q}$ recurrence or closure structure.

The components need not be represented identically in every application.

The important point is that

$$\Sigma(W)$$

is relational.

It is not merely an inventory of objects.

Two candidate worlds may therefore contain equivalent components while possessing inequivalent world signatures.

D.3. The Failure of Componentwise Persistence

Suppose

$$W = (X, \mathcal{R}, \mathcal{C}, \mathcal{A})$$

and

$$W' = (X', \mathcal{R}', \mathcal{C}', \mathcal{A}').$$

Assume there exists a bijection

$$f : X \rightarrow X'$$

such that every object in X has a corresponding object in X' .

This alone does not imply

$$W \equiv_{\text{world}} W'.$$

The relations may differ.

The constraints may differ.

The available trajectories may differ.

The boundary conditions under which the entities jointly realize one another may differ.

Proposition D.1 (Component preservation is insufficient). *A bijection between the constituent sets of two relational realizations is not sufficient to establish world-equivalence.*

Proof. Choose

$$X = \{a, b\}$$

and

$$X' = \{a', b'\},$$

with bijection

$$f(a) = a', \quad f(b) = b'.$$

Let R hold between a and b , while the corresponding relation R' does not hold between a' and b' . The constituent sets are bijectively matched, but their relational structures are not preserved. Therefore constituent correspondence alone cannot establish equivalence of the complete relational realizations. $\square$

The result is elementary.

Its philosophical consequence is not.

Replacing every component of a world with an individually adequate counterpart does not by itself replace the world.

D.4. Three Persistence Questions

Let

$$o_t$$

denote an object,

$$C_t$$

a civilization, and

$$W_t$$

a candidate world at time t .

Define three distinct continuation predicates:

$$\text{Cont}_O(o_t, o_{t'})$$

for object-continuation,

$$\text{Cont}_C(C_t, C_{t'})$$

for civilization-continuation, and

$$\text{Cont}_W(W_t, W_{t'})$$

for world-continuation.

No implication among these predicates should be assumed without argument.

In particular,

$$\text{Cont}_O(o_t, o_{t'}) \not\Rightarrow \text{Cont}_C(C_t, C_{t'}),$$

$$\text{Cont}_C(C_t, C_{t'}) \not\Rightarrow \text{Cont}_W(W_t, W_{t'}),$$

and

$$\text{Cont}_W(W_t, W_{t'}) \not\Rightarrow \text{Cont}_O(o_t, o_{t'})$$

in general.

A world may continue while particular objects disappear.

A civilization may continue while the ecological and relational world from which it arose does not.

An object may persist through the collapse of the civilization that once gave it significance.

These are different questions because their admissibility constraints are different.

D.5. Macrolife and the Separation of Scales

Zebrowski's Macrolife supplies an unusually strong thought experiment because the relevant unit of persistence expands beyond the organism and even beyond the planetary society [2].

Suppose a civilization undergoes a trajectory

$$C_0 \rightsquigarrow_{\text{causal}} C_1 \rightsquigarrow_{\text{causal}} \cdots \rightsquigarrow_{\text{causal}} C_n$$

through migration, habitat construction, technological transformation, and changes of material substrate.

It may be defensible that

$$\text{Cont}_C(C_0, C_n) = 1.$$

But let the ancestral world be

$$W_0 = (X_0, \mathcal{R}_0, C_0, A_0)$$

and the later world be

$$W_n = (X_n, \mathcal{R}_n, C_n, A_n).$$

Civilizational continuation does not settle whether

$$\text{Cont}_W(W_0, W_n) = 1.$$

The civilization may have survived precisely by ceasing to participate in the relations that constituted its former world.

The success of one continuation can therefore coincide with the failure of another.

D.6. Constraint-Relative World-Equivalence

Let

$$\mathfrak{W}$$

be a space of candidate world realizations.

Define a task-relative relation

$$\equiv_{\text{world}}^{\mathcal{K}}$$

by

$$W \equiv_{\text{world}}^{\mathcal{K}} W'$$

when W and W' preserve the world-constituting structures selected by a constraint family $\mathcal{K}$.

The superscript is important.

There is no reason to expect world-equivalence to be absolute.

For one inquiry, preserving causal accessibility may suffice.

For another, ecological reciprocity may be essential.

For another, the relevant structure may include institutional memory, boundary relations, or recurrence classes.

Thus

$$W \equiv_{\text{world}}^{\mathcal{K}_1} W'$$

need not imply

$$W \equiv_{\text{world}}^{\mathcal{K}_2} W'.$$

Worldhood, like provenance, is typed by the distinctions one requires the representation to preserve.

D.7. Signature-Preserving Maps

Let

$$F : W \rightarrow W'$$

be a transformation between candidate world realizations.

Suppose there exists an induced map

$$F_\Sigma : \Sigma(W) \rightarrow \Sigma(W').$$

Remark D.2 (Inducedness is assumed, not derived). Σ is given schematically in appendix D.2 as a 5-tuple and is not equipped here with a functorial construction. The existence of F_Σ for a given F is therefore a standing assumption of this subsection, component by component, rather than a consequence derived from the definition of Σ itself. A fully general construction of F_Σ from F is left open.

A strong form of world preservation would require F_Σ to preserve all relations designated by $\mathcal{K}$.

Schematically,

$$\Sigma_{\mathcal{K}}(W) \simeq \Sigma_{\mathcal{K}}(W').$$

This condition is stronger than preservation of the objects in W .

It is also weaker than literal identity of every constituent.

Remark D.3 ($\mathcal{D}$ is local; A_W is global). One component of $\Sigma(W)$ is $\mathcal{D}$, the admissible path structure available at W — this is a per-state, local property, in the sense of A_X from section 5.3: which elementary transformations are admissible starting from this state. It is not A_W , the global, trajectory-level property of which complete histories count as admissible world-continuations. Preserving $\mathcal{D}$ under F_Σ says something about the local menu of transitions available at corresponding states; it does not by itself place any history through those states inside A_W , for the same reason $\gamma(t) \in A_X$ for all t does not imply $\gamma \in A_T$.

This supplies an intermediate notion of world-structural preservation appropriate to a theory in which nothing original need survive. It does not, by itself, establish world-continuation. Two terminal realizations may preserve the same $\mathcal{K}$ -selected world signature while differing in provenance, or while failing to be connected by any admissible world history: continuation requires the further trajectory-level condition introduced in appendix D.9 below, and

$$\Sigma_{\mathcal{K}}(W_0) \simeq \Sigma_{\mathcal{K}}(W_1) \not\Rightarrow \text{Cont}_W(W_0, W_1).$$

D.8. Total Material Replacement

Suppose a world trajectory

$$\Gamma_W = (W_0 \rightarrow W_1 \rightarrow \dots \rightarrow W_n)$$

replaces every original material constituent.

Let

$$M(W_i)$$

denote the material inventory of W_i .

Assume

$$M(W_0) \cap M(W_n) = \emptyset.$$

This fact alone proves neither world-discontinuity nor world-continuation.

Proposition D.4 (Material overlap is neither necessary nor sufficient). *Within a relational account of worldhood, nonzero material overlap is neither a necessary nor a sufficient condition for world-continuation.*

Proof. For non-necessity, consider a trajectory in which every material component is replaced while all world-defining relations designated by $\mathcal{K}$ are continuously preserved and the trajectory remains within the admissible world-history family $\mathcal{A}_W$ introduced in appendix D.9 below. Under such a criterion, continuation may hold despite

$$M(W_0) \cap M(W_n) = \emptyset.$$

For non-sufficiency, preserve a single material component while destroying the relations designated by $\mathcal{K}$ or leaving the admissible family $\mathcal{A}_W$. Material overlap remains nonempty, but the selected world-continuation criterion fails. $\square$

This is the formal core of the title's claim.

The word “need” matters.

The proposition does not say that material continuity is irrelevant.

It says that material overlap cannot serve as a universal criterion.

D.9. The World Path Space

Let

$$\Gamma(\mathfrak{W})$$

denote histories of candidate world realizations.

Let

$$\mathcal{A}_W \subseteq \Gamma(\mathfrak{W})$$

be the subset satisfying the selected world-continuation constraints.

Remark D.5 ($\mathcal{K}$ and $\mathcal{A}_W$ are distinct constraint families). $\mathcal{K}$ (appendix D.6) selects which *states* count as world-equivalent; $\mathcal{A}_W$ selects which *histories* count as admissible world-continuations. Nothing in their definitions identifies one with the other, and a trajectory can satisfy either without satisfying the other: a history can preserve every $\mathcal{K}$ -designated relation at each endpoint while failing to lie in $\mathcal{A}_W$, and conversely. Any stated relationship between them — for instance, that $\mathcal{A}_W$ consists exactly of the histories along which $\mathcal{K}$ -equivalence holds at every intermediate state — is a bridge principle in the sense of theorem D.6, and is not assumed here.

For $W_0, W_1 \in \mathfrak{W}$, define

$$\Gamma_{A_W}(W_0, W_1) = \{\gamma \in A_W : \text{Orig}(\gamma) = W_0, \text{End}(\gamma) = W_1\}.$$

Then a trajectory-based world-continuation predicate may be defined by

$$\text{Cont}_W(W_0, W_1) = 1$$

exactly when

$$\Gamma_{A_W}(W_0, W_1) \neq \emptyset.$$

The definition makes world-continuation a property of admissible histories between world realizations.

It is not a binary comparison of isolated endpoints.

D.10. World-Level Convergent Reconstruction

The Originist problem now reappears at world scale.

Suppose

$$W_A \equiv_{\text{world}}^{\mathcal{K}} W_B.$$

It does not follow that their histories are equivalent.

One world may be the uninterrupted continuation of an earlier realization.

Another may have been independently reconstructed from records.

A third may be a deliberate simulation.

A fourth may have converged upon the same organization without any common genealogical path.

Thus

$$W_A \equiv_{\text{world}}^{\mathcal{K}} W_B$$

can coexist with

$$\gamma_{W_A} \neq \gamma_{W_B}.$$

This is the world-level analogue of the essay's original case

$$x_A = x_B, \quad \gamma_A \neq \gamma_B.$$

The same distinction has survived every increase in scale.

D.11. Worlds Have Provenance

If worldhood is reconstructed from relational organization, then candidate worlds themselves inherit provenance.

Define

$$\text{Prov}_W : \Gamma(\mathfrak{W}) \rightarrow D_W$$

as a world-provenance observable.

Its values may encode ancestral worlds, transformation classes, branching events, reconstruction episodes, or uncertainty over these.

Two worlds can therefore satisfy

$$\Sigma_K(W_A) = \Sigma_K(W_B)$$

while

$$\text{Prov}_W(\gamma_{W_A}) \neq \text{Prov}_W(\gamma_{W_B}).$$

Consequently,

$$\text{world-equivalence} \neq \text{world-provenance equivalence}.$$

The distinction is not an exotic extension of the Originist thesis.

It is that thesis applied consistently.

D.12. Worldhood Is Not Presupposed

The expression “No-World” can now be stated negatively and positively.

Negatively, the framework refuses the inference

$$\text{entities exist} \Rightarrow \text{one determinate world containing them is primitive}.$$

Positively, it treats worldhood as a successful organization of relations, constraints, boundaries, and admissible continuations.

Let

$$\omega : \mathfrak{W} \rightarrow \{0, 1\}$$

be a worldhood predicate.

Then

$$\omega(W) = 1$$

only when W satisfies the selected closure conditions.

The exact closure conditions belong to the underlying theory and need not be fixed universally here.

What matters is the order of explanation:

relational realization $\rightarrow$ closure $\rightarrow$ worldhood,

rather than

world $\rightarrow$ relations inside it.

D.13. The Originist Reading of Worldhood

This reversal reveals the deeper relation to Card.

An Originist begins with surviving traces and attempts to infer a structure that is no longer directly available [1].

A No-World theorist begins with local realizations, recurrences, constraints, and relations and asks whether they warrant reconstruction of a coherent world.

The formal shapes are similar.

Let E denote available evidence and let

$$\mathcal{W}(E)$$

be the class of candidate worlds compatible with it.

Then world reconstruction is an inverse problem:

$$E \rightsquigarrow \mathcal{W}(E).$$

If

$$|\mathcal{W}(E)| > 1,$$

the evidence underdetermines worldhood.

A single inferred world may still be selected by additional constraints or priors.

But selection should not be confused with direct possession of the world as a primitive datum.

D.14. Branching World-Continuation

Suppose a world realization W_0 admits two admissible continuations:

$$W_0 \rightsquigarrow_{\text{causal}} W_A$$

and

$$W_0 \rightsquigarrow_{\text{causal}} W_B.$$

Assume

$$W_A \neq W_B.$$

If both trajectories satisfy the selected world-admissibility conditions, then world-continuation branches.

The resulting structure is not a single line

$$W_0 \rightarrow W_1 \rightarrow W_2,$$

but a provenance graph

$$\mathcal{G}_W.$$

Worldhood therefore inherits the branching problem established for personal and civilizational continuation.

A unique future world cannot be inferred merely from continuity with the present.

D.15. Le Guin's Dissemination Problem

The dissemination of Shevek's work in The Dispossessed supplies a different kind of branching [3].

Knowledge leaves one political world and becomes available beyond the institutions that previously constrained its circulation.

The relevant trajectory is therefore not merely

$$\gamma : O \rightarrow X \rightarrow O'.$$

It also branches:

$$\gamma \longrightarrow \{\gamma_1, \gamma_2, \dots\}.$$

Once the knowledge becomes multiply instantiated, no single receiving world exhausts its continuation.

This matters because dissemination can preserve content while breaking the exclusive provenance relation through which one institution previously controlled it.

The return and the branching are therefore coupled.

The origin remains part of the history.

It ceases to be the sole container of the future.

D.16. Recurrence Without Restoration

Suppose a world trajectory satisfies

$$W_0 \rightsquigarrow W_1 \rightsquigarrow \dots \rightsquigarrow W_n$$

and

$$W_n \equiv_{\text{world}}^{\mathcal{K}} W_0.$$

Even then,

$$\gamma_{W_n} \neq \gamma_{W_0}$$

in the relevant historical sense.

If the loop carries nontrivial holonomy as in appendix C.11, the return can be world-equivalent while historically nontrivial.

Thus a restored world is not an untouched world.

A reconstructed world is not an unbroken world.

A returned world is not a world that never departed.

The endpoint relation cannot erase the loop that produced it.

D.17. An RSVP Reading

The RSVP framework offers one possible continuous realization of these ideas.

Let a candidate world state be represented schematically by

$$\mathfrak{R}_t = (\Phi_t, \mathbf{v}_t, S_t),$$

where Φ_t is a scalar field, $\mathbf{v}_t$ a vector field, and S_t an entropy-like field.

The present essay does not require a specific RSVP dynamics.

It requires only that world-relevant structure be encoded relationally across the fields and their evolution.

A trajectory is then

$$\Gamma_{\text{RSVP}} = \{\mathfrak{R}_t\}_{t \in I}.$$

World-continuation cannot be reduced to equality

$$\mathfrak{R}_{t_0} = \mathfrak{R}_{t_1}.$$

Nor need it require such equality.

Instead, one asks whether the field evolution remains within an admissible class

$$\Gamma_{\text{RSVP}} \in \mathcal{A}_{\text{W}}$$

and whether the relations constitutive of the relevant world signature remain realizable along that history.

This places RSVP on the trajectory side of the state/history distinction.

D.18. World-Continuation Is Not Temporal Inversion

Suppose an admissible transformation carries

$$W_0 \rightarrow W_1.$$

Even if another admissible transformation later produces

$$W_1 \rightarrow W'_0$$

with

$$W'_0 \equiv_{\text{world}}^{\mathcal{K}} W_0,$$

it does not follow that the second transformation inverted the first.

The composite history

$$W_0 \rightarrow W_1 \rightarrow W'_0$$

contains events absent from the zero-length history at W_0 .

If provenance is retained, then

$$[W_0] \neq [W'_0]_{\text{prov}}.$$

Irreversibility here need not mean that no state can recur.

It means that recurrence of state does not annihilate occurrence of history.

This is the minimal irreversibility thesis required by the essay.

D.19. The Separation Theorem

The distinctions developed above can now be stated formally.

The three persistence predicates used below are instances of the same trajectory-relative construction at different scales. Let $S \in \{O, C, W\}$ denote respectively the object, civilizational, and world scales. For each S , let X_S be the corresponding state space, let $\Gamma(X_S)$ be its history space, and let

$$A_S = A_{C_S} \subseteq \Gamma(X_S)$$

be the histories admissible relative to a specified scale-appropriate constraint family C_S , in the sense of remark 5.2. Define

$$\Gamma_{A_S}(a, b) = \{\gamma \in A_S : \text{Orig}(\gamma) = a, \text{End}(\gamma) = b\},$$

and

$$\text{Cont}_S(a, b) = 1 \iff \Gamma_{A_S}(a, b) \neq \emptyset.$$

Thus Cont_O , Cont_C , and Cont_W share a common formal shape without thereby sharing a common admissibility criterion: Cont_W is exactly the $S = W$ instance already defined in appendix D.9, and Cont_O , Cont_C are its $S = O$, $S = C$ counterparts. A bridge principle between two persistence scales is additional structure relating their state spaces, histories, or admissibility constraints. No such bridge is contained merely in the fact that continuation holds at one scale.

Theorem D.6 (Separation of persistence scales). *For $S, S' \in \{O, C, W\}$ with $S \neq S'$, no bridge principle between scale S and scale S' is derivable from the schema above alone. Consequently, without additional assumptions relating A_O , A_C , and A_W , none of Cont_O , Cont_C , Cont_W determines either of the other two.*

Proof. It is enough to provide separating cases.

An object can persist while its civilization and world collapse, so Cont_O does not determine Cont_C or Cont_W .

A civilization can preserve its organizational continuity while migrating away from the ecological and relational structure constitutive of its prior world, so Cont_C does not determine Cont_W .

A world can preserve its relevant relational organization while particular objects and civilizations disappear and are replaced, so Cont_W does not determine Cont_O or Cont_C .

In each case the schema above supplies the reason such a case is even statable: X_O , X_C , and X_W are distinct state spaces with distinct admissible families A_O , A_C , A_W , so a nonempty $\Gamma_{A_S}(a, b)$ at one scale carries no formal content about $\Gamma_{A_{S'}}(a', b')$ at another unless a bridge principle explicitly relates A_S to $A_{S'}$. Therefore no implication follows without additional assumptions connecting the respective admissibility criteria. $\square$

The theorem is deliberately modest.

It does not claim that the scales are unrelated.

It says that their relation must be supplied rather than smuggled into the word “continuity”.

D.20. Persistence Without a Primitive Container

If the preceding analysis is accepted, then the familiar question

Does x remain in the same world?

decomposes into at least two questions.

First,

$\text{Cont}_O(x_0, x_1)?$

Second,

$\text{Cont}_W(W_0, W_1)?$

The second cannot be answered merely by pointing to a container in which both states are located, because the persistence of that container is precisely what is at issue.

Worldhood must itself possess a trajectory.

Thus

$W_0 W_1$

is not background notation.

It is part of the object of inquiry.

D.21. The Result Needed by the Essay

The technical argument of this appendix can be compressed into the following statement.

Theorem D.7 (World-Originist principle). *Suppose worldhood is constituted by relational and trajectory-dependent structure. Then equality or equivalence of terminal world states is insufficient, in general, to determine world provenance. If, in addition, world-continuation is evaluated by an admissibility criterion that distinguishes histories with equivalent terminal states, then terminal world equivalence is likewise insufficient to determine world-continuation.*

Proof. Let

$$\text{End}_W : \Gamma(\mathfrak{W}) \rightarrow \mathfrak{W}$$

be the world-level endpoint map.

Suppose two distinct world histories satisfy

$$\gamma_A \neq \gamma_B$$

while

$$\text{End}_W(\gamma_A) \equiv_{\text{world}}^{\mathcal{K}} \text{End}_W(\gamma_B).$$

Any world-provenance observable that differs on γ_A and γ_B is not determined by the equivalent endpoints. By theorem A.8, such an observable cannot factor through the endpoint representation alone.

If the admissibility of continuation also depends upon the histories, then world-continuation likewise cannot be inferred from terminal equivalence alone. $\square$

NO-WORLD CONSEQUENCE

*A world is not what remains after history is discarded.
If worldhood persists, its persistence has a history too.*

This completes the mathematical ascent begun with the smallest Originist example.

At the artifact level,

$$x_A = x_B$$

did not imply equality of histories.

At the civilizational level, material replacement did not settle continuation.

At the world level, even world-equivalent endpoints fail to determine whether one world has continued into another.

The scale has changed.

The structural distinction has not.

MOVEMENT V. IRREVERSIBILITY, BRANCHING, AND THE PATH CATEGORY

What changes when histories are treated as arrows rather than when states alone are treated as the objects of metaphysical comparison?

The preceding appendices have repeatedly used the same structure without yet naming it categorically. There are states. There are transformations between states. Transformations can be composed when the endpoint of one is the origin of another. Different histories may share the same endpoints. Some histories can be reversed; others cannot. Branches can depart from a common origin and later converge.

This is naturally represented by a category of paths.

The categorical language is useful here for a specific reason. It prevents several distinctions from being collapsed into the notation for endpoint identity. A path from x to y is not the equation $x = y$. Two paths with the same source and target need not be the same path. The existence of a path from x to y does not imply the existence of a path from y to x . Even when both exist, they need not be inverses.

Those elementary facts provide a compact formal home for the essay's irreversibility thesis. They also expose the danger of passing too quickly to a groupoid, where every arrow is invertible. Groupoid completion can be mathematically useful, but an Originist must ask what historical distinction is being changed when an irreversible path is supplied with a formal inverse.

The appendix ends by returning to the three literary probes. Card asks about arrows whose sources are partially hidden. Zebrowski asks which outgoing arrows count as continuation. Le Guin asks what it means for a path to return to an object or its equivalence class without thereby becoming the identity arrow.

E.1. States as Objects and Histories as Morphisms

As in remark 5.2, admissibility here is relative to a specified constraint family C . Thus the category constructed below is, more explicitly, $\mathbf{Path}_A(X)$. When a single constraint family is fixed by context, we suppress this dependence and write $\mathbf{Path}_A(X)$. Accordingly, every result stated below in terms of $\mathbf{Path}_A(X)$ — including faithfulness and cancellation — is conditional on the admissibility structure induced by that fixed C . (The Separation Theorem of appendix D.19 is not among these: its continuation predicates Cont_O , Cont_C , Cont_W are introduced independently of A and are not currently defined in terms of it.) In particular,

$$C_1 \neq C_2 \implies \mathbf{Path}_{A_{C_1}}(X) \text{ need not equal } \mathbf{Path}_{A_{C_2}}(X).$$

Let X be a state space and let A specify the admissible elementary transformations between states.

Construct a directed graph whose vertices are states

$$x \in X$$

and whose directed edges are admissible elementary transformations

$$x \xrightarrow{T} y.$$

The free path category generated by this graph will be denoted

$$\mathbf{Path}_A(X).$$

Its objects are the states of X .

Its morphisms

$$\mathrm{Hom}_{\mathbf{Path}_A(X)}(x, y)$$

are finite admissible paths from x to y .

A morphism may therefore be written

$$\gamma : x \longrightarrow y,$$

where

$$\gamma = \left(x = x_0 \xrightarrow{T_1} x_1 \xrightarrow{T_2} \cdots \xrightarrow{T_n} x_n = y \right).$$

Composition is concatenation.

If

$$\gamma : x \rightarrow y$$

and

$$\eta : y \rightarrow z,$$

then

$$\eta \circ \gamma : x \rightarrow z$$

is the history obtained by traversing γ and then η .

For each state x , the identity morphism

$$1_x : x \rightarrow x$$

is the zero-length path at x .

E.2. Parallel Histories

The central Originist distinction appears categorically as the possibility of parallel morphisms.

Suppose

$$\gamma_A, \gamma_B : x \rightarrow y.$$

Both histories have the same origin and endpoint.

Nevertheless,

$$\gamma_A \neq \gamma_B$$

may hold.

Thus

$$\text{Hom}(x, y)$$

need not contain only one element.

A state-only representation effectively forgets which member of

$$\text{Hom}(x, y)$$

was realized.

Proposition E.1 (Endpoint coincidence does not determine a morphism). *If*

$$|\text{Hom}(x, y)| > 1,$$

then knowledge of the ordered pair

$$(x, y)$$

is insufficient to determine the realized history.

Proof. Let

$$\gamma_1, \gamma_2 \in \text{Hom}(x, y)$$

with

$$\gamma_1 \neq \gamma_2.$$

Both correspond to the same source-target pair. Therefore the pair (x, y) cannot uniquely select which morphism was realized. $\square$

This is the categorical form of

$$x_A = x_B \quad \text{while} \quad \gamma_A \neq \gamma_B.$$

The endpoint state may converge.

The morphisms remain distinct.

E.3. Remaining Is Not Returning

The distinction between the identity morphism and a nontrivial loop is especially important.

For a state x ,

$$1_x : x \rightarrow x$$

contains no intervening transformation.

Now suppose

$$\gamma : x \rightarrow x$$

is a nontrivial loop.

Although

$$\text{Orig}(\gamma) = \text{End}(\gamma) = x,$$

it does not follow that

$$\gamma = 1_x.$$

Indeed, in the free path category,

$$\gamma = 1_x$$

only if γ is the empty path.

CATEGORICAL FORM OF THE RETURN PROBLEM

To return to the same object is not to have taken the identity morphism.

This is the categorical core of recurrence without restoration.

E.4. Invertibility Is an Additional Property

Let

$$\gamma : x \rightarrow y.$$

The existence of γ does not imply the existence of any morphism

$$\eta : y \rightarrow x.$$

Even when such an η exists, it does not follow that

$$\eta \circ \gamma = 1_x$$

and

$$\gamma \circ \eta = 1_y.$$

Only when both equations hold is γ an isomorphism with inverse η .

Thus causal reachability

$$x \rightsquigarrow_{\text{causal}} y$$

is weaker than categorical invertibility.

Definition E.2 (Historical irreversibility). An admissible history

$$\gamma : x \rightarrow y$$

is *historically irreversible* in a path category when it is not an isomorphism.

This definition is intentionally structural.

It does not require a thermodynamic claim.

A process may be historically irreversible simply because the category of admissible transformations contains no genuine inverse for it.

E.5. Going Back Is Not Undoing

Suppose

$$\gamma : x \rightarrow y$$

and

$$\eta : y \rightarrow x.$$

The existence of both directions establishes mutual reachability.

It does not establish

$$\eta = \gamma^{-1}.$$

Their composite may be a nontrivial loop:

$$\eta \circ \gamma : x \rightarrow x,$$

with

$$\eta \circ \gamma \neq 1_x.$$

Similarly,

$$\gamma \circ \eta \neq 1_y$$

may hold.

This provides a categorical version of the distinction already developed through recurrence and holonomy.

One may return to an equivalent state without undoing the history by which one left it.

E.6. Recording Histories Functorially

Let $\mathbf{P}$ be a category whose objects encode provenance states and whose morphisms encode provenance transformations.

A provenance assignment may be represented by a functor

$$\text{Prov} : \mathbf{Path}_A(X) \rightarrow \mathbf{P}.$$

Functoriality requires

$$\text{Prov}(1_x) = 1_{\text{Prov}(x)}$$

and

$$\text{Prov}(\eta \circ \gamma) = \text{Prov}(\eta) \circ \text{Prov}(\gamma).$$

The construction makes composition history-sensitive.

For example, if provenance morphisms record transformation words, then

$$\text{Prov}(\gamma) = R \circ C \circ R$$

may differ from

$$\text{Prov}(\gamma') = C \circ R \circ R$$

even when

$$\text{Orig}(\gamma) = \text{Orig}(\gamma')$$

and

$$\text{End}(\gamma) = \text{End}(\gamma').$$

Generation count can then be obtained by a further forgetting map that retains only word length.

E.7. Forgetting the Arrow

A state-oriented system can be modeled by a representation that forgets some or all morphism structure.

At the crudest level, consider the endpoint operation

$$\text{End} : \text{Mor}(\mathbf{Path}_A(X)) \rightarrow \text{Ob}(\mathbf{Path}_A(X)).$$

This is not itself ordinarily a functor between the same categories, because it maps morphisms to objects, but it captures the relevant forgetting operation.

More structured quotients may instead be represented by functors

$$F : \mathbf{Path}_A(X) \rightarrow \mathbf{C}$$

that identify multiple morphisms.

If

$$F(\gamma_1) = F(\gamma_2)$$

while

$$\text{Prov}(\gamma_1) \neq \text{Prov}(\gamma_2),$$

then F is not faithful with respect to the provenance distinction.

This suggests a categorical reformulation of Originist loss.

E.8. Faithfulness

Recall that a functor

$$F : \mathbf{C} \rightarrow \mathbf{D}$$

is faithful when, for every pair of objects x, y , the induced map

$$F_{x,y} : \text{Hom}_{\mathbf{C}}(x, y) \rightarrow \text{Hom}_{\mathbf{D}}(F(x), F(y))$$

is injective.

If F is not faithful, then there exist distinct parallel morphisms

$$\gamma_1 \neq \gamma_2$$

such that

$$F(\gamma_1) = F(\gamma_2).$$

This is almost exactly the Originist failure mode.

Definition E.3 (Originist-faithful representation). A functorial representation F is *Originist-faithful* relative to a provenance distinction when it does not identify morphisms that differ under that provenance distinction.

Full categorical faithfulness may preserve more information than a task requires.

Originist faithfulness is therefore relative to the distinctions whose loss would affect the intended inference.

E.9. Branching as Multiple Outgoing Morphisms

Suppose

$$\alpha : x \rightarrow y$$

and

$$\beta : x \rightarrow z$$

are admissible histories with

$$y \neq z.$$

The common source x has branched into distinct descendants.

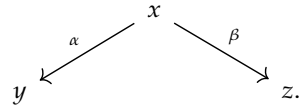
Nothing in category theory requires one branch to be more authentic than the other.

Both morphisms exist.

If both satisfy the relevant admissibility constraints, then both are continuations in the weaker relational sense.

The question of numerical identity cannot be settled by the mere existence of these arrows, as established in proposition A.7.

Categorically, the structure is simply



The fork is not a defect in the model.

It is information the model must preserve.

E.10. Convergence as Multiple Incoming Histories

Dually, suppose

$$\alpha : x \rightarrow z$$

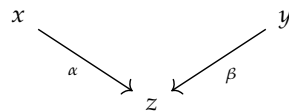
and

$$\beta : y \rightarrow z$$

with

$$x \neq y.$$

Then distinct origins converge upon the same endpoint.



This is the categorical shape of independent rediscovery and convergent reconstruction.

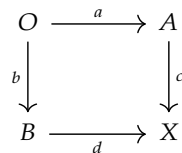
The terminal object z , considered only as a state, does not tell us whether it was reached through α , through β , or through some other morphism.

The convergence problem is therefore not exceptional.

It is built into any category in which distinct arrows may share a codomain.

E.11. Commutativity Can Erase a Distinction

Suppose



commutes.

Then

$$c \circ a = d \circ b$$

as morphisms in the category.

This equality should not automatically be interpreted as historical identity.

Whether the two composites are genuinely to be identified depends upon what relations were imposed when constructing the category.

In a free path category, the two paths remain distinct unless an explicit relation equates them.

In a quotient category, they may become equal.

Thus the statement that a diagram commutes can itself encode a decision to forget path distinctions.

The Originist question is therefore prior:

Why are these composites being identified?

E.12. Relations Are Historical Commitments

A category may be presented by generators and relations.

Let G be a directed graph of elementary transformations and let

$$\mathbf{Free}(G)$$

be its free category.

Now impose a collection of relations

$$\mathcal{R}$$

among paths.

The resulting category is schematically

$$\mathbf{C} = \mathbf{Free}(G) / \mathcal{R}.$$

Every relation of the form

$$\gamma_1 \sim_{\mathcal{R}} \gamma_2$$

declares two histories equivalent for the purposes of $\mathbf{C}$.

This is mathematically ordinary.

From the Originist perspective, however, the relation set $\mathcal{R}$ becomes an epistemic object.

Each relation states which historical distinctions the formalism has chosen not to preserve.

The quotient-loss operator of Appendix B can therefore be applied to categorical presentations themselves.

E.13. Formal Reversibility

Given a category $\mathbf{C}$, one may formally invert a selected collection of morphisms.

In the extreme case, invert every morphism to obtain a groupoid completion

$$\mathbf{C} \longrightarrow \mathbf{C}[\mathrm{Mor}(\mathbf{C})^{-1}].$$

For the path category, denote this schematically by

$$\mathbf{Path}_{\mathcal{A}}(X) \longrightarrow \mathbf{Gpd}_{\mathcal{A}}(X).$$

Every path

$$\gamma : x \rightarrow y$$

then acquires a formal inverse

$$\gamma^{-1} : y \rightarrow x$$

satisfying

$$\gamma^{-1} \circ \gamma = 1_x$$

and

$$\gamma \circ \gamma^{-1} = 1_y.$$

This construction is mathematically legitimate.

Its ontological interpretation requires caution.

E.14. The Groupoid Warning

Suppose the original path category contains an irreversible history

$$\gamma : x \rightarrow y$$

with no inverse.

The groupoid completion introduces

$$\gamma^{-1}$$

formally.

It does not thereby establish that an admissible physical, historical, or computational process exists that literally undoes γ .

The inverse belongs to the completed formal structure.

It need not belong to the original process ontology.

GROUPOID WARNING

*Formal invertibility is a property of a chosen completion.
It is not evidence that history itself ran backward.*

This distinction matters whenever groupoid language is used in the No-World framework.

A groupoid can represent equivalences among world presentations without implying that every realized transformation is historically reversible.

E.15. Irreversibility as Lost Structure

Consider a category $\mathbf{C}$ containing

$$\gamma : x \rightarrow y$$

without an inverse.

After groupoid completion, γ becomes invertible.

The completed category therefore no longer distinguishes between

“an inverse existed in the original process category”

and

“an inverse was supplied by localization.”

Unless that provenance is recorded separately, the completion erases a historical distinction about the status of the inverse.

This is itself an Originist phenomenon.

Two arrows can be extensionally identical inside the completed groupoid while possessing different derivational status.

One was realized.

The other was formally adjoined.

E.16. Preserving the Provenance of Formal Inverses

An Originist-aware formalism can preserve this distinction by enriching the completed arrows with provenance tags.

Write

$$\gamma_{[\text{formal}]}^{-1}$$

for an inverse introduced by localization and

$$\eta_{[0]}$$

for a reverse transformation independently present in the original category.

Even if the completed category identifies

$$\eta = \gamma^{-1},$$

their provenance annotations may remain distinct:

$$\text{Prov}(\eta) \neq \text{Prov}(\gamma_{[\text{formal}]}^{-1}).$$

This is another instance of the general principle

semantic or structural equality $\nRightarrow$ provenance equality.

The provenance layer does not invalidate the quotient.

It records what the quotient would otherwise conceal.

E.17. Cancellation Is Weaker Than Invertibility

Some categories permit cancellation without general invertibility.

For example, a morphism $\gamma : x \rightarrow y$ may be left-cancellative when

$$\gamma \circ \alpha = \gamma \circ \beta$$

implies

$$\alpha = \beta.$$

Similarly, it may be right-cancellative.

These properties preserve some historical distinguishability.

They do not imply that γ possesses an inverse.

Thus a process can retain enough structure to distinguish prior paths while remaining irreversible.

This intermediate case is useful for provenance systems.

One need not choose between total reversibility and total loss.

E.18. Non-Cancellative Transformations

Suppose a transformation

$$C : x \rightarrow y$$

acts as a lossy compression.

If two distinct preceding histories

$$\alpha, \beta : o \rightarrow x$$

satisfy

$$C \circ \alpha = C \circ \beta,$$

then C is not left-cancellative with respect to those histories.

The compression has merged distinct incoming derivations.

After the merge, observing the composite does not determine whether the prior history was α or β .

This categorical pattern is exactly the one formalized by Originist loss:

$$\alpha \neq \beta, \quad C \circ \alpha = C \circ \beta.$$

A later repair morphism

$$R : y \rightarrow z$$

cannot restore left-cancellativity merely by composition, because

$$R \circ C \circ \alpha = R \circ C \circ \beta.$$

This recovers theorem B.5 categorically.

E.19. Postcomposition Cannot Separate an Existing Merge

Theorem E.4 (Categorical repair corollary). *Let*

$$\alpha, \beta : o \rightarrow x$$

be distinct morphisms and let

$$C : x \rightarrow y$$

satisfy

$$C \circ \alpha = C \circ \beta.$$

Then for every morphism

$$R : y \rightarrow z,$$

one has

$$R \circ C \circ \alpha = R \circ C \circ \beta.$$

Proof. By assumption,

$$C \circ \alpha = C \circ \beta.$$

Postcompose both sides with R . Associativity gives

$$R \circ (C \circ \alpha) = R \circ (C \circ \beta),$$

hence

$$R \circ C \circ \alpha = R \circ C \circ \beta.$$

□

The result is trivial algebraically.

Conceptually it is central.

Once two histories have been merged by a representation, deterministic postprocessing of that representation cannot separate them again.

A distinction must enter from somewhere else.

E.20. Restoring Distinguishability by Enrichment

Suppose an archival channel supplies additional information

$$A : x \rightarrow p.$$

Instead of representing the history only through C , construct the paired representation

$$\langle C, A \rangle : x \rightarrow y \times p.$$

It may happen that

$$C \circ \alpha = C \circ \beta$$

while

$$A \circ \alpha \neq A \circ \beta.$$

Then

$$\langle C, A \rangle \circ \alpha \neq \langle C, A \rangle \circ \beta.$$

The archive restores distinguishability not by reversing the compression but by preserving another projection.

This gives a categorical interpretation of the Archivist/Originist split.

The Archivist maintains additional arrows.

The Originist knows when they are required.

E.21. Hidden Sources

Card's originism can now be represented as an inference problem over incoming morphisms [1].

Given a present state x , one seeks candidate pairs

$$(O, \gamma)$$

such that

$$\gamma : O \rightarrow x.$$

The inverse problem is therefore not merely

$$x \rightsquigarrow O?$$

but

$$x \rightsquigarrow \{(O, \gamma) : \gamma \in \text{Hom}(O, x)\}.$$

Even if the origin object O were uniquely identified, the morphism γ might remain underdetermined.

Thus origin recovery and history recovery are distinct inverse problems.

E.22. Admissible Futures

The Macrolife problem points in the opposite direction [2].

Given an origin O , consider the collection

$$\coprod_X \text{Hom}(O, X).$$

This is the family of represented outgoing histories from O .

Continuation introduces an admissibility predicate

$$A : \text{Mor}(\mathbf{Path}_A(X)) \rightarrow \{0, 1\}.$$

The relevant future space becomes

$$\{\gamma : O \rightarrow X : A(\gamma) = 1\}.$$

The problem is therefore not to identify one predetermined future.

It is to characterize the admissible cone of descent.

E.23. Return and Endomorphisms

Le Guin's recurrence problem is naturally expressed through endomorphisms [3].

An endomorphism of O is a morphism

$$\gamma : O \rightarrow O.$$

More generally, if return is only to an equivalent origin O' , one has

$$\gamma : O \rightarrow O'$$

with

$$O' \sim_c O.$$

The crucial distinction is between

$$1_O$$

and a nontrivial historical loop

$$\gamma.$$

The former says nothing happened.

The latter says departure and return occurred.

Endpoint recurrence identifies what the two share.

Provenance records what they do not.

E.24. One Category, Three Directions

The three literary probes can now be expressed within one structure.

Card begins at X and asks which incoming histories are warranted:

$$\coprod_O \text{Hom}(O, X).$$

Zebrowski begins at O and asks which outgoing histories remain admissible:

$$\coprod_X \text{Hom}(O, X).$$

Le Guin asks about histories that return:

$$\text{End}(O) = \text{Hom}(O, O),$$

or, more generally,

$$\coprod_{O' \sim_c O} \text{Hom}(O, O').$$

The three questions are therefore neither identical nor accidentally similar.

They interrogate different regions of the same path structure.

E.25. Closure Under Composition

For admissible histories to form a category, admissibility must satisfy at least two closure conditions.

Identity histories must be admissible:

$$A(1_x) = 1.$$

And whenever

$$A(\gamma) = 1$$

and

$$A(\eta) = 1$$

for composable histories, one must have

$$A(\eta \circ \gamma) = 1.$$

If the second condition fails, admissible segments do not automatically compose into admissible histories.

This reproduces the local-to-global warning of Appendix C in categorical language.

One should therefore distinguish a category of globally admissible histories from a graph whose edges are merely locally admissible.

Proposition E.5 (Composition requires a global admissibility principle). *Local admissibility of elementary transformations defines a category of admissible histories only if admissibility is closed under finite composition.*

This condition should never be presumed merely because each step passes an individual test.

E.26. When Composition Changes the Judgment

Suppose

$$A(\gamma) = 1$$

and

$$A(\eta) = 1$$

but

$$A(\eta \circ \gamma) = 0.$$

Then admissibility depends upon more than the local morphisms considered in isolation.

This can occur through accumulated drift, forbidden transformation sequences, resource exhaustion, provenance depth, or global gluing obstruction.

The correct structure may then require enriched objects carrying sufficient history to make composition local again.

For example, replace a state x by

$$(x, h),$$

where h records a relevant historical summary.

A transformation acts on both:

$$(x, h) \longrightarrow (y, h').$$

This maneuver does not eliminate history dependence.

It moves the required history into the state representation.

The price of recovering Markovian composition is therefore an enlarged state.

E.27. When History Becomes State

This observation produces an apparent challenge to the essay's thesis.

If every relevant historical quantity can be appended to the state, why insist that continuity is a property of trajectories rather than states?

Let

$$\widehat{X} = X \times H$$

be an augmented state space containing a complete history variable H .

Then a sufficiently rich augmented state

$$\hat{x} = (x, h)$$

may indeed determine provenance.

But h is itself a representation of the trajectory.

The construction therefore does not show that history was unnecessary.

It shows that history can be encoded into a larger state.

Originist Objection E.6 (The State-Augmentation Objection). If a state is allowed to contain its complete derivational history, then every trajectory-dependent property can apparently be rewritten as a state property. Why, then, privilege trajectories?

The answer is that the distinction in this essay concerns representational content, not grammatical location.

A state containing its complete history is no longer a state in the thin sense against which the trajectory argument was directed.

It is an endpoint plus a provenance archive.

The Originist has won by annexation.

E.28. How Much History Must Be Carried Forward?

The useful question is therefore not whether history can be encoded in state.

It is how much historical information must be retained for a specified future task.

Let

$$F : \Gamma(X) \rightarrow Y$$

be a task.

Seek a historical summary

$$h_F : \Gamma(X) \rightarrow H_F$$

such that

$$F(\gamma)$$

is determined by

$$(\text{End}(\gamma), h_F(\gamma)).$$

The pair

$$\hat{x}_F = (\text{End}(\gamma), h_F(\gamma))$$

is a task-sufficient augmented state.

This connects the path-category formulation directly to the minimal sufficient provenance problem of appendix B.19.

The practical Originist role is therefore not to preserve infinite history indiscriminately.

It is to determine which historical summaries future judgments cannot safely do without.

E.29. The Formal Result

We can now state the categorical result needed by the essay.

Theorem E.7 (Path-category thesis). *Let $\mathbf{C}$ be a category of admissible histories containing distinct parallel morphisms*

$$\gamma_1, \gamma_2 : x \rightarrow y.$$

Any property P satisfying

$$P(\gamma_1) \neq P(\gamma_2)$$

cannot be represented as a function solely of the source-target pair (x, y) .

Proof. Assume there exists

$$\tilde{P} : \text{Ob}(\mathbf{C}) \times \text{Ob}(\mathbf{C}) \rightarrow Z$$

such that for every morphism

$$\gamma : a \rightarrow b$$

one has

$$P(\gamma) = \tilde{P}(a, b).$$

Since γ_1 and γ_2 have the same source x and target y ,

$$P(\gamma_1) = \tilde{P}(x, y) = P(\gamma_2),$$

contradicting

$$P(\gamma_1) \neq P(\gamma_2).$$

Therefore no such state-pair representation exists. □

The theorem is simply the trajectory necessity criterion translated into categorical language.

Its advantage is that branching, convergence, composition, loops, and irreversibility now belong to one formal object.

E.30. History Survives Recurrence

Theorem E.8 (Recurrence does not erase history). *Let*

$$\gamma : x \rightarrow x$$

be a nonidentity endomorphism in a path category. Then equality of source and target does not imply

$$\gamma = 1_x.$$

Proof. By hypothesis, γ is a nonidentity endomorphism. Therefore

$$\gamma \neq 1_x$$

despite having the same source and target as 1_x . □

The proof is intentionally almost empty.

The philosophical mistake it blocks is not.

Endpoint restoration is not historical erasure.

E.31. Against Premature Thinness

The Originist objection can finally be expressed as a warning about functors and quotient categories.

Originist Objection E.9 (Categorical Originist Objection). Let

$$F : \mathbf{C} \rightarrow \mathbf{D}$$

be a representation of a history-bearing category. If F identifies morphisms whose distinction is required by a future provenance, admissibility, or continuation judgment, then F is too coarse for that judgment even when it preserves every endpoint relevant to the present task.

This objection does not oppose abstraction.

Category theory itself proceeds by finding the correct level of abstraction.

The objection concerns the word “correct”.

A quotient appropriate for one inference can be destructive for another.

The loss becomes visible only when histories are allowed to remain distinct long enough to ask what the quotient has done to them.

E.32. Descent as the Primitive Candidate

The essay began by asking whether the primitive object should be the state

$$x,$$

the trajectory

$$\gamma,$$

the admissibility class

$$[\gamma]_{\Lambda},$$

or the provenance graph

$$\mathcal{G}.$$

The categorical analysis does not force a single answer.

It does, however, establish an ordering of expressive capacity.

A bare object records less than an object together with its incoming and outgoing morphisms.

A single morphism records less than the branching category in which alternative morphisms remain available.

A quotient category may recover tractability while discarding distinctions among those morphisms.

A provenance enrichment may restore some of what the quotient forgets.

Thus there is no representation-free primitive waiting to be discovered by notation alone.

The selection of primitive structure determines which histories can still be distinguished.

That selection therefore has provenance consequences of its own.

E.33. *What the Category Adds*

The path-category formulation adds no new literary thesis to the essay.

It shows that the distinctions already extracted from Card, Zebrowski, and Le Guin possess a common compositional structure.

Origin is an incoming-morphism problem.

Continuation is an admissible outgoing-morphism problem.

Return is an endomorphism problem.

Branching is multiplicity of outgoing morphisms.

Convergence is multiplicity of incoming morphisms.

Irreversibility is failure of general invertibility.

Compression can appear as non-cancellation.

Reconstruction is postcomposition and therefore cannot separate histories already identified upstream.

Archival side information enriches the representation rather than reversing the loss.

World-continuation lifts the same structure to a category whose objects are candidate world realizations.

Nothing in this formalization requires the endpoint to disappear.

It requires only that the endpoint cease to monopolize the ontology.

PATH-CATEGORY THESIS
The state tells us where an arrow ends. It does not tell us which arrow occurred.

This is enough to connect the formal apparatus back to the sentence around which the essay has repeatedly circled:

continuity is a property of trajectories, not of states .

Even this sentence now requires one qualification.

A trajectory may itself be too thin if branching alternatives, provenance relations, admissibility constraints, or world-level gluing are relevant.

The primitive may therefore be not a path but a structured space of possible paths.

That question is left open deliberately.

Closing it by fiat would reproduce exactly the operation this essay has spent its length learning to inspect.

MOVEMENT VI. PROVENANCE TYPES, EPISTEMIC ANNOTATION, AND THE $[\omega?]$ WOUND

What changes when provenance ceases to be metadata attached to a proposition and becomes part of the proposition's epistemic type?

A citation normally answers a question adjacent to a claim. It tells the reader where to look for support, attribution, or prior discussion. The claim itself is ordinarily treated as unchanged by the citation attached to it.

The apparatus used throughout this essay makes a stronger distinction. Identical linguistic content can arrive through different histories. One copy may have been inspected directly. Another may have been reconstructed from a summary. A third may have passed through repeated compression and regeneration. A fourth may have a derivational history that certainly exists but can no longer be recovered.

These propositions may say exactly the same thing.

They need not occupy the same epistemic position.

The notation $[0]$, $[1]$, $[2]$, and the longer transformation words used in the main text are therefore not intended as decorative citation styles. They encode properties of a derivational trajectory. The exceptional tag $[\omega?]$ marks a different failure: not a known large generation count, but the loss of our ability to establish what the generation count or transformation history was.

That distinction permits the essay's typographic conceit to be stated formally. A proposition has content. Its occurrence has provenance. Our knowledge of that provenance is a third object. Truth, derivation, and provenance knowledge can therefore change independently.

F.1. Content Is Not Occurrence

Let

$$\Phi$$

be a space of propositional contents.

An element

$$\varphi \in \Phi$$

represents what is asserted.

Now let

$$O(\varphi)$$

denote the set of concrete occurrences or realizations of that content.

Two occurrences

$$o_1, o_2 \in O(\varphi)$$

may therefore satisfy

$$\text{Content}(o_1) = \text{Content}(o_2) = \varphi$$

while

$$o_1 \neq o_2.$$

The distinction is elementary but indispensable.

Provenance belongs first to occurrences and histories, not to abstract propositional content considered without realization.

F.2. The Provenance-Typed Proposition

Let D be a space of provenance descriptions.

Define a provenance-typed claim as a pair

$$\widehat{\varphi} = (\varphi, \pi),$$

where

$$\varphi \in \Phi$$

and

$$\pi \in D.$$

The projection

$$\text{Content} : \Phi \times D \rightarrow \Phi$$

is given by

$$\text{Content}(\varphi, \pi) = \varphi.$$

The provenance projection is

$$\text{Prov} : \Phi \times D \rightarrow D$$

with

$$\text{Prov}(\varphi, \pi) = \pi.$$

Consequently,

$$(\varphi, \pi_1) \neq (\varphi, \pi_2)$$

whenever

$$\pi_1 \neq \pi_2,$$

even though

$$\text{Content}(\varphi, \pi_1) = \text{Content}(\varphi, \pi_2).$$

The essay's notation

$$\varphi^{[0]}, \quad \varphi^{[1]}, \quad \varphi^{[3:R \circ C \circ R]}$$

is shorthand for such typed occurrences.

F.3. Generation as a Provenance Observable

Let

$$\gamma = (o_0 \xrightarrow{T_1} o_1 \xrightarrow{T_2} \dots \xrightarrow{T_n} o_n)$$

be a derivational history.

Define the generation-depth observable

$$g(\gamma) = n.$$

A directly inspected source occurrence has

$$g(\gamma) = 0$$

relative to the selected source boundary.

A first-generation reconstruction has

$$g(\gamma) = 1.$$

More generally,

$$\varphi^{[n]}$$

asserts that the occurrence carrying φ lies at known derivational depth n .

Generation depth is therefore not a measure of semantic error.

One may have

$$\text{Content}(o_0) = \text{Content}(o_n)$$

while

$$g(o_0) \neq g(o_n).$$

This is the smallest possible formal example of

reconstructed spans encountered: 2

LuaLaTeX

state $\neq$ history.

F.4. Depth Is Too Coarse

Generation count forgets which transformations occurred.

Let

$$\mathcal{T} = \{R, C, S, E, \dots\}$$

be an alphabet of transformation classes.

A history determines a transformation word

$$w(\gamma) = T_n \circ \dots \circ T_2 \circ T_1.$$

Two histories can satisfy

$$g(\gamma_1) = g(\gamma_2)$$

while

$$w(\gamma_1) \neq w(\gamma_2).$$

For example,

$$w(\gamma_1) = R \circ C \circ R$$

and

$$w(\gamma_2) = C \circ R \circ R$$

both have depth three.

Thus

$$[3]$$

is insufficient whenever transformation order matters.

The fuller annotation

$$[3 : R \circ C \circ R]$$

retains strictly more provenance information.

F.5. A Composite Provenance Type

For the purposes of this essay, define a provenance record schematically by

$$\pi = (g, w, \iota, p),$$

where g is generation depth, w a transformation word, ι an invariant-preservation descriptor, and p an epistemic confidence assigned to the provenance reconstruction.

Thus the notation

$$\varphi^{[3:R \circ C \circ R; \mathcal{I}^+; p=.71]}$$

abbreviates a typed proposition whose provenance record contains

$$g = 3,$$

$$w = R \circ C \circ R,$$

$$\iota = \mathcal{I}^+,$$

and

$$p = .71.$$

The confidence coordinate refers to confidence in the provenance characterization unless explicitly stated otherwise.

It is not automatically confidence in the truth of φ .

F.6. Orthogonal Questions

Let

$$\text{Truth} : \Phi \rightarrow \{0, 1\}$$

be a truth valuation in a setting where bivalent notation is appropriate.

Let

$$\text{Prov} : \widehat{\Phi} \rightarrow D$$

be the provenance projection on typed propositions.

Then

$$\text{Truth}(\varphi)$$

and

$$\text{Prov}(\widehat{\varphi})$$

answer different questions.

The first asks whether the proposition is true.

The second asks how this occurrence of the proposition was derived.

Consequently,

$$\text{Truth}(\varphi) \neq \text{Prov}(\widehat{\varphi})$$

not merely in value but in type.

More importantly, a change in one need not imply a change in the other.

Proposition F.1 (Truth-provenance independence). *Two occurrences may have identical propositional content and therefore the same truth value while possessing distinct provenance records.*

Proof. Let

$$\widehat{\varphi}_1 = (\varphi, \pi_1)$$

and

$$\widehat{\varphi}_2 = (\varphi, \pi_2)$$

with

$$\pi_1 \neq \pi_2.$$

Since both project to the same content φ ,

$$\text{Truth}(\text{Content}(\widehat{\varphi}_1)) = \text{Truth}(\varphi) = \text{Truth}(\text{Content}(\widehat{\varphi}_2)).$$

Yet by construction,

$$\text{Prov}(\widehat{\varphi}_1) \neq \text{Prov}(\widehat{\varphi}_2).$$

□

F.7. Provenance Is Not Evidence Strength

A second distinction is required.

A low generation count does not guarantee that a proposition is well supported.

A directly inspected source can be wrong.

Likewise, a high generation count does not entail falsehood.

A repeatedly copied mathematical identity may remain exactly correct.

Let

$$E(\varphi)$$

denote evidential support for a proposition and let

$$g(\widehat{\varphi})$$

denote generation depth.

There is no universal monotone law

$$E(\varphi) = f(g(\widehat{\varphi})).$$

Generation depth may affect reliability under a particular transformation process.

It is not itself reliability.

This prevents the provenance notation from becoming a disguised hierarchy of truth.

F.8. The Epistemic Layer

So far π has represented actual provenance.

An observer does not necessarily know π .

Let

$$K_t(\pi)$$

denote the observer's epistemic state concerning provenance at time t .

For example,

$$K_t(\pi) = \{\pi\}$$

may represent exact provenance knowledge.

A set

$$K_t(\pi) = \{\pi_1, \pi_2, \pi_3\}$$

may represent unresolved alternatives.

A probability distribution

$$\mu_t(\pi)$$

may encode graded uncertainty.

The important distinction is therefore among

$$\varphi, \quad \pi, \quad K_t(\pi).$$

These are respectively content, derivation, and knowledge of derivation.

F.9. Content Change, History Change, Knowledge Change

Consider a typed occurrence

$$\widehat{\varphi}_t = (\varphi_t, \pi_t, K_t(\pi_t)).$$

Three changes must be distinguished.

A content change occurs when

$$\varphi_t \neq \varphi_{t+1}.$$

A derivational change occurs when a new transformation extends the history:

$$\pi_t \neq \pi_{t+1}.$$

An epistemic provenance change occurs when

$$K_t(\pi) \neq K_{t+1}(\pi)$$

while both

$$\varphi_t = \varphi_{t+1}$$

and

$$\pi_t = \pi_{t+1}.$$

The last case is the one enacted by the wound.

Nothing happened to the proposition.

Nothing happened to its past.

Something happened to what could responsibly be said about that past.

F.10. $[\?]$ as Unresolved Provenance

The ordinary tag

$$[\?]$$

means that the provenance class required by the current discussion has not been established.

Formally, if

$$\Pi$$

is the relevant provenance space, then

$$[\?]$$

indicates that the epistemically admissible set

$$K_t(\pi) \subseteq \Pi$$

contains more than one live possibility.

The notation makes no claim that the provenance is intrinsically unrecoverable.

Further archival work may reduce

$$K_t(\pi)$$

to a singleton.

Thus

$$[\?]$$

means unresolved.

It does not yet mean lost.

F.11. What $[\omega?]$ Means

The exceptional tag

$$[\omega?]$$

marks a stronger condition.

It does not mean

$$g(\gamma) = \omega.$$

Nor does it mean that infinitely many transformations literally occurred.

The symbol ω is used here as a visual marker for unbounded or unrecoverably open derivational depth.

Let

$$\Pi_{\text{recoverable}}(E)$$

be the provenance distinctions recoverable from the surviving evidence E .

Then

$$[\omega?]$$

marks a case in which the provenance coordinate required by the argument is not determined by E , and no currently available derivation establishes a finite exact generation count or transformation word.

Schematically,

$$K_t(g) = \{n \in \mathbb{N} : n \text{ remains compatible with } E\}$$

may be unbounded.

The tag therefore means not “infinite history” but “derivational depth no longer responsibly bounded by the available record”.

F.12. Scarcity as Semantics

The preamble enforces that

$$[\omega?]$$

may occur only once.

This is not merely a typographic joke.

The ordinary uncertainty tag already handles routine provenance ambiguity.

If every unresolved claim received

$$[\omega?],$$

the symbol would cease to distinguish ordinary uncertainty from a specific failure of provenance recovery.

Its scarcity is therefore part of its semantics.

The compile-time constraint

$$N_{\omega?} \leq 1$$

acts as a tiny formal discipline imposed upon the document itself.

The source file refuses a second use unless the author deliberately changes the rule.

F.13. The Wound as an Epistemic Event

Let the proposition planted in Movement I be

$$\varphi.$$

At its first occurrence, suppose the essay represented its provenance as

$$\widehat{\varphi}_{t_0} = \varphi^{[0]}.$$

The reader was therefore licensed to infer

$$K_{t_0}(g) = \{0\}.$$

Movement IV revises that status.

The proposition's wording remains

$$\varphi.$$

Its truth conditions remain those of φ .

Its actual historical derivation, whatever it was, has not retroactively changed.

What changes is the warranted provenance description:

$$K_{t_1}(g) \neq K_{t_0}(g).$$

If the surviving derivational record is insufficient to establish any bounded exact depth, the annotation becomes

$$\varphi^{[\omega?]}.$$

Hence

$$\text{Content}_{t_0}(\varphi) = \text{Content}_{t_1}(\varphi),$$

while

$$K_{t_0}(\text{Prov}(\varphi)) \neq K_{t_1}(\text{Prov}(\varphi)).$$

That is the wound.

F.14. Discovery Is Not Derivation

It would be a mistake to say that the proposition's provenance changed when the essay discovered its uncertainty.

Let the actual provenance be

$$\pi^*.$$

Then before and after the discovery,

$$\pi_{t_0}^* = \pi_{t_1}^*.$$

Only the epistemic representation changes:

$$K_{t_0}(\pi^*) \neq K_{t_1}(\pi^*).$$

This gives the precise distinction requested by the main argument:

$$\text{history} \neq \text{knowledge of history}.$$

An Originist must track both.

Otherwise uncertainty about provenance can be mistaken for instability in the past itself.

F.15. Revision Without Semantic Revision

Define a provenance-revision operator

$$\mathcal{U}_E$$

acting on epistemic provenance states.

Given new evidence E' ,

$$\mathcal{U}_{E'} : K_t(\pi) \mapsto K_{t+1}(\pi).$$

A pure provenance revision satisfies

$$\text{Content}_{t+1} = \text{Content}_t$$

while

$$K_{t+1}(\pi) \neq K_t(\pi).$$

Thus a document may require revision even when none of its propositional sentences requires rewriting.

The revision concerns what the document claims to know about its own derivation.

This is one reason provenance cannot be reduced to bibliography.

F.16. Two Confidence Coordinates

The fuller notation can be refined by separating two probabilities.

Let

$$p_T$$

represent confidence assigned to the truth or correctness of the content under a specified epistemic model.

Let

$$p_P$$

represent confidence assigned to the provenance reconstruction.

Then a fully explicit typed claim could be written

$$\varphi^{[3:R \circ C \circ R; J^+; p_T=.94; p_P=.71]}.$$

The main text suppresses this distinction unless needed, because the notation would otherwise become unreadable.

Conceptually, however,

$$p_T \neq p_P$$

must remain possible.

One may be highly confident that a proposition is correct while uncertain about where it came from.

Conversely, one may know exactly where a false proposition came from.

F.17. A Useful Counterexample

Suppose a source S states a false proposition

$$\psi.$$

The source is inspected directly.

Then the occurrence may correctly carry

$$\psi^{[0]}.$$

Its provenance status is excellent.

Its truth status is not.

Thus

$$\text{Prov}(\psi^{[0]})$$

can be maximally well established while

$$\text{Truth}(\psi) = 0.$$

This counterexample prevents the entire provenance apparatus from being misread as a surrogate truth calculus.

F.18. The Converse Counterexample

Now suppose a true proposition

$$\chi$$

passes through a chain

$$\chi_0 \xrightarrow{R} \chi_1 \xrightarrow{C} \chi_2 \xrightarrow{R} \chi_3$$

without semantic alteration:

$$\text{Content}(\chi_0) = \text{Content}(\chi_1) = \text{Content}(\chi_2) = \text{Content}(\chi_3) = \chi.$$

Then

$$\text{Truth}(\chi) = 1$$

throughout, while the final occurrence has provenance

$$\chi^{[3:R \circ C \circ R]}.$$

Truth has remained fixed.

History has grown.

The two coordinates are therefore demonstrably independent.

F.19. Typing Rules

The notation may be understood as a lightweight type system.

Write

$$\Gamma \vdash \varphi : \pi$$

to mean that under provenance context Γ , the occurrence of φ is assigned provenance type π .

A direct-source rule has schematic form

$$\frac{\varphi \text{ inspected in designated source } S}{\Gamma \vdash \varphi : [0]}.$$

A reconstruction rule may take the form

$$\frac{\Gamma \vdash \varphi : [n : w] \quad R(\varphi) = \varphi'}{\Gamma \vdash \varphi' : [n + 1 : R \circ w]}.$$

reconstructed spans encountered: 2

LuaLaTeX

A compression rule is analogous:

$$\frac{\Gamma \vdash \varphi : [n : w] \quad C(\varphi) = \varphi'}{\Gamma \vdash \varphi' : [n + 1 : C \circ w]}.$$

These rules propagate derivational information even when

$$\varphi' = \varphi.$$

F.20. Failure of Derivational Typing

Suppose the available evidence does not determine whether

$$\varphi$$

was copied directly, reconstructed once, or regenerated through several intermediate states.

Then no exact rule justifies

$$\Gamma \vdash \varphi : [n : w].$$

The responsible judgment is instead

$$\Gamma \vdash \varphi : [?].$$

If the available record additionally fails to bound the relevant derivational depth, the exceptional judgment is

$$\Gamma \vdash \varphi : [\omega?].$$

This notation records a failure of derivational knowledge rather than filling the gap with a guessed history.

F.21. Content Equality Does Not License Typed Substitution

Suppose

$$\varphi^{[0]}$$

and

$$\varphi^{[3:R \circ C \circ R]}$$

have identical content.

At the untyped semantic level one may substitute one occurrence for the other where only content matters.

At the provenance-typed level, unrestricted substitution is invalid.

Proposition F.2 (Typed substitution failure). *If*

$$\pi_1 \neq \pi_2,$$

then content equality

$$\text{Content}(\varphi, \pi_1) = \text{Content}(\varphi, \pi_2)$$

does not imply equality of the typed claims.

This is the proposition-level analogue of the failure of state equality to determine trajectory equality.

F.22. Why the Apparatus Is in the Footnotes

The footnote is particularly suited to this experiment because it normally occupies a subordinate bibliographic role.

Here it carries an additional state variable.

A footnote attached to

$$\varphi$$

may identify a source while the superscript attached to the claim specifies how the present occurrence relates derivationally to that source.

Thus the bibliography answers

Which source is relevant?

while the provenance annotation answers

What happened between that source and this occurrence?

These questions overlap.

They are not identical.

F.23. The Page Does Not Display the Whole Type

Even the elaborate notation of this essay does not display complete provenance.

Let

$$\pi$$

be the full provenance record and let

$$D_{\text{page}}(\pi)$$

be the displayed annotation.

Then

reconstructed spans encountered: 2

LuaLaTeX

$$D_{\text{page}}$$

is itself a quotient.

Many complete provenance histories may produce the same visible tag.

For example,

$$D_{\text{page}}(\pi_1) = D_{\text{page}}(\pi_2) = [2]$$

even though

$$\pi_1 \neq \pi_2.$$

The essay therefore cannot escape its own Originist objection.

It can only make its chosen losses explicit.

F.24. This PDF Has a Trajectory

Let

$$D_0$$

be an initial source file and let successive editing, compilation, correction, and reconstruction operations produce

$$D_0 \xrightarrow{E_1} D_1 \xrightarrow{E_2} D_2 \xrightarrow{K} P_1 \xrightarrow{K} P_2,$$

where K denotes compilation.

The final PDF P_2 is an endpoint.

It does not contain, merely by existing, the complete derivational chain that produced it.

Two byte-identical PDFs could have different source histories.

Thus even

$$P_A =_{\text{byte}} P_B$$

does not imply

$$\text{Prov}(P_A) = \text{Prov}(P_B).$$

The essay's own artifact therefore instantiates the distinction it argues for.

F.25. Compilation and Self-Knowledge

The preamble's insistence on multiple compilation passes is intentionally minor but structurally apt.

On an early pass, the document may not yet possess resolved information about cross-references or counters whose values depend upon the compiled whole.

After another pass, the visible document can incorporate information generated by its prior compilation state.

Schematically,

$$S_0 \xrightarrow{K} S_1 \xrightarrow{K} S_2.$$

The final state

$$S_2$$

contains information that depends upon the trajectory

$$S_0 \rightarrow S_1 \rightarrow S_2.$$

This does not make LaTeX compilation metaphysically profound.

It makes it an unusually literal local example of a document whose present display depends upon its own prior states.

F.26. The Limit of the Device

The self-application of provenance notation must remain subordinate to the argument.

The essay is not primarily about its own footnotes.

Its apparatus serves as a controlled demonstration of a more general claim.

Card's archives concern historical descent [1].

Zebrowski's transformations concern future continuation [2].

Le Guin's departures, returns, and dissemination concern recurrence and branching [3].

The document's provenance notation supplies a fourth case at a deliberately smaller scale.

Its function is evidential and performative, not foundational.

F.27. The Formal Payoff

Theorem F.3 (Epistemic wound theorem). *Let a proposition occurrence have fixed content φ and fixed actual provenance π^* . If new evidence changes the warranted epistemic state from*

$$K_0(\pi^*)$$

to

$$K_1(\pi^*)$$

with

$$K_0(\pi^*) \neq K_1(\pi^*),$$

then the epistemic type of the occurrence changes even though neither its content nor its actual history changes.

Proof. The enriched occurrence is represented by

$$\widehat{\varphi}_t = (\varphi, \pi^*, K_t(\pi^*)).$$

By hypothesis,

$$\varphi_0 = \varphi_1$$

and

$$\pi_0^* = \pi_1^*,$$

while

$$K_0(\pi^*) \neq K_1(\pi^*).$$

Therefore

$$\widehat{\varphi}_0 \neq \widehat{\varphi}_1$$

at the epistemic-type level despite invariance of content and actual derivation. □

This is exactly the distinction enacted when a proposition formerly marked

$$[0]$$

must later be marked

$$[\omega?].$$

F.28. Do Not Invent the Missing Path

The formal apparatus yields a simple methodological rule.

Originist Objection F.4 (Originist Rule of Responsible Annotation). When the surviving evidence fails to determine a derivational path, a representation should preserve the uncertainty rather than silently replace the missing path with the most convenient reconstruction.

This rule is the epistemic counterpart of preserving branching in the path category.

If several histories remain admissible, the representation should not collapse them merely because one endpoint description is easier to print.

F.29. Later Knowledge Can Be Worse

One might expect provenance knowledge to improve monotonically as inquiry continues.

That expectation is false.

New evidence can reveal that an apparently secure derivation was less secure than previously believed.

Thus an epistemic sequence may move from

[0]

to

[?]

or even

$[\omega?]$.

This is not a contradiction.

The earlier tag represented an earlier epistemic state.

The later tag represents a revision of what was warranted.

Provenance inquiry is therefore itself historical.

Its judgments have trajectories.

F.30. The Provenance of Provenance Claims

Once provenance claims are treated as claims, they too possess provenance.

Let

$$\rho = \text{“the occurrence of } \varphi \text{ is generation zero”}.$$

Then ρ has its own derivational history.

One may therefore write schematically

$$\rho^{[1]} : \varphi^{[0]}.$$

The outer annotation concerns the provenance of the provenance judgment.

The inner annotation concerns the provenance attributed to φ .

This recursion can continue.

There is no practical reason to display it indefinitely.

The important fact is that provenance annotation does not create an epistemically privileged metalanguage immune to the theory.

F.31. Operational Closure

The regress of provenance-about-provenance is stopped operationally rather than metaphysically.

For a task τ , retain provenance information only until additional provenance distinctions cease to alter the admissible judgments required by τ .

If

$$P_k$$

denotes provenance retained to order k , choose k such that

$$J_\tau(P_k) = J_\tau(P_{k+1})$$

for all distinctions relevant to the task.

This is the same closure principle governing the essay as a whole.

One stops not because every possible distinction has been exhausted, but because further extension no longer changes the structure needed by the argument.

F.32. What the Notation Actually Claims

The provenance typography can now be stated without metaphor.

The expressions

$$\varphi^{[0]}$$

and

$$\varphi^{[3:R \circ C \circ R]}$$

may have identical propositional content.

They are nevertheless different typed occurrences because their derivational coordinates differ.

Likewise,

$$\varphi^{[?]}$$

and

$$\varphi^{[\omega?]}$$

distinguish ordinary unresolved provenance from a stronger failure to bound or recover the derivational depth relevant to the inquiry.

Typography is therefore functioning as a visible projection of a provenance type system.

It does not make the type system complete.

It makes one otherwise invisible coordinate legible.

F.33. The Wound and the Thesis

The planted wound now returns the essay to its simplest distinction.

Suppose the sentence is unchanged.

Suppose its truth value is unchanged.

Suppose even its actual derivational history is unchanged.

The reader can nevertheless learn that the earlier representation of that history was unjustified.

Nothing about the terminal string reveals this.

Only the document's trajectory does.

*The proposition did not change.
Its history did not change.
What changed was whether the history could still be known.*

The distinction among

Content, Prov, $K(\text{Prov})$

therefore completes the provenance apparatus required by the essay.
It also prevents the slogan

state $\neq$ history

from becoming too simple.
There are at least three layers:

state, history, knowledge of history.

A representation may preserve the first while losing the second.
An archive may preserve the second while an observer loses access to it.
A reconstruction may recover enough of the second to support one judgment but not another.
And a proposition may remain word-for-word unchanged while moving from apparent certainty to an explicit wound.

PROVENANCE-TYPE THESIS
<i>What a statement says, how this occurrence came to say it, and what we know about how it came to say it are three different objects.</i>

This appendix completes the formal apparatus.
What remains is not another extension of the stack but its bibliographic grounding: the primary literary works and the secondary sources required by the argument. The references that follow should therefore remain deliberately ordinary. After a document devoted to the difference between content and derivation, the bibliography need not perform another trick.

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$state \neq history$

*The inequality is printed in the final state of the document.
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